

# Sheet (1)

## Cartesian Product

### The ordered pair

(a , b) is called an ordered pair

- a is called the first projection
- b is called the second projection

#### Notice that :

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- 1  $(a,b) \neq \{a,b\}, (a,b) \neq [a,b]$
- 2 The element in the ordered pair can be repeated while that cannot happen in the sets.

#### ש For example :

We say the ordered pair (2, 2) while we cannot say  $\{2, 2\}$  but we say  $\{2\}$ 

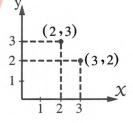
3 There is an empty set which is denoted by  $\emptyset$  while there is not an empty ordered pair.

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- 4  $(a,b) \neq (b,a)$  where  $a \neq b$
- **¥** For example:  $(2,3) \neq (3,2)$

Notice that: (2,3) and (3,2)

are represented by two different points as shown in the opposite graph.



### The equality of two ordered pairs

If 
$$(a,b) = (x,y)$$
, then  $a = x$ ,  $b = y$  limits also limits  $a = x$ 

#### ץ For example :

- If (a, b) = (3, -4), then a = 3, b = -4
- If (X, 2) = (-5, y), then X = -5, y = 2

### **Example**

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Find the values of X and y in each of the following if:

1 
$$(x^2-1,8)=(48,\sqrt[3]{y})$$

2 
$$(32, x + y) = (y^5, 2)$$

#### The Cartesian product of two finite sets and representing it

For any two finite and non empty sets X and Y, we get:

- 1 The Cartesian product of the set X by the set Y and it is denoted by  $|Y \times X|$  is the set of all ordered pairs whose first projection of each of them belongs to X and the second projection of each of them belongs to Y i.e.  $X \times Y = \{(a, b) : a \in X, b \in Y\}$
- ¥ For example:

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If 
$$X = \{1, 2\}$$
,  $Y = \{5, 7, 8\}$ , then

$\mathbf{Y}_{\mathbf{Y}}\mathbf{Y} = \begin{bmatrix} 1 & 2 \\ 1 & 2 \end{bmatrix} \times \begin{bmatrix} 5 & 7 & 8 \end{bmatrix}$			Secon	Second projection		
$X \times Y = \{1, 2\} \times \{5, 7, 8\}$		X	5	7	8	
$= \{(1,5), (1,7), (1,8), (2,5), $	First	1	(1,5)	(1,7)	(1,8)	
(2,7),(2,8)	projection	2	(2,5)	(2,7)	(2,8)	

The opposite table helps us to get  $X \times Y$ 

We can represent  $X \times Y$  by an arrow diagram or graphical (Cartesian) diagram as follows:



The arrow diagram

The graphical diagram (The Cartesian diagram)

2 The Cartesian product of the set Y by the set X and which is denoted by  $|Y \times X|$  is the set of all ordered pairs whose first projection belongs to the set Y and the second projection belongs to the set X

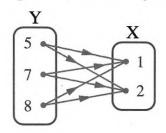
**i.e.** 
$$Y \times X = \{(a, b) : a \in Y, b \in X\}$$

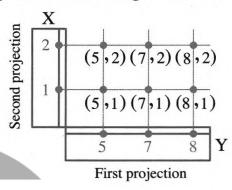
### ש For example :

If 
$$X = \{1, 2\}$$
,  $Y = \{5, 7, 8\}$ , then  $Y \times X = \{5, 7, 8\} \times \{1, 2\}$ 

$$= \{(5,1),(5,2),(7,1),(7,2),(8,1),(8,2)\}$$

We can represent  $Y \times X$  by an arrow diagram or by a Cartesian diagram as follows:





The arrow diagram

The Cartesian diagram

### **Remarks**

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## ## From the previous, we notice that:

•  $X \times Y \neq Y \times X$  where  $X \neq Y$ 

because  $(1, 5) \neq (5, 1)$ 

We say  $X \times Y = Y \times X$  at the following cases:

- (1) X = Y
- 2 One of the two sets =  $\emptyset$

«  $X \times \emptyset = \emptyset \times X = \emptyset$  because  $\emptyset$  has no elements »

3 The Cartesian product of the set X by itself and we denote it by  $X \times X$  in the same times it is denoted by  $X^2$  (it is read X two) is the set of all ordered pairs whose first projections and second projections belong to X

**i.e.**  $X \times X = \{(a, b) : a \in X, b \in X\}$ 

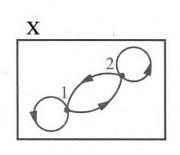
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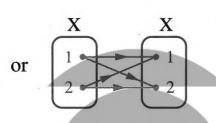
#### For example:

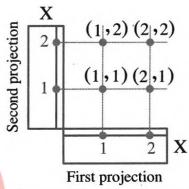
If $X = \{1, 2\}$ , then
$X \times X = \{1, 2\} \times \{1, 2\}$
$= \{(1,1),(1,2),(2,1),(2,2)\}$

			Second projection		
	×	1	2		
First	1	(1,1)	(1,2)		
projection	2	(2,1)	(2,2)		

We can represent  $X \times X$  by an arrow diagram or Cartesian diagram as follows :







The arrow diagram

Cartesian diagram

### Remark

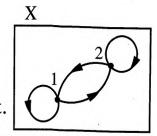
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The ordered pairs in which the first projection equals the second projection in the previous Cartesian product (1, 1)

, (2, 2) are represented in the arrow diagram by

a loop to show that the arrow goes and returns to the same point.



### Remarks

If we denote the number of elements of any set by «n» then from the previous example , we find that :

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• 
$$n(X) = 3$$
,  $n(Y) = 2$ 

i.e. 
$$1 n(X \times Y) = n(Y \times X) = n(X) \times n(Y)$$

$$2 n(X \times X) = (n(X))^2$$

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# Remark

If:  $(a,b) \in X \times Y$ , then  $a \in X, b \in Y$ 

צ For example :

If:  $(3,5) \in X \times Y$ , then  $3 \in X, 5 \in Y$ 

#### The Cartesian product of two infinite sets

• We know that if X is a finite set (having n elements), then the Cartesian product  $X \times X$  is also a finite set (having  $n^2$  elements).

For example: If n(X) = 3, then  $n(X \times X) = 9$ 

• But if X is an infinite set, then  $X \times X$  is an infinite set also

As examples for that

$$\mathbb{N} \times \mathbb{N} = \{(x, y) : x \in \mathbb{N}, y \in \mathbb{N}\}, \mathbb{Z} \times \mathbb{Z} = \{(x, y) : x \in \mathbb{Z}, y \in \mathbb{Z}\},$$

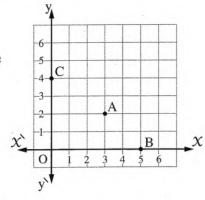
$$\mathbb{Q} \times \mathbb{Q} = \{(x, y) : x \in \mathbb{Q}, y \in \mathbb{Q}\}, \mathbb{R} \times \mathbb{R} = \{(x, y) : x \in \mathbb{R}, y \in \mathbb{R}\}$$

### Representing the Cartesian product of two infinite sets

- We know that if X is a finite set , we represent the Cartesian product  $X \times X$  graphically by a finite number of points.
- But if X is an infinite set, then the Cartesian product X × X represented graphically by an infinite number of points.

### First Representing the Cartesian product $\mathbb{N} \times \mathbb{N}$ ( $\mathbb{N}^2$ )

- Represent the natural numbers on two perpendicular straight lines, one of them  $\overrightarrow{xx}$  is horizontal and the other  $\overrightarrow{yy}$  is vertical, where they intersect at the point which represents the number zero on each of them *i.e.* O = (0, 0)
- And the opposite figure shows a small part of the perpendicular graphical net of the Cartesian product  $\mathbb{N} \times \mathbb{N}$  which consists of the vertical and the horizontal straight lines that pass through the points which represent



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the natural numbers on each of  $\overrightarrow{xx}$  and  $\overrightarrow{yy}$ 

 $\bullet$  And each point of the points of this net represents an ordered pair of the Cartesian product  $\mathbb{N}\times\mathbb{N}$ 

#### For example:

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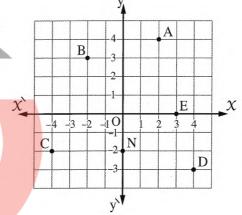
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- The point A represents the ordered pair (3, 2)
- The point B represents the ordered pair (5,0)
- The point C represents the ordered pair (0,4)
- The point O represents the ordered pair (0,0)

### Second Representing the Cartesian product $\mathbb{Z} \times \mathbb{Z}$ ( $\mathbb{Z}^2$ )

- Represent the integers on each of  $\overrightarrow{xx}$  and  $\overrightarrow{yy}$  which are intersecting at O (0,0)
- And the opposite figure shows a small part of the perpendicular graphical net of the Cartesian product  $\mathbb{Z} \times \mathbb{Z}$
- And each point of its points represents an ordered pair of the Cartesian product  $\mathbb{Z} \times \mathbb{Z}$

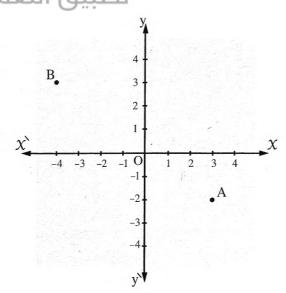


#### For example:

- The point A represents the ordered pair (2,4)
- The point B represents the ordered pair (-2,3)
- The point C represents the ordered pair (-42+2)
- The point D represents the ordered pair (4, -3)
- The point E represents the ordered pair (3,0)
- The point N represents the ordered pair (0, -2)

### Third Representing the Cartesian product $\mathbb{R} \times \mathbb{R}$ ( $\mathbb{R}^2$ )

- The perpendicular graphical net of the Cartesian product  $\mathbb{R} \times \mathbb{R}$  is an infinite extended surface from all sides and the opposite figure shows a small part of this region.
- Each point of this region represents an ordered pair of the Cartesian product  $\mathbb{R} \times \mathbb{R}$



#### For example:

- The point A represents the ordered pair (3, -2)
- The point B represents the ordered pair (-4,3)

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# (M	athematics 3 <sup>rd</sup> P	rep 1st term	****	
7	If $n(X) = 3$ (a) 4	$n (X \times Y) = 12$ , then (b) 9	n (Y) = (c) 15	(El-Kalyoubia 2011) (d) 36
8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	If: $n(X) = 5$ , (a) 1	$n (X \times Y) = 15$ , then n (b) 5	(Y) = (c) 3	(d) 15
9 9	If: $X \times Y = \{(a) \mid 1\}$	(1,3), (1,4), then note $(b)$ 2	(c) 3	(d) 4
#10 ##	If: $(3,5) \in \{3,6\}$	$\{x, 8\} \text{ then } x$	(c) 5	(d) 3
######################################	If: $(X - Y) \times$ (a) $\{1\}$	$Y = \{(1, 2), (1, 3)\}$ (b) $\{1, 2\}$		then $X = \dots$ (d) $\{1, 3, 2\}$
## 12 ## ## ## ## ## ## ## ## ## ## ## ## ##	The point (-5 (a) first	,7) lies in	nadrant. (c) third	(d) fourth
##13 ##################################	The point (-3 (a) first	, 4) lies in q (b) second	uadrant. 2024 (c) third	(d) fourth
## 14 ##################################		product $\{2\} \times \mathbb{R}$ represe to points $(2,0)$ and $(b)$ $(2,5)$		traight line passing (d) (-2,2)
### 15 ### ### #########################	The point A (5) (a) first	• -3) lies on the	البيق التعلم التربية ا (c) third	(d) fourth
## 16 ## ###############################	If the point (5 (a) zero	(b), $(b)$ $(b)$		(d) 10
# 17 # # # # # # # # # # # # # # # # # #	If the point (a) 2	(5, b – 7) is located on (b) 5	the $X$ -axis, then b = (c) 7	(d) 12
	<b>*******</b>		أو الأيفون	تطبيق مذكرات جاهزة للط الله الله الله الله الله الأخوات الله الأندرويد أو التطبيق على موبايلك الأندرويد أو دوست موقع مذكرات جاهزة للطباعة - com .

If:  $(|X|, 4) = (3, y^2)$  and the point (X, y) lies in the second quadrant, then  $X + y = \dots$  (El-Sharkia 2014)

(a) 7

(b) 1

(c) - 1

(d) - 7

If the point (X - 5, 3 - X) where  $X \in \mathbb{Z}$  is located in the third quadrant, then X equals ......

(a) 2

(b) 3

(c)4

(d) 5

Essay problems:

Find: a, b if  $(a-7, 26) = (-2, b^3 - 1)$ 

2 If (x-1, 11) = (8, y+3), then find:  $\sqrt{x+2y}$ 

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تطبيق التعلم التفاعلي عن بعد

If  $(x^2, 27) = (1, y^3)$  and the point (x, y) lies in the second quadrant, find the value of  $\sqrt[3]{y-x}$ 

Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term If  $(2 \times 4) = (8 \cdot y + 1)$ , then find the value of  $(2 \times 4) = (8 \cdot y + 1)$ If  $X = \{2, 5\}$ ,  $Y = \{1, 3, 7\}$ , then find : (1)  $X \times Y$ (2) n  $(Y^2)$ If  $X = \{3, 7\}$ ,  $Y = \{1, 2, 5\}$  Find:  $X \times Y$ ,  $n(Y^2)$ If  $X = \{2, 3\}$ , then find:  $X^2$ تطبيق التعلم التفاعلي عن بعد If  $X \times Y = \{(1, 1), (1, 3), (1, 5)\}$ Find:  $(1) X \cdot Y$ (2)  $Y \times X$ 

Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term If  $X = \{1, 3, 5\}, Y = \{4, 5\}$  Find:  $(X \cap Y) \times (X \cup Y)$ If  $X \times Y = \{(2,3), (2,2), (2,4)\}$ 10 Find each of the following: (1) X, Y (a)  $X \times (X \cap Y)$ Choose the correct answer: If: (5, x-8) = (y+1, -5), then:  $x + y = \dots$ (Aswan 201. (a) 4 (d)7(c)6If: (2, X-1) = (y, 0), then X +(d) - 3(a) 3If:  $X = \{3\}$ , then:  $X^2 = \dots$ (Cairo 2013) (b) (3,3)(a) 9  $(c) \{9\}$ (d)  $\{(3,3)\}$ If:  $X = \{5\}$ ,  $Y = \emptyset$ , then  $n(X \times Y) = \cdots$ (c) 5 (d) zero (a) 1 (b) 2\* If: n(X) = 2,  $Y = \{1, 2\}$ , then  $n(X \times Y) = \cdots$ (a) 4 (b) 3(c) 5(d) 6If:  $X = \{3\}$  and n(Y) = 4, then  $n(X \times Y) = \dots$ (a) 1 (d) 12 (c) 7 12

Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term If:  $X = \{5\}$ ,  $Y = \{3\}$ , then  $n(X \times Y) = \dots$ (a) 15 (b) 5(d) 1 (c) 3 If:  $X = \{3, 5, 6\}$ , then  $n(X^2) = \cdots$ (b) 6(c) 9 (a) 3 (d) 12 \* If:  $X \times Y = \{(6, 3), (6, 4)\}$ , then  $n(X) = \dots$ (b) 1 (a) 3 (d) 2**⊞**10 ☐ If  $(3,5) \in \{3,6\} \times \{x,8\}$ , then  $x = \dots$ (El-Behaira 2011) (d) 3 (a) 8 (b) 6(c) 5The point (-4,3) lies in the ..... quadrant. (b) second (d) fourth (a) first (c) third The point (-2, -5) lies in the ..... quadrant. (c) third (a) first (b) second (d) fourth If:  $(|X|, 4) = (3, y^2)$  and the point (X, y) lies in the second quadrant, 13 then :  $X + y = \cdots$ (a) 7(d) - 7(b) 1 The cartesian product  $\{2\} \times \mathbb{R}$  represent graphically by a straight line passing through the two points (2 + 0) and (c)(5,2)(a) (0, 2)(b) (2,5)(d)(-2,2)The point (5, -2) lies on the ..... quadrant. (a) first (b) second (c) third (d) fourth If the point (5 - X, X - 4) lies in the fourth quadrant, then the value of  $X = \cdots$ (a) 9 (c)6(d) 2(b) 8 **\*** If the point (X, 2) lies on y-axis, then  $X = \dots$ (El-Fayoum 2011) (b) 1 (c) 2(d) 3 (a) zero 13 حمَل التطبيق على موبايلك الأندرويد أو الأيفون

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Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term If  $X = \{2, 15\}$ ,  $Y = \{4, 1\}$  and  $Z = \{15\}$ Find:  $(1) Y \times Z$ (2) n ( $X^2$ ) (3)  $(X \cap Z) \times Y$ If  $X = \{1\}$ ,  $Y = \{2, 3\}$ ,  $Z = \{2, 5, 6\}$ Find: the Cartesian product  $(Z - Y) \times (X \cup Y)$ If:  $X = \{1, 2, 6\}$ ,  $Y = \{2, 4, 5, 6\}$  and  $Z = \{4\}$ Find:  $(1) X \times Y$  $(2)(X \cap Y) \times Z$ If  $X = \{1, 2\}$ ,  $Y = \{2, 5\}$ ,  $Z = \{4, 5\}$ , then: Find:  $(X \cap Y) \times (Y \cup Z)$ 

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### Sheet (2)

### Relation - Function (mapping)

#### First The relation

#### Remarks

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- 1 The relation R is a subset of the Cartesian product  $X \times Y$  i.e.  $R \subset X \times Y$
- 2 If (a, b) ∈ the relation R, then we can express that by another method, we write "a R b", it means that the element a is connected with the element b by the relation R

#### The conclusion

- 1 The relation from a set X to a set Y is a connection joining some or all the elements of X with some or all the elements of Y
- 2 If R is a relation from the set X to the set Y, then R is a set of ordered pairs where the first projection of each belongs to X and the second projection belongs to Y and the first projection connects with the second projection with respect to this relation.
- 3 The relation R from the set X to the set Y is a subset from the Cartesian product  $X \times Y$  i.e. The relation  $R \subset X \times Y$

Inversely: any subset of the Cartesian product X × Y expresses a relation from X to Y

4 The relation can be represented by an arrow diagram or by a Cartesian diagram (graphically).

#### Remark

If R is a relation from X to X , then : R is a relation on X and the relation  $R \subset X \times X$ 

#### Second Functions (Mapping)

#### Generally

#### A relation from X to Y is said to be a function if:

- 11 In the relation, each element of the set X appears only once as a first projection in one of the ordered pairs of the relation. (Notice the relation R in the previous example)
- 2 In the arrow diagram which represents the relation, each element of X has one and only one arrow going out of it to one element of Y (Notice the arrow diagram of the previous relation)
- 3 In the Cartesian diagram which represents the relation, each vertical line has one and only one point lying on it of the points which represent the relation.

  (Notice the Cartesian diagram of the previous relation)

#### Introductory example

If  $X = \{0, 1, 2, 3\}$ ,  $Y = \{0, 1, 2, 3, 4, 5, 6\}$  and R is a relation from X to Y where "a R b" means "a =  $\frac{1}{2}$  b" for each a  $\in$  X, b  $\in$  Y

Write R and represent it by an arrow diagram and a Cartesian diagram.

Solution

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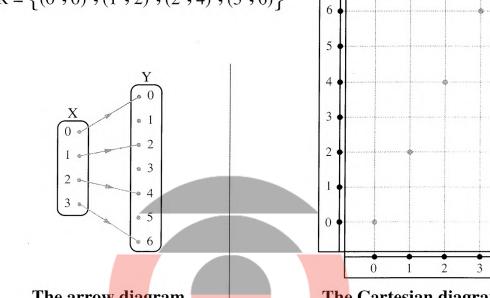
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$$R = \{(0,0), (1,2), (2,4), (3,6)\}$$



The arrow diagram

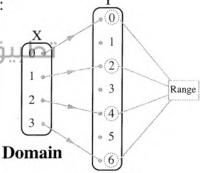
The Cartesian diagram

#### In the previous relation, we notice that:

Each element of the set X has been connected with one and only one element of the elements of the set Y

Such as , this relation is called a function or (mapping) , also :

- The set of  $X = \{0, 1, 2, 3\}$  is called "the domain of the function".
- The set of  $Y = \{0, 1, 2, 3, 4, 5, 6\}$  is called "the codomain of the function".
- The set  $\{0, 2, 4, 6\}$  is called "the range of the function" and it is a subset from the codomain of the function.



Codomain

Prime numbers = { 2 , 3 , 5 , 7 , 11 , 13 , 17 , 19 , 23 , 29 , 31 , 37 }

Odd numbers =  $\{1, 3, 5, 7, 9, 11, 13, 15, 17, 19, \ldots\}$ 

Even numbers =  $\{0, 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, \dots\}$ 

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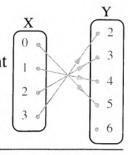
Example [8]

If  $X = \{0, 1, 2, 3\}$ ,  $Y = \{2, 3, 4, 5, 6\}$  and R is a relation from X to Y where "a R b" means "a + b = 5" for each a  $\in X$ , b  $\in Y$ Write the relation R and represent it by an arrow diagram. Mention giving reasons if R is a function from X to Y or not? And if it is a function, find its range.

Solution

•  $R = \{(0,5), (1,4), (2,3), (3,2)\}$ R represents a function from X to Y because each element of X connects with only one element of Y

The range of the function =  $\{5, 4, 3, 2\}$ 



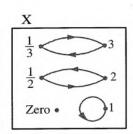
**Example** 9 If  $X = \{3, 2, 1, 0, \frac{1}{2}, \frac{1}{3}\}$ , and R is a relation on X where "a R b" means "a is the multiplicative inverse of b" for each  $a \in X$ ,  $b \in X$ 

> Write R and represent it by an arrow diagram and mention giving reasons if R represents a function or not.

Solution

• R = 
$$\{(3, \frac{1}{3}), (2, \frac{1}{2}), (1, 1), (\frac{1}{2}, 2), (\frac{1}{3}, 3)\}$$

R does not represent a function because the element zero  $\subseteq X$  does not connect with any element in X (There is no arrow going out from zero in the arrow diagram which represents the relation)



### Choose the correct answer:

If f is a function from the set X to the set Y then the domain of f is .....

(a) X

(b) Y

(c)  $X \times Y$ 

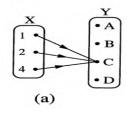
(d)  $Y \times X$ 

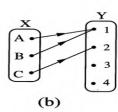
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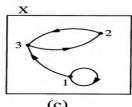
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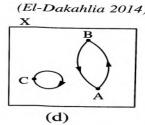
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8 8 The following figures shows four arrow diagrams one of them is not function



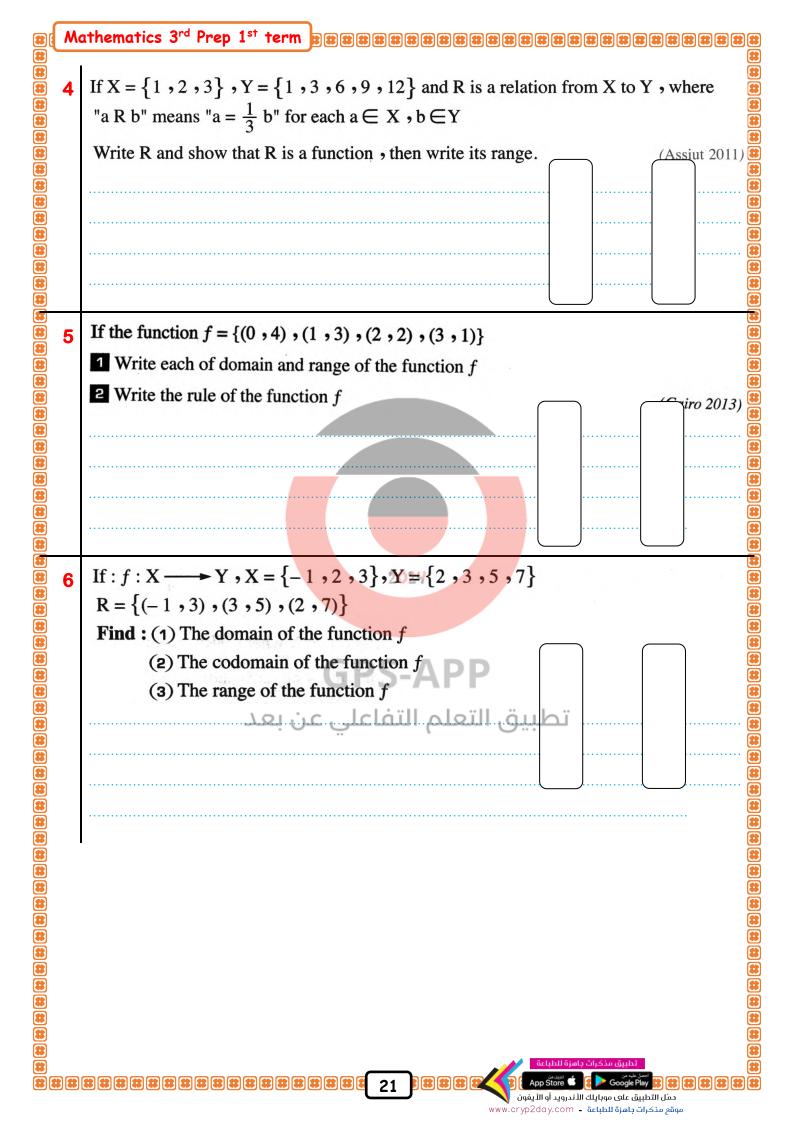




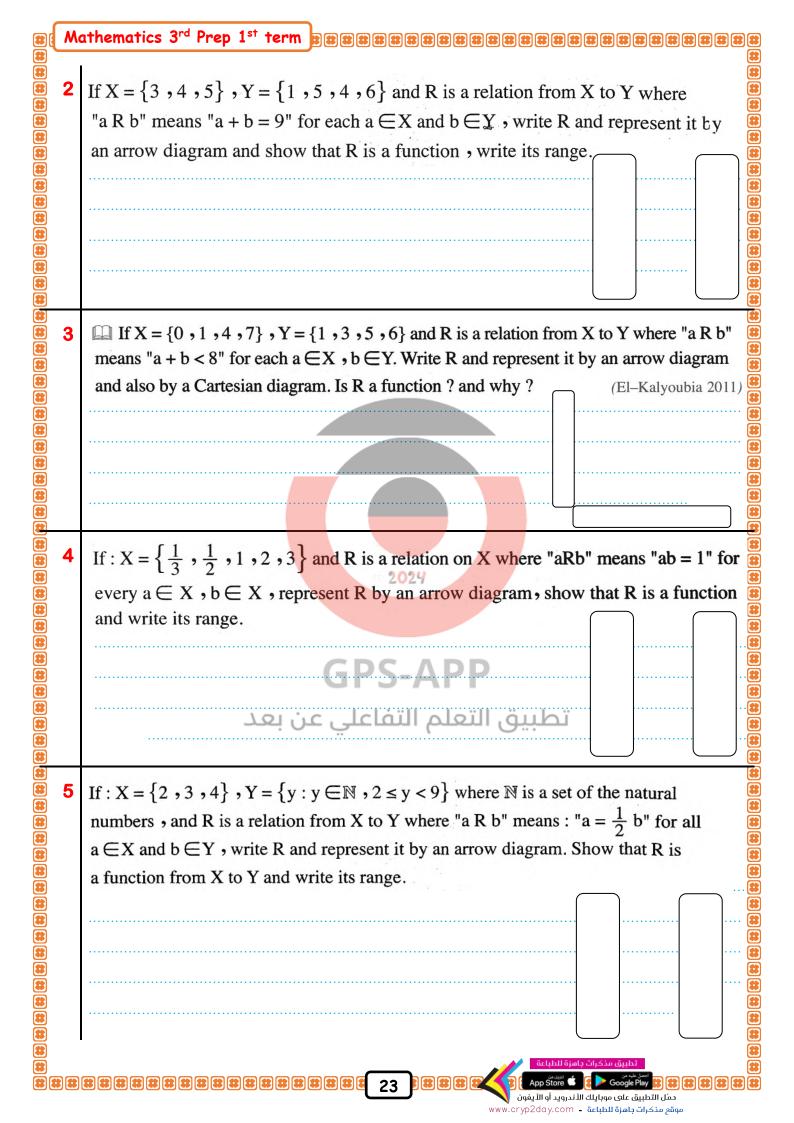


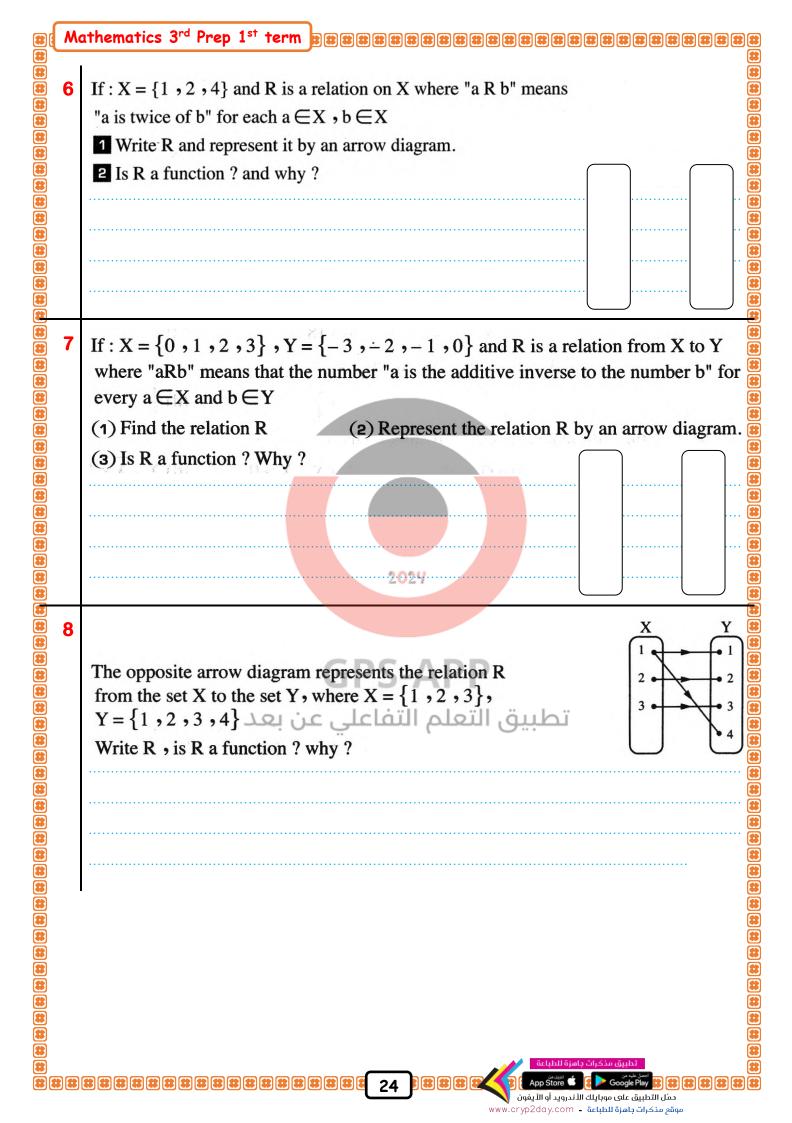
Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term REE 3 If the point (5 - x, x - 4) lies in the fourth quadrant, then the value of  $x = \dots$ **88** (a) 9 (c)6(d) 2(b) 8 If:  $X = \{1, 3, 5\}$  and R is function on X where  $R = \{(a, 3), (b, 1), (1, 5)\}$ , then the numerical value of the expression :  $a + b = \dots$ **33** \* (a) 3 (b) 4(c)5(d) 8\* 5 The opposite figure represents a function on X, its range = ..... (b)  $\{a, b, c\}$ (a)  $\{a\}$ **33 33** (d)  $\{b,c\}$ (c)  $\{a,b\}$ ## ## Which of the following relations does not represent a function from X to Y? 8 (Helwan 2011) **33** .L A 8 •M ۰M 8 (c) B (a) (d) The opposite diagram represents 8 a function on X, its range is ...... (Cairo 2011) (b)  $\{a, b, c\}$  $(a) \{a\}$ (c)  $\{a, b\}$ (d)  $\{b, c\}$ **33** If: (2, x-1) = (y + 0); then x + y = 1(c)2(d) - 3(a) 3 (b) 1 If: n(X) = 2,  $Y = \{1, 2\}$ , then  $n(X \times Y) = \cdots$ (a) 4 (b) 3 (c)5(d) 6**33** 10 If: n(X) = 5,  $n(X \times Y) = 15$ , then  $n(Y) = \dots$ (a) 1 (b) 5(c) 3 (d) 15 11 If:  $X \times Y = \{(1,3), (1,4)\}$ , then  $n(X) = \dots$ (a) 1 (c) 3 (d) 419 حمَل التطبيق على موبايلك الأندرويد أو الأيفون بوقع مذكرات جاهزة للطباعة • www.cryp2day.com

<b>33:</b> Mo	athematics 3 <sup>rd</sup> Prep	1 <sup>st</sup> term			<b>33 33 33</b>
# 12 # 12 # #	The point (-3,4)	lies in quad	drant.	(d) fourth	######################################
# 13 # 13 #	If: $(a + 1, 5) = (-1)$ (a) - 12	(b) zero	$a + b = \dots$ (c) 2	(El-Ismailia (d) 12	2014)
## 14 ## ## ##	The point $(5, -2)$ (a) first	lies on the (b) second		(d) fourth	######################################
## 15 ## ##	If the point $(x, 2)$ (a) zero	lies on y-axis, then 2 (b) 1	$X = \dots$ (c) 2	(El-Fayoum (d) 3	2011)
### Ess ## 1	"a R b" means "a +	$b = 6$ " for all $a \in X$ R a function ? and w	$, b \in Y, $ Write R	tion from X to Y whe	
2 *************************************	-		ite R and represent	ans "a + 2b = an odd it by an arrow diagra	im. 8
3 *** *** ** ** ** ** ** ** ** ** **	where "aRb" means	"a <sup>2</sup> = b" for each of a nt it by a cartesian dia	a∈X,b∈Y agram.	a relation from X to Y	



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### Sheet (3)

### Polynomial Functions Part (1)

#### The symbolic representation of the function

• The function is usually denoted by one of the following letters. f or m or q or ... and the function f from the set X to the set Y is written mathematically as:

 $f: X \longrightarrow Y$  and is read as f is a function from X to Y

or  $m: X \longrightarrow Y$  and is read as m is a function from X to Y and so on ...

• If the ordered pair (X, y) belongs to the function, then the element y is called the image of the element X by the function f and we express it by one of the following two forms:

 $f: X \longmapsto y$  it is read as f maps X to y

or f : f(X) = y it is read as f is a function where f(X) = y

#### For example:

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If  $f: X \longrightarrow Y$  where  $f: X \longmapsto X^2$ , then  $f: 3 \longmapsto 9$ 

, also can be written in the form:  $f(X) = X^2$ , hence f(3) = 9

#### Remark

The mathematical form  $f(x) = x^2$  is called the rule of the function f, and it is used to find the image of any element of the domain by the function f

#### Remember that:

- If f is a function from the set X to the set Y i.e.  $f: X \longrightarrow Y$ , then:
- 1 X is called the **domain** of the function f
- 2 Y is called the codomain of the function f
- 3 The set of images of the elements of the set X by the function f is called the range of the function f which is a subset of the codomain Y

#### **Polynomial functions**

#### Definition

The function  $f: \mathbf{R} \longrightarrow \mathbf{R}$ ,  $f(X) = \mathbf{a_0} + \mathbf{a_1} X + \mathbf{a_2} X^2 + \dots + \mathbf{a_n} X^n$ 

where  $a_0$  ,  $a_1$  ,  $a_2$  , ........ ,  $a_n$   $\in \mathbb{R}$  , n  $\in \mathbb{N}$  is called a polynomial function.

i.e. The polynomial function is a function whose rule is a term or an algebraic expression in condition that the following should be identified:

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For example: The following functions are all polynomial functions:

$$f: f(X) = 2 X + 5$$

• 
$$g : g(X) = X^2 - 2X + 1$$

• 
$$k : k(X) = 8$$

• n : n (
$$X$$
) = 1 +  $\sqrt{2} X - 9 X^3$ 

#### Remark

If the domain or the codomain of a function is not the set of real numbers, then that function is not a polynomial function.

For example:

•  $f: f(X) = \sqrt{X}$  is not a polynomial function because f(X) doesn't exist in  $\mathbb{R}$  if X equals a negative number.

For example:

 $f(-1) \notin \mathbb{R}$  because  $\sqrt{-1} \notin \mathbb{R}$ , so the domain of the function f is not the set of real numbers.

• h : h (X) =  $\frac{1}{X}$  is not a polynomial function because h(X) doesn't exist in  $\mathbb{R}$  if X equals zero.

, so the domain of the function h is not the set of real numbers.

Remark

When we search if the function is a polynomial or not, we do not simplify its rule.

For example:

تطبيق التعلم التفاعلي عن بعد The function  $f_1: f_1(x) = x\left(x + \frac{1}{x}\right)$  doesn't represent a polynomial function

because  $f_1(0) \notin \mathbb{R}$  while the function  $f_2: f_2(x) = x^2 + 1$  represents a polynomial function.

And notice that:  $\chi(x + \frac{1}{x}) = x^2 + 1$  for all real numbers except 0

The degree of the polynomial function

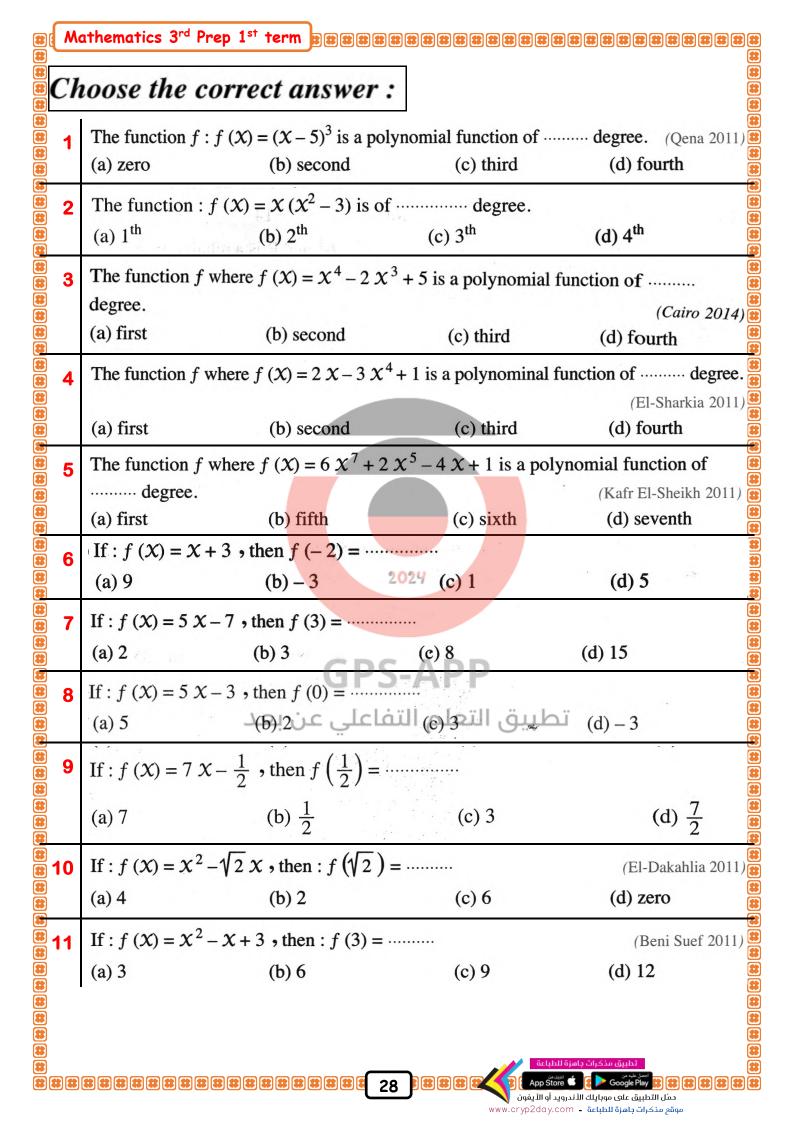
The degree of the polynomial function is the highest power of the variable in the function rule.

For example:

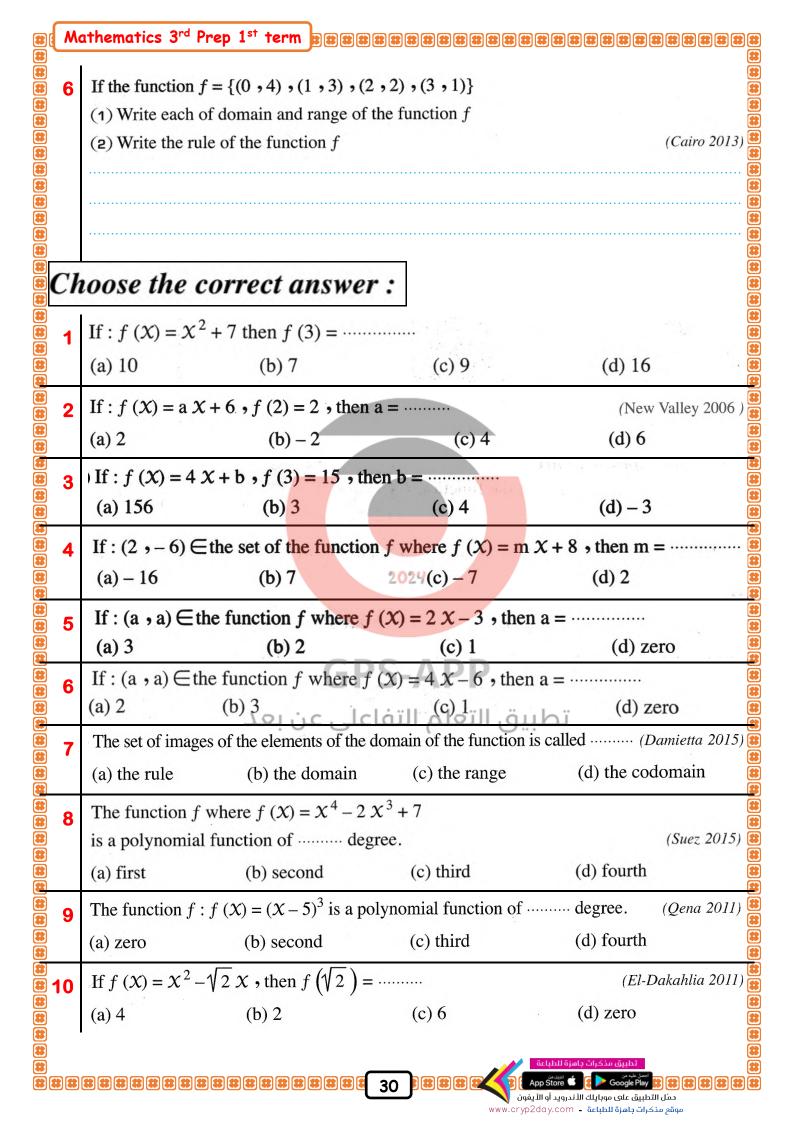
• The function  $f_1: f_1(x) = 3x - \frac{1}{2}$  is of the first degree (a linear function)

• The function  $f_2: f_2(x) = \sqrt{5}x^2 - 3x + 4$  is of the second degree (quadratic function)

• The function  $f_3: f_3(x) = x^3 - 5x^2 + 4$  is of the third degree (cubic function)



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Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term If f(X) = k X + 8, f(2) = 0, then  $k = \dots$ (El-Sharkia 2015) (d) - 4(c)4(b) 6 (a) 8 Essay problems: If:  $f(X) = X^2 - X + 3$ , then find: f(-2),  $\dot{f}(0)$ , f(1)If the function  $f = \{(0, 4), (1, 3), (2, 2), (3, 1)\}$ (1) Write each of domain and range of the function f(2) Write the rule of the function f (Cairo 2013 If the set of the function  $f = \{(1,3), (2,5), (3,7), (4,9), (5,11)\}$ (1) Write the domain and the range of the function f(2) Write the rule of the function f (Red Sea 2015 GPS-APP تطبيق التعلم التفاعلي عن بعد If f(X) = 2X - 1, then prove that: f(2) - 3f(1) = zero(El-Gharbia 201 If  $f(x) = 2x^2 - 5x + 2$ , then prove that:  $f(2) = f(\frac{1}{2})$ (Luxor 2014 31

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## Sheet (4)

## Polynomial functions Part (2)

#### The linear function **First**

#### **Definition**

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The function  $f: \mathbb{R} \longrightarrow \mathbb{R}$  where f(X) = aX + b where  $a \in \mathbb{R} - \{0\}$ ,  $b \in \mathbb{R}$  is called a linear function (it is a polynomial function of the first degree).

#### **Examples of linear functions:**

• 
$$f: \mathbb{R} \longrightarrow \mathbb{R}$$
 ,  $f(X) = X - 1$ 

• 
$$f: \mathbb{R} \longrightarrow \mathbb{R}$$
 ,  $f(X) = 2X + 1$ 

• 
$$f: \mathbb{R} \longrightarrow \mathbb{R}$$
 ,  $f(X) = 3X$ 

#### Notice that:

• In each of the shown functions, the index of X is 1, therefore each of them is a function of the first degree. 

#### The graphical representation of the linear function

**Example (1)** Graph each of the following linear functions:

1 
$$f: f(x) = 2x - 3$$

2 
$$r: r(X) = -\frac{1}{2}X$$

				2	024
	x				x
3	y = f(X)				y = r(X)
			GP) اعلی عر	S	علم التعلم ا
			ا عني عر	d.	العلم

Generally

The function  $f: \mathbb{R} \longrightarrow \mathbb{R}$  where  $f(X) = aX \cdot a \in \mathbb{R}^*$ 

is represented graphically by a straight line passing through the origin point (0,0)

Second The constant function

Definition

The function  $f: \mathbb{R} \longrightarrow \mathbb{R}$  where f(X) = b,  $b \in \mathbb{R}$  is called a constant function.

For example:

f: f(X) = 5 is a constant function where

f(1) = 5, f(0) = 5, f(-2) = 5, ... and so on.

Graphical representation of the constant function

The constant function f: f(x) = b (where  $b \in \mathbb{R}$ ) is represented by a straight line parallel to  $\chi$ -axis and passes through the point (0, b) this line is:

• above X-axis if b > 0

- below X-axis if b < 0
- coincident with X-axis if b = 0

The following examples illustrate that:

$$\left( f:f\left( X\right) =2\right)$$

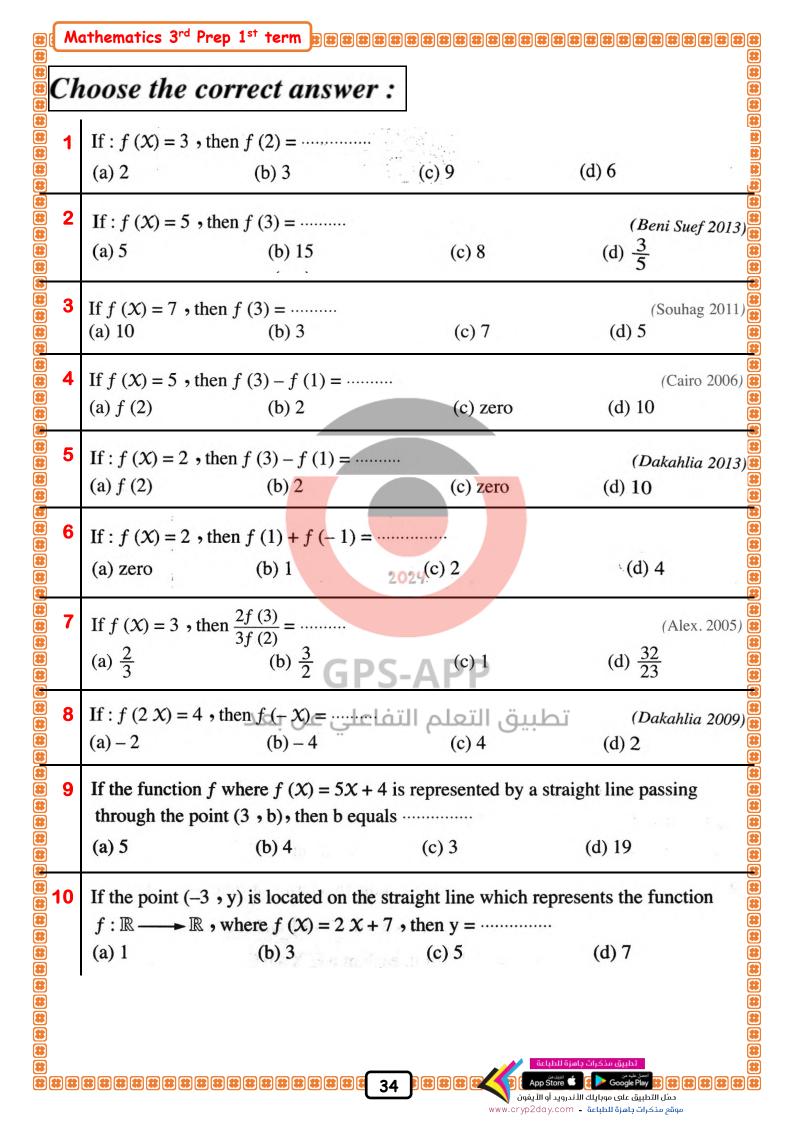
$$f:f(X)=-3$$

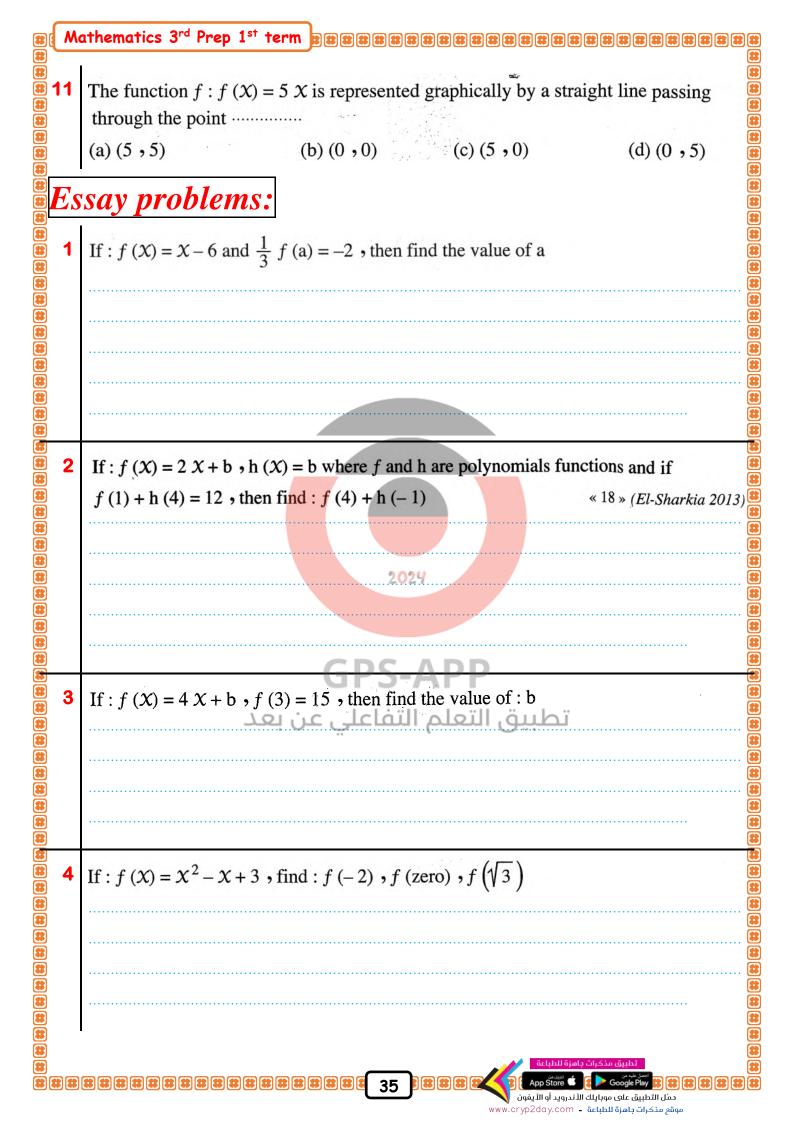
$$f:f(X)=0$$

The straight line is above  $\chi$ -axis and passes through the point (0, 2)

The straight line is below  $\chi$ -axis and passes through the point (0, -3)

The straight line is coincident with X-axis and passes through the point (0, 0)





B( W	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term
5	Represent graphically the function $f: \mathbb{R} \longrightarrow \mathbb{R}$ , where $f(X) = 2 - X$ and find the points of intersection of the straight line by the two coordinate axes.
Co	omplete each of the following:
1	If: $f(x) = 5$ , then $f(3) = \dots$ (a) 5 (b) 15 (c) 8 (d) $\frac{3}{5}$
2	If $f(x) = 5$ , then $f(3) - f(1) = \dots$ (Cairo 2006) (a) $f(2)$ (b) 2 (c) zero (d) 10
3	) If : $f(x) = 2$ , then $f(1) + f(-1) = \dots$ (a) zero (b) 1 (c) 2
4	If the point (-3, y) is located on the straight line which represents the function
	$f: \mathbb{R} \longrightarrow \mathbb{R}$ , where $f(x) = 2x + 7$ , then $y = \dots$ (a) 1 (b) 3 (c) 5 (d) 7
Es	تطبيق التعلم التفاعلي عن ب
1	If $f: \mathbb{R} \longrightarrow \mathbb{R}$ is represented by a straight line cuts y-axis at (b, 3) where $f(X) = 6X - a$ Find the value of: $2a + 7b$
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	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term
2	If the straight line which represents the function $f: \mathbb{R} \longrightarrow \mathbb{R}$ where $f(x) = 2x - a$ cuts y-axis at the point (b, 5) <b>Find the value of:</b> $3a + 2b$
3	Represent graphically the linear function $f(X) = 2 X + 1$ and find the points of
	intersection of the straight line representing it, with the two coordinate axes.
	2000
4	If the curve of the function: $f(x) = ax - 5$ passes through the point $(2,3)$ ,
4	then find the value of a and find the point of intersection of the straight line which
4	then find the value of a and find the point of intersection of the straight line which represents it with y-axis.
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# Sheet (5)

# Polynomial functions Part (3)

#### The quadratic function Third

#### Definition

The function  $f : \mathbb{R} \longrightarrow \mathbb{R}$  where  $f(X) = a X^2 + b X + c$ 

where a, b and c are real numbers,  $a \neq 0$ 

is called a quadratic function (it is a polynomial function of the second degree).

## **Example (2)** Graph each of the following quadratic functions:

 $f: f(X) = X^2 \text{ taking } X \in [-3, 3]$ 

 $f: f(X) = -X^2 \text{ taking } X \in [-3, 3]$ 

#### Solution

1 
$$f(X) = X^2$$

x	- 3	-2	- 1	0	1	2	3
f(X)	9	4	1	0	1	4	9

2 
$$f(X) = -X^2$$

x	-3	-2	- 1	0	1	2	3
f(x)	<b>-</b> 9	-4	-1	0	- 1	-4	-9

1 The point of the vertex of the curve.

The equation of the line of symmetry.

3 The maximum or minimum value of the function.

1 The point of the vertex of the curve.

2 The equation of the line of symmetry.

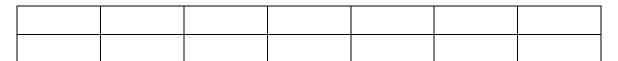
3 The maximum or minimum value of the function.



Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term

Example 4

- Graph the function  $f: f(X) = -X^2 + 3X + 2$  taking  $X \in [-1, 4]$  and from the graph, find:
- 1 The maximum value or minimum value of the function.
- 2 The equation of the line of symmetry.





Finding the point of the vertex of the curve:
At the point of the vertex of the curve of the quadratic function; it will be:

• The X-coordinate =  $\frac{-b}{2a}$ 

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• The y-coordinate =  $f\left(\frac{-b}{2a}\right)$ 

where b is the coefficient of X, a is the coefficient of  $X^2$ 

$$\therefore$$
 X at the vertex of the curve  $=\frac{-3}{2\times-1}=\frac{-3}{-2}=1\frac{1}{2}$ 

$$f(1\frac{1}{2}) = -\frac{9}{4} + \frac{9}{2} + 2 = 4\frac{1}{4}$$

## Choose the correct answer:

- If the curve of the function f where  $f(X) = X^2 a$  passes through the point (1, 0), then  $a = \cdots$  (Alex. 2011)
  - $(a) \pm 1$

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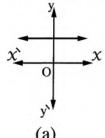
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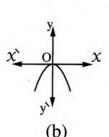
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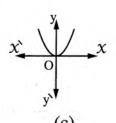
(b) - 1

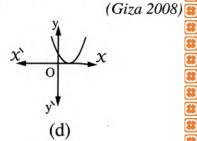
(c) 1

- (d) zero
- **2** The graph of the function  $f: f(x) = x^2 2x + 1$  is the graph number ........









# Essay problems:

Represent graphically the function f where  $f(x) = x^2$ ,  $x \in \mathbb{R}$  consider  $x \in [-3, 3]$  and from the drawing deduce the coordinate of the vertex of the curve, and the equation of the symmetry axis and the minimum or the maximum value of the function.

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- Draw the curve of the function f such that  $f(X) = X^2 3$  taking that  $X \in [-3, 3]$ , and from the graph deduce:
  - (1) The coordinates of the vertex of the curve.
  - (2) The maximum or minimum value of the curve.
  - (3) The equation of the symmetric axis.





Graph the function f where

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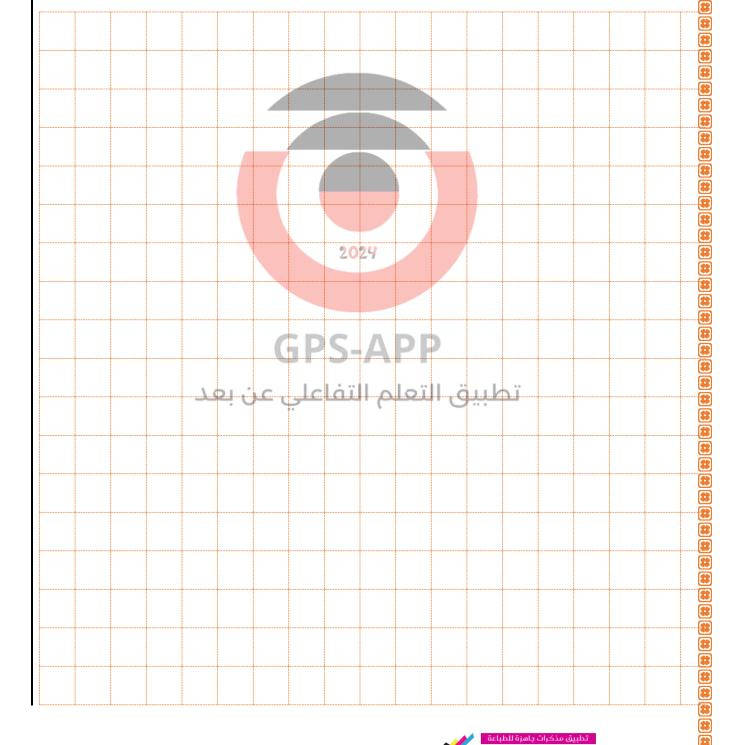
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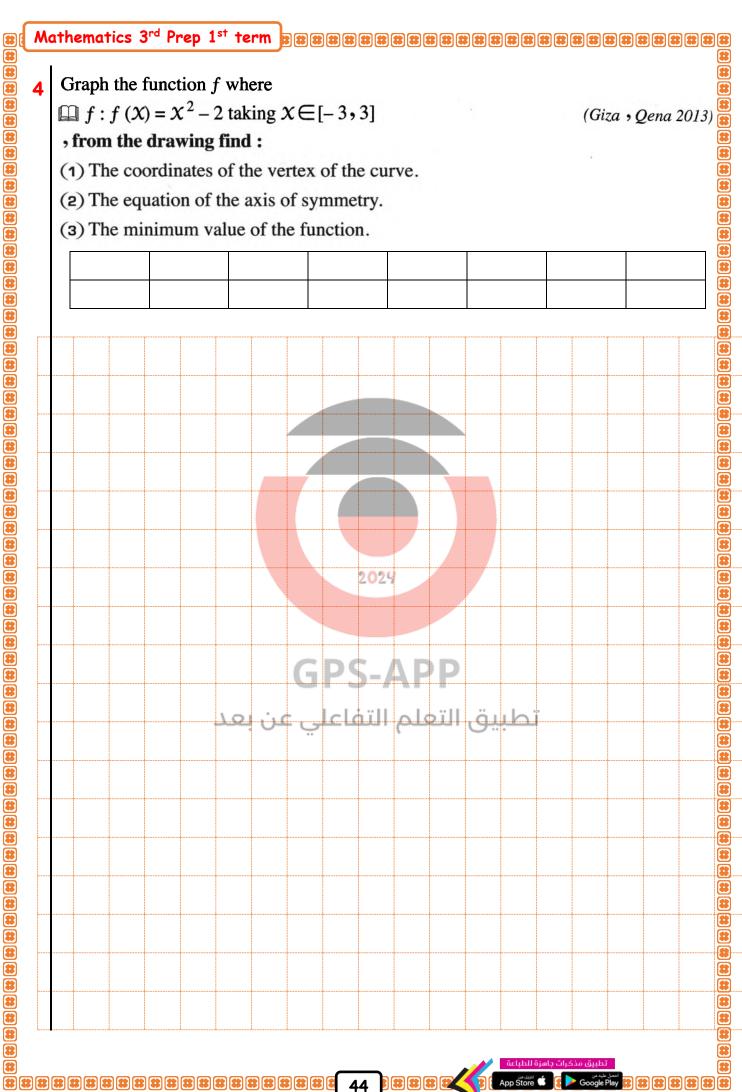
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(Giza , Qena 2013)

- , from the drawing find:
- (1) The coordinates of the vertex of the curve.
- (2) The equation of the axis of symmetry.
- (3) The minimum value of the function.







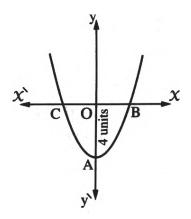
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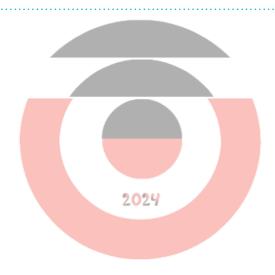
The opposite figure:

represents the curve of the function f, where:

$$f(X) = X^2 - m$$
 If  $OA = 4$  units, find:

- (1) The value of m
- (2) The area of the triangle with vertices A, B and C





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# Sheet (6)

## Ratio and Proportion

## First: The Ratio: -

#### Generally

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If a and b are two real numbers, then:

The ratio between a and b is written a: b or  $\frac{a}{b}$  and is read a to b where:

a is called the antecedent of the ratio, b is called the consequent of the ratio, a and b are called together the two terms of the ratio.

#### Properties of the ratio

The value of the ratio does not change if each of its terms is multiplied or divided by the same non-zero real number.

The value of the ratio  $(\neq 1)$  changes if we add or subtract (to or from) each of its two terms a non-zero real number.

## First: The Proportion: -

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#### Definition of proportion

It is the equality of two ratios or more.

If  $\frac{a}{b} = \frac{c}{d}$ , then the quantities a, b, c and d are proportional. i.e.

And vice versa: If a, b, c and d are proportional, then:  $\frac{a}{b} = \frac{c}{d}$ 

• a is called the first proportional.

• b is called the second proportional.

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• c is called the third proportional.

• d is called the fourth proportional.

a and d | are called extremes and | b and c | are called means.

#### For example:

The numbers 1, 4, 7 and 28 are proportional numbers, because  $\frac{1}{4} = \frac{7}{28}$ 

And: 1 is the first proportional, 4 is the second proportional, 7 is the third proportional,

28 is the fourth proportional, 1 and 28 | are the extremes of this proportion and 4 and 7 are the means.

Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term

#### **Properties of proportion**

Property (1)

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If  $\frac{a}{b} = \frac{c}{d}$ , then:  $a \times d = b \times c$  (The product of the extremes = the product of the means)

Property (2)

If 
$$a \times d = b \times c$$
, then  $\frac{a}{b} = \frac{c}{d}$ 

Also we can deduce that : .

• If 
$$\overrightarrow{a \times d} = \overrightarrow{b} \times \overrightarrow{c}$$
, then  $\frac{a}{c} = \frac{b}{d}$ 

• If 
$$a \times d = b \times c$$
, then  $\frac{b}{a} = \frac{d}{c}$ 

• If 
$$a \times d = b \times c$$
, then  $\frac{c}{a} = \frac{d}{b}$ 

## Property (3)

If 
$$\frac{a}{b} = \frac{c}{d}$$
, then  $\frac{a}{c} = \frac{b}{d}$ 

The antecedent of the first ratio

The antecedent of the second ratio

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The consequent of the first ratio The consequent of the second ratio

For example:

If 
$$\frac{a}{4} = \frac{b}{3}$$
, then  $\frac{a}{b} = \frac{4}{3}$  and  $\frac{b}{a} = \frac{3}{4}$  it is a likely like

Property (4)

If 
$$\frac{a}{b} = \frac{c}{d}$$
, then  $a = cm$  and  $b = dm$  (where m is a constant  $\neq 0$ )

For example:

If 
$$\frac{a}{b} = \frac{3}{4}$$
, then:  $a = 3$  m,  $b = 4$  m (where m is a constant  $\neq 0$ )

Important remark

If a, b, c and d are proportional quantities and we assume that:  $\frac{a}{b} = \frac{c}{d} = m$ , then

$$(a) = bm$$
,  $(c) = dm$ 

For example:

If 
$$\frac{a}{b} = \frac{c}{d} = \frac{3}{4}$$
, then  $a = \frac{3}{4}b$ ,  $c = \frac{3}{4}d$ 

Mathematics 3rd Prep 1st term

#### Generally

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8

If a, b, c, d, e, f, ... are proportional quantities and we assume that:

$$\frac{a}{b} = \frac{c}{d} = \frac{e}{f} = \dots = m$$
, then  $(a) = bm$ ,  $(c) = dm$ ,  $(e) = fm$ ,  $\dots$ 

#### Property (5)

If we consider the proportion :  $\frac{9}{15} = \frac{6}{10} = \frac{3}{5}$ 

- If we add the antecedents and consequents of the 1<sup>st</sup> and the 2<sup>nd</sup> ratios, we get the ratio  $\frac{9+6}{15+10} = \frac{15}{25} = \frac{3}{5}$  which is one of given ratios.
- Also if we add the antecedents and consequents of the 2<sup>nd</sup> and the 3<sup>rd</sup> ratios, we get the ratio  $\frac{6+3}{10+5} = \frac{9}{15} = \frac{3}{5}$  = one of the given ratios.
- If we add the antecedents and consequents of the three given ratios, we get the ratio  $\frac{9+6+3}{15+10+5} = \frac{18}{30} = \frac{3}{5} = \text{one of the given ratios.}$

If 
$$\frac{a}{b} = \frac{c}{d} = \frac{e}{f} = \cdots$$
 and  $m_1$ ,  $m_2$ ,  $m_3$ ,  $\cdots$  are non-zero real numbers

then  $\frac{m_1 a + m_2 c + m_3 e + \cdots}{m_1 b + m_2 d + m_3 f + \cdots} = \text{one of the given ratios}$ 

# Choose the correct answer: A D

- The fourth proportional for the 3, 6, 6 is.....
- A) -12 B) 6 C) 9 D) 12
- 4 If  $\frac{a}{b} = \frac{3}{2}$ , then  $\frac{a+b}{a-b} = \frac{1}{2}$ A)  $\frac{3}{2}$  B) 5 C)  $\frac{4}{5}$  D) 2

Mathematics 3rd Prep 1st term REPRESE 

5 If:  $\frac{a}{b} = \frac{3}{4}$ , then 4a - 3b + 5 = ...

- A) 0
- B) 1
- C) 3
- D) 5

6 If:  $\frac{a}{b} = \frac{5}{3}$ , then  $\frac{3a}{5b} = \frac{1}{3}$ 

- A) 1
- B)  $\frac{5}{3}$
- **C**) 3
- D) 5

7 If:  $\frac{a}{b} = \frac{c}{d} = \frac{3}{4}$ , then  $\frac{a+c}{b+d} = \dots$ 

- D)  $\frac{9}{16}$

8 If:  $\frac{a}{2} = \frac{b}{3}$ , then  $\frac{b-a}{b+a} = \dots$ 

- A)  $\frac{1}{5}$
- B)  $\frac{1}{3}$  C)  $\frac{2}{5}$
- D)  $\frac{3}{5}$

9 If:  $\frac{a}{12} = \frac{b}{5} = \frac{a-2b}{k}$ , then k

- A) 1

- D) 4

10 If:  $\frac{a}{5} = \frac{b}{4} = \frac{a+b}{k}$ , then  $k = \frac{a+b}{2024}$ 

A) 5

B) 4

C) 9

D) 1

11 If:  $\frac{X}{Y} = \frac{Z}{1}$  which of the following is right ....

- A)  $\frac{X}{1} = \frac{Y}{Z}$  B)  $\frac{X}{Z} = \frac{1}{Y}$  C)  $\frac{X}{Y} = \frac{1}{Z}$  D)  $\frac{X}{Z} = \frac{Y}{1}$

12 If:  $\frac{X}{2} = \frac{Y}{7} = \frac{X+Y}{K}$ , then K =.....

A) 4

- B) 10
- C) 9

D) 14

13 4 X = 25 Y, then  $\frac{X}{Y}$  = .....

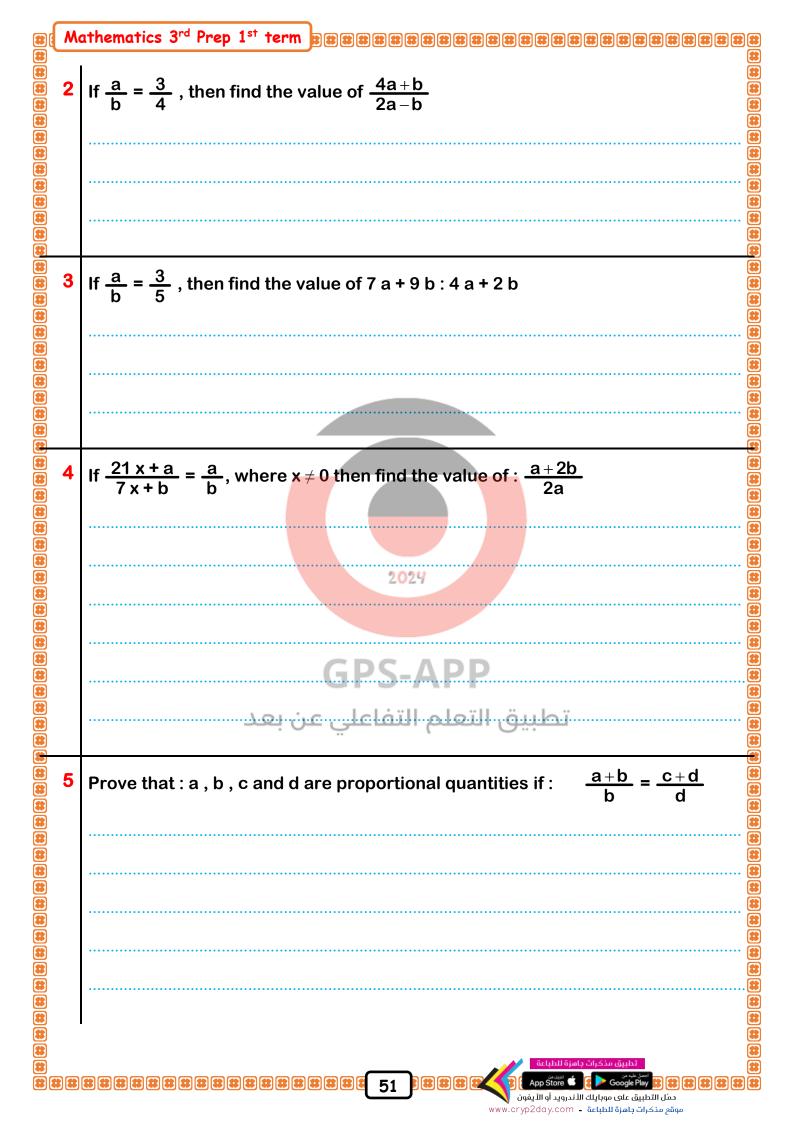
- A)  $\frac{4}{25}$
- B)  $\frac{2}{5}$
- C)  $\frac{5}{2}$
- D)  $\frac{25}{4}$

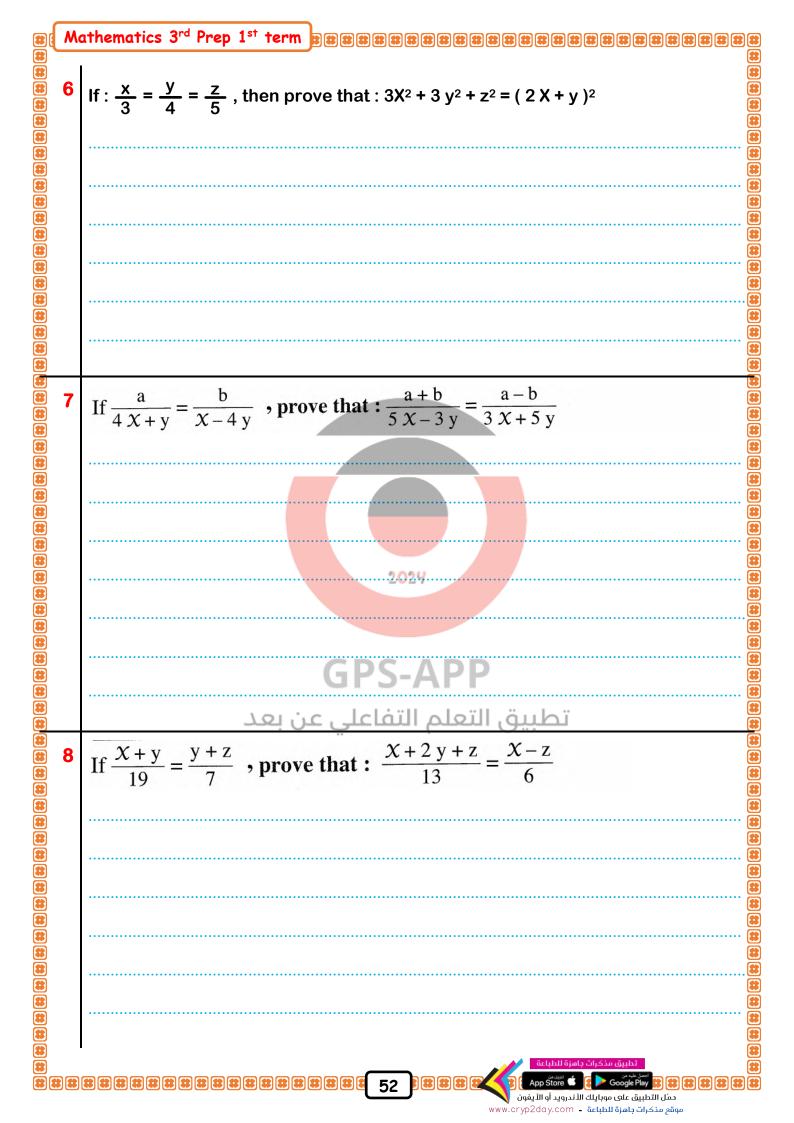
14 If: A, X, B and 2 X are proportional, then:  $\frac{A}{B}$  = .....

- A) 2:1
- B) 1:2
- C) 1:3
- D) 1:4



Mathematics 3rd Prep 1st term 15 If:  $\frac{3a}{5b} = \frac{1}{2}$ , then:  $\frac{a}{b} = \frac{1}{2}$ D)  $\frac{3}{2}$ 16 If:  $\frac{a+b}{5} = \frac{a-b}{3}$ , then:  $\frac{a}{b} = \dots$ 17 If: 2 a = 3 b, then  $\frac{5 \text{ b}}{a}$  = ..... A)  $\frac{5}{3}$ B)  $\frac{5}{2}$ 18 If 3 x = 5 y, then  $\frac{5 y}{3 x}$  = ..... D)  $\frac{5}{3}$ A) 1 B) 2 19 If: 4 x = 5 y, then:  $\frac{5 y}{4 x}$ A) 1 C) 3 D) 4 20 If  $\frac{x}{2} = \frac{y}{7} = \frac{2x + y}{a}$ , then  $a = \dots$ (Kafr El-Sheikh 2011) (d) 5(a) 9(c) 1621 If  $\frac{a}{b} = \frac{c}{d} = \frac{e}{f}$ , then  $\frac{a+2c+3e}{b+2d+3f} = \frac{\dots}{5f}$  (c) 5 e رُّهُ) وَ الْمُواعِلِي عِنْ بِعِدِ طبيق التعلم التفاعلي عِنْ بِعِدِ طبيق التعلم التفاعلي عِنْ بِعِدِ التعلم التفاعلي عِنْ بِعِدِ التعلم التفاعلي عِنْ بِعِدِ (d) 5 a + 5 c + 5 e1 If  $\frac{x-2y}{x+3y} = \frac{1}{3}$ , find:  $\frac{y}{x}$ 





Mo	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term ************************************
9	If $\frac{x}{a-b+c} = \frac{y}{b-c+a} = \frac{z}{c-a+b}$ , prove that : $\frac{x+y}{a} = \frac{y+z}{b}$
10	Find the number which if it is added to the two terms of the ratio 7:11, it will be 2:3
	2024
11	The ratio between two integers is $\frac{3}{4}$ , if we add 4 to the small number and
	subtract 3 from the great number, the ratio will become 8:9 Find the two numbers.
	قطبيق مذكرات باهزة للطباعة
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Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term Two integers, the ratio between them is 2:3, if you add to the first 7 and subtract from the second 12, the ratio between them becomes 5:3 Find the two numbers. Choose the correct answer: The first proportional of the numbers: 21, 15 and 35 is ..... D)  $\frac{7}{3}$ B) 3 A) 9 The fourth proportional for the 8, 6 and 4 is..... 8 A) 2 B) 3 C) 4 D) 7 The fourth proportional for the 9, 12, 3 is ..... A) 6 D) 1 If  $\frac{a}{b} = \frac{3}{2}$ , then  $\frac{a+b}{a-b}$ A)  $\frac{3}{2}$ B) 5 D) 2 If:  $\frac{a}{b} = \frac{3}{7}$ , then  $\frac{a}{b-a} =$ D) Otherwise 6 If:  $\frac{a}{b} = \frac{5}{4}$ , then  $\frac{a+b}{a-b} =$ C)  $\frac{4}{5}$ B) 9 D) 2 حمَل التطبيق على موبايلك الأندرويد أو الأيفون

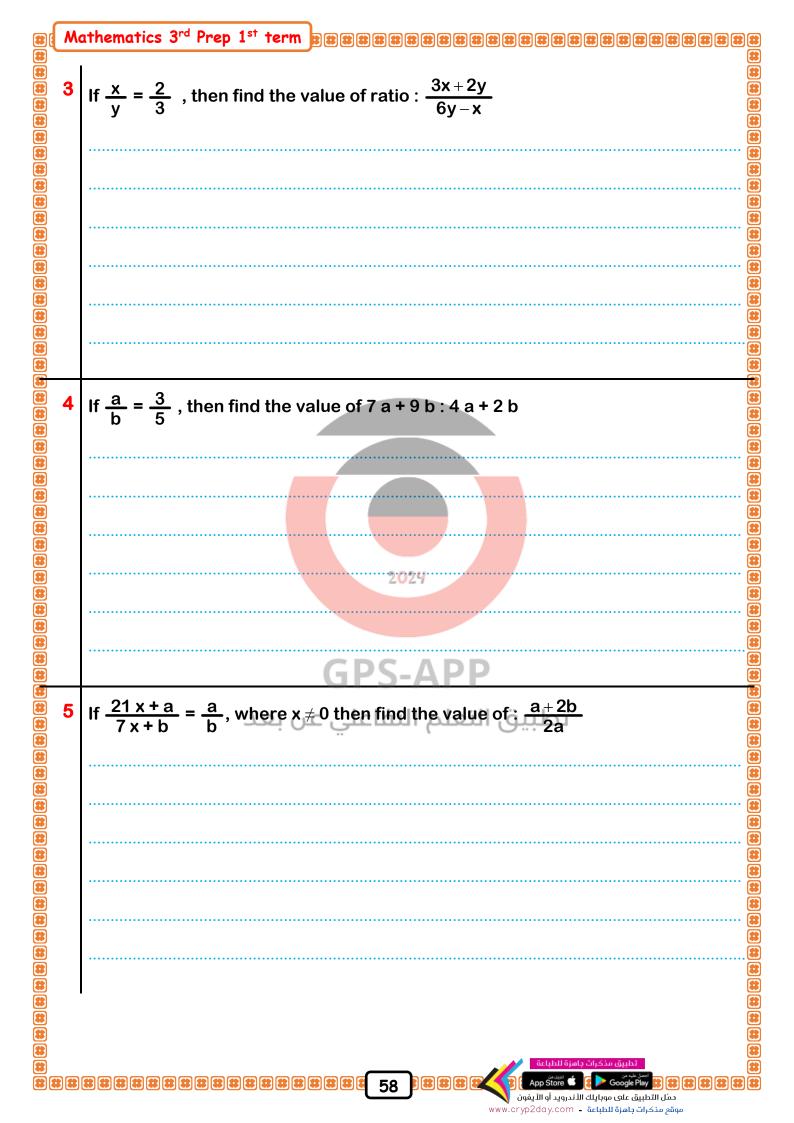
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Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term 7 If:  $\frac{a}{5} = \frac{b}{7}$ , then 7 a – 5 b + 3 = ..... A) 3 C) 5 B) 7 D) 2 8 If:  $\frac{a}{5} = \frac{b}{2} = \frac{a-2b}{k}$ , then k = ....D) 1 If:  $\frac{a}{2} = \frac{b}{3} = \frac{4a-2b}{c}$ , then c = ...C)  $-\frac{1}{2}$ A) -2B) 2 B) 5 A) 6 D) 2 D) 5 If:  $\frac{X}{5} = \frac{Y}{3} = \frac{X - Y}{\Delta}$ , then A = A) -2If: X, Y, 2 and 3 are proportional, then : X = ..... A)  $\frac{3}{2}$ **C**) 3 D) 2 If: 5 a, 2, 3 b, 7 are four proportional quantities, then:  $\frac{a}{b}$  = ..... B)  $\frac{6}{35}$ C)  $\frac{3}{5}$ D)  $\frac{3}{2}$ 15 If:  $\frac{a+2b}{a-b} = \frac{2}{3}$ , then:  $\frac{b}{a} = \dots$ C)  $-\frac{1}{8}$ D) - 8

Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term If:  $4 X^2 + 9 Y^2 = 12 XY$ , then:  $\frac{X}{Y} = \dots$ A)  $\frac{3}{2}$ B)  $\frac{2}{3}$  C)  $-\frac{2}{3}$ D)  $-\frac{3}{2}$ If: 2 x = 7 y, then  $(\frac{x}{v})^{-1} = \dots$ C)  $\frac{49}{4}$ B)  $\frac{7}{2}$ A)  $\frac{2}{7}$ D)  $\frac{4}{49}$ If 3 a = 8 b, then:  $\frac{2a}{b}$  = ...... C)  $\frac{16}{3}$ D)  $\frac{3}{8}$ B) 16 A) 24 The ratio between the area of a square shaped region of side length L to the area of another square shaped region of side length 2 L is..... C) 1:4 A) 1:2 B) L:4 D) 4:1 If: 24, X, 6 and 3 are proportional quantities, then X = ..... A) 9 D) 48 22 If  $\frac{a}{b} = \frac{3}{2}$ , then  $\frac{a+b}{a-b} = \frac{3}{2024}$ A)  $\frac{3}{2}$ B) 5 D) 2 23 If:  $\frac{a}{b} = \frac{3}{4}$ , then  $4a - 3b + 5 = \dots$ تطبيق التعلم التفاعلي عن بعد D) 5  $\frac{24}{1}$  If:  $\frac{a}{b} = \frac{5}{3}$ , then  $\frac{3a}{5b} = \frac{1}{3}$ B)  $\frac{5}{3}$ A) 1 **C**) 3 D) 5 25 If:  $\frac{a}{b} = \frac{c}{d} = \frac{3}{4}$ , then  $\frac{a+c}{b+d} = \dots$ B)  $\frac{7}{4}$ C)  $\frac{3}{7}$ D)  $\frac{9}{16}$  $\frac{a}{a} = \frac{a}{2} = \frac{b}{3}$ , then  $\frac{b-a}{b+a} = \frac{a}{2} = \frac{b}{3}$ A)  $\frac{1}{5}$ B)  $\frac{1}{3}$ C)  $\frac{2}{5}$ D)  $\frac{3}{5}$ 56 حمَل التطبيق على موبايلك الأندرويد أو الأيفون

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Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term | R If:  $\frac{a}{12} = \frac{b}{5} = \frac{a-2b}{k}$ , then k = ...B) 2 **C**) 3 D) 4 If:  $\frac{a}{5} = \frac{b}{4} = \frac{a+b}{k}$ , then k = ...B) 4 C) 9 D) 1 If:  $\frac{X}{Y} = \frac{Z}{1}$  which of the following is right ........... A)  $\frac{X}{1} = \frac{Y}{7}$ B)  $\frac{X}{7} = \frac{1}{Y}$ C)  $\frac{X}{Y} = \frac{1}{7}$  D)  $\frac{X}{7} = \frac{Y}{1}$ Essay problems: 1 If  $\frac{x-2y}{x+3y} = \frac{1}{3}$ , find:  $\frac{y}{x}$ تطبيق التعلم التفاعلي عن بعد 2 If  $\frac{a}{b} = \frac{3}{4}$ , then find the value of  $\frac{4a+b}{2a-b}$ 

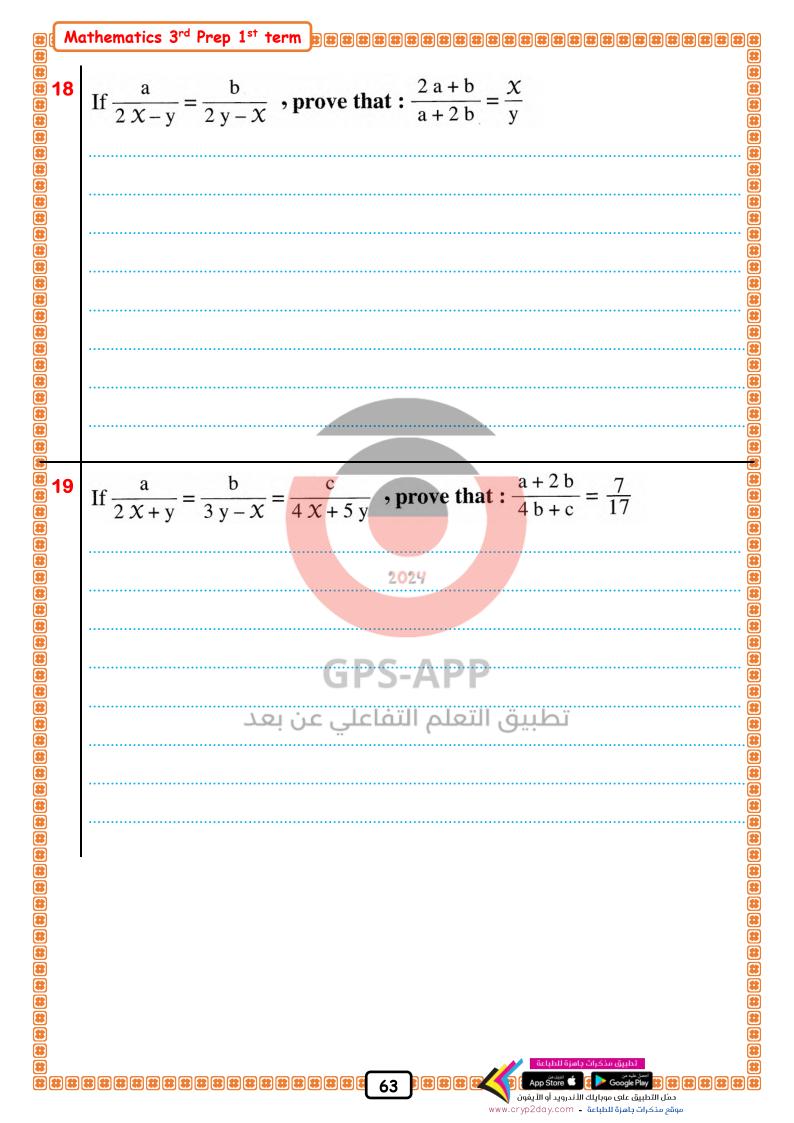


<b>33</b> [	M	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>BBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBB</b>
<b>33</b>	6	Prove that : a , b , c and d are proportional quantities if : $\frac{a+b}{b} = \frac{c+d}{d}$
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#	7	Prove that : a b c and d are proportional quantities if : A = C
**	•	Prove that : a , b , c and d are proportional quantities if : $\frac{a}{b-a} = \frac{c}{d-c}$
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***		CDC ADD
# <u></u>		GP3-APP
***	8	If: $\frac{x}{3} = \frac{y}{4} = \frac{z}{5}$ , then prove that: $\frac{2y-z}{3x-2y+z} = \frac{1}{2}$
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	Mo	thematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>BSSSSSSSSSSSSSSSSSSSSSS</b>	<b>88</b>
			33 33 33
	9	If: $\frac{x}{3} = \frac{y}{4} = \frac{z}{5}$ , then prove that: $3X^2 + 3y^2 + z^2 = (2X + y)^2$	88
<b>33</b>		3 4 5 , then prove that: 6x + 6y + 2 (2x + y)	33 33
			<b>3</b>
			#  ##
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## ##			# #
<b>33</b> <b>22</b>			33 93
			<b>3</b>
<b>33</b> <b>33</b>			33 [88
			<b>33</b>
# #			#    }
<b>88</b>			88
**************************************	10	Find the number which if it is added to the two terms of the ratio 7:11, it will be	** **
		2:3	83 FE
			<b>3</b>
<b>33</b> <b>33</b>			<u>#</u>
			<b>88</b>
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** **		2024	# #
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		GPS-APP	88
## ## ##	4.4	Find the number that if we subtract thrice of it from each of the two terms of	# <u>#</u>
		المستبيل المستمين عن بعد	(# (#
		the Ratio $\frac{49}{69}$ , the ratio becomes $\frac{2}{3}$	<b>**</b>
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<b>33</b>			## ## ## ## ## ## ## ## ## ## ## ## ##
** **			<b>88</b> <b>88</b>
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<b>3</b>	Mo	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>BSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSS</b>
88) 1	12	Find the number which if its square is added to each of the two terms of ratio
		7:11 it becomes 4:5
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#5 #3		
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<del>22</del>	-	
***	13	Two integers, the ratio between them is 3:7 and if we subtracted 5 from each
<b>33</b>		term, the ratio between each of them becomes 1:3, find the two numbers.
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# # #		GPS-APP
		GF3-AFF
<b>88</b>	14	
# 1 #	14	The ratio between two integers is $\frac{3}{4}$ , if we add 4 to the small number and
**		subtract 3 from the great number , the ratio will become 8 : 9 Find the two
## ##		-
<b>33</b>		numbers.
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		دمن الطبيق على موبايلت الدندرويد او الديمون موقع مذكرات جاهزة للطباعة      www.cryp2day.com

<b>.</b>	Ma	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>Bassassassassassassassassas</b>
***	٠	
33 ·	15	Two integers, the ratio between them is 2 : 3 , if you add to the first 7 and
# #		subtract from the second 12 , the ratio between them becomes 5 : 3 Find the
		two numbers.
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# #		
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		<u> </u>
33 33 4	16	In the opposite figure: Alaa shaded $\frac{5}{6}$ the area of the circle,
**		
**		$\frac{2}{3}$ the area of the triangle, find the ratio between the area of
#		the circle and the area of the triangle.
**		and on one and and an out of the
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<del>18</del>	4 -	عن بعد عصبيق النعام النفاعلي عن بعد عصب عدد عدد عدد عدد عدد عدد النفاع ا
## (## )	17	If $\frac{x}{2a+b} = \frac{y}{2b-c} = \frac{z}{2c-a}$ , then prove that : $\frac{2x+y}{4a+4b-c} = \frac{2x+2y+z}{3a+6b}$
**		2a+0 2b-c 2c-a 4a+4b-c 3a+6b
# #		
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		حمَّل التطبيق على موبايلك الأندرويد أو الأيفون موقع مذكرات باهزة للطباعة  - www.cryp2day.com



# Sheet (7)

# Continued Proportion

## **Definition:**

The quantities a, b and c are said to be in continued proportion if  $\frac{a}{b} = \frac{b}{c}$ 

In this proportion, a is called the first proportion, c is called the third proportion and b is called the middle proportion (proportional mean).

## For Example : -

The numbers 4, 6 and 9 form a continued proportion because:  $\frac{4}{6} = \frac{6}{9}$  or because:  $(6)^2 = 4 \times 9$  where 6 is the middle proportion, 4 is the first proportion and 9 is the third proportion.

#### Notice That:-

- If a, b and c are in continued proportion, then:  $b^2 = a c$  i.e.  $b = \pm \sqrt{ac}$  and the two quantities a and c should be either both positive or both negative.
- 2 For any two positive numbers or any two negative numbers x and y, there are two middle proportions  $(\sqrt{x} y)$  and  $-\sqrt{x} y$

#### Remark: -

# **GPS-APP**

If a, b and c are in continued proportion and we assume that:  $\frac{a}{b} = \frac{b}{c} = m$ 

, then 
$$\frac{b}{c} = m$$

$$\therefore$$
 b = cm

$$\cdot \cdot \cdot \frac{a}{b} = m$$

8

8

$$\therefore$$
 a = bm

Substituting for b from (1):  $\therefore$  a = (cm) m

$$\therefore$$
 (a) = cm<sup>2</sup>

i.e. If 
$$\frac{a}{b} = \frac{b}{c} = m$$
, then  $\begin{cases} b = cm \\ a = cm^2 \end{cases}$ 

#### General Definition: -

The quantities a, b, c, d, ... are in continued proportion if:  $\frac{a}{b} = \frac{b}{c} = \frac{c}{d} = ...$ 

The numbers 16, 24, 36 and 54 are in continued proportion

because :  $\frac{16}{24} = \frac{24}{36} = \frac{36}{54}$ , each ratio =  $\frac{2}{3}$ 

## Remark:-

If a, b, c and d are in continued proportion and we assume that:  $\frac{a}{b} = \frac{b}{c} = \frac{c}{d} = m$ , then:

$$\frac{c}{d} = m$$

$$\therefore$$
 (c) = dm

$$\frac{b}{c} = m$$

$$\therefore$$
 b = cm

Substituting for c from (1):  $\therefore$  b = (dm) m

$$\therefore$$
 (b) = dm<sup>2</sup>

$$\frac{a}{b} = m$$

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$$\therefore$$
 a = bm

Substituting for b from (2):  $\therefore$  a = (dm<sup>2</sup>) m

$$\therefore$$
 (a) = dm<sup>3</sup>

If  $\frac{a}{b} = \frac{b}{c} = \frac{c}{d} = m$ , then c = dm,  $b = dm^2$  and  $a = dm^3$ 

## Choose the correct answer:

The third proportion of the two numbers 9 and - 12 is .....

- A) 16
- B) 8
- C) 16
- D) 108

The middle proportion of the two numbers 3 and 27 is .....

- A) -9
- B) 9 C) ±9
- D) 21

The middle proportion of the two numbers 4 and 36 is ......

- A) 32
- B) 40
- C) 12
- D) ± 12

The middle proportion of the two numbers 4 and 25 equals .....

- A) 10
- B) 29
- C) 100
- D) ± 10

The proportional mean between a and b is .....

- A) ab
- B) √ab
- C)  $-\sqrt{ab}$
- D)  $\pm \sqrt{ab}$

The proportional mean between (X-2) and (X+2) is .....

- A)  $\sqrt{X+2}$
- B)  $X^2 4$  C)  $\pm \sqrt{X^2 4}$  D)  $\sqrt{X^2 4}$

65

<b>33</b> ( Mc	athematics 3 <sup>rd</sup> Pr	rep 1 <sup>st</sup> term			
** 7	If the numbe		tional mean of the	two numbers 3 and	k ,
**		B) 81	C) 27	D) 9	
** 8 **	If the number , then m =	-	proportional mean	of two numbers 2 and	m
# # #	A) 8	B) 12	C) 18	D) 36	
# 9 # # # # # # # # # # # # # # # # # #	If he middle p A) 6	roportion betwee B) 4	n 9 , k is 6 , then k C) 9	= D) 15	
# 10 # 10		which is added to ontinued proporti		oers 1 , 3 , and 6 to	
# # **	A) 1	B) 2	C) 3	D) 6	
3 11 3 11	continued pro	oportion is		ers 1, 3, 7, 15 to be	in
# #	A) 1	B) 2	C) 3	D) 4	
# 12 # # #	If a, 2, 4, b A) 8	are in co <mark>ntinu</mark> ed <sub> </sub> B) 1	proportion , then C) 9	a + b = D) 7	
# 13 # 13	If: $\frac{a}{b} = \frac{b}{c} =$	$\frac{c}{5} = 2$ , then $a = 1$	2024		
# # #	A) 5 X 2 <sup>2</sup>	B) 40	C) 10	D) 2 X 5 <sup>3</sup>	
14	The positive	middle proporti	on between 3 an	d 27 is	
# #	A) 3	B) 4	C) 8 قرالتعلم التفاء	D) 9	
# 15 # # # # # # # # # # # # # # # # # # #	If 2, 6, X + 1 A) 1	5 are proportion B) 2	nal , then X = C) 3	D) 4	
# 16	If: 24, X, 6 A) 9	and 3 are propor B) 12	tional quantities C) 18	, then X = D) 48	
# 17 # 17	If $\frac{a}{b} = \frac{3}{2}$ , t	hen <u>a+b</u> =			
## ## ##	A) $\frac{3}{2}$	B) 5	C) $\frac{4}{5}$	D) 2	
18	If: $\frac{a}{b} = \frac{3}{4}$ ,	then 4 a – 3 b + 5	=		
** ** **	A) 0	B) 1	<b>C</b> ) 3	D) 5	
######################################	*****	***	66	تطبيق مذكرات جاهزة للطباعة  *** ( الطباعة	
			•	حمل التطبيق على موبايلك الاندرويد أو الايمور موقع مذكرات جاهزة للطباعة  -  yp2day.com	

Mo	athematics 3 <sup>rd</sup> Pre	p 1 <sup>st</sup> term			
19	If 3 a = 8 b , th	2a _			
	11 3 a = 6 b , ti	b		,	
	A) 24	B) 16	C) $\frac{16}{3}$	D) {	3
20		en the area of a squ ther square shaped B) L:4			
Ess	say problems	•			
1	Find the middle	proportion between	3 and 27		
				•••••	••••••
2	Find the third pr	oportion for 6 and	12		
				•••••	
3				$a^2 + h^2$	а
	If b is the middle	e propor <mark>tion betwee</mark>	n a and c , prove	that: $\frac{a+b}{b^2+c^2}$	= <del>a</del> C
			2024		
		C D	* A B B		
		GP:	S-APP		•••••
4	If b is middle pro	pportion between a	and c , prove tha	$t: \frac{2\ddot{c}^2 - 3b^2}{3} =$	$\frac{2 b^2 - 3 a^2}{1 + 3 a^2}$
	•	•	• •	c² =	b²
					_
5	If a , b , c and d	are in continued pro	portion prove th	aı. —— = -	<u>od</u> a
<u> </u>				تطبيق مذكرات باهزة للطباعة	ı
	***		7 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	مل عليه من Google Pla	

Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term Republic If a, b, c and d are in continued proportion prove that:  $\frac{a^2-3c^2}{b^2-3d^2} = \frac{b}{d}$ 7 If a, b, c and d are in continued proportion prove that:  $\frac{ab-cd}{b^2-c^2} = \frac{a+c}{b}$ Choose the correct answer: The third proportion of the two numbers 3 and 6 is ..... A)  $\frac{1}{2}$ C) 9 B) 2 D) 12 The proportional mean between a and b is ..... C)  $-\sqrt{ab}$ A) ab B) √ab D) ± √ab If he middle proportion between 9, k is 6, then k = ..... A) 6 B) 4 D) 15 The number which is added to each of the numbers 1, 3, and 6 to become in continued proportion is ..... A) 1 B) 2 **C**) 3 D) 6 If  $\frac{a}{h} = \frac{3}{2}$ , then  $\frac{a+b}{a-b} =$ A)  $\frac{3}{2}$ B) 5 D) 2 If:  $\frac{a}{12} = \frac{b}{5} = \frac{a-2b}{k}$ , then k = ...A) 1 **C**) 3 D) 4 If:  $\frac{a}{5} = \frac{b}{4} = \frac{a+b}{k}$ , then k = ...C) 9 حمّل التطبيق على موبايلك الأندرويد أو الأيفون

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B (Ma	thematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term
8	The middle proportion of the two numbers 3 and 27 is
	The proportional mean between $(X-2)$ and $(X+2)$ is
10	The number which is added to each of the numbers 1, 3, 7, 15 to be in continued proportion is
11 88 88 88	The positive middle proportion between 3 and 27 is
# 12 <b># 12</b>	If: $\frac{a}{b} = \frac{3}{4}$ , then $4a - 3b + 5 =$ A) 0 B) 1 C) 3 D) 5
13	If: $\frac{X}{Y} = \frac{Z}{1}$ which of the following is right  A) $\frac{X}{1} = \frac{Y}{Z}$ B) $\frac{X}{Z} = \frac{1}{Y}$ C) $\frac{X}{Y} = \frac{1}{Z}$ D) $\frac{X}{Z} = \frac{Y}{1}$
B 14	The middle proportion of the two numbers 4 and 36 is  A) 32  B) 40  C) 12  D) ± 12
15 15	If the number 9 is the proportional mean of the two numbers 3 and k, then k =
######################################	If a, 2, 4, b are in continued proportion, then: a + b =
17 18 18	If 2, 6, X + 15 are proportional, then X =
18	If: $\frac{a}{b} = \frac{c}{d} = \frac{3}{4}$ , then $\frac{a+c}{b+d} =$ A) $\frac{3}{4}$ B) $\frac{7}{4}$ C) $\frac{3}{7}$ D) $\frac{9}{16}$
	The third proportion of the two numbers 9 and -12 is
	الطبيق مذكرات جاهزة للطباعة [49] [49] [49] [49] [49] [49] [49] [49]

		m			ı
o numbers 2 and m 0) 36	onal mean of the		ber 6 is the  B)	hen m =	, tł
		hen a =	•	· .	
D) 2 X 5 <sup>3</sup>	c) 10		5 <sup>2</sup> B		
n X = D) 48	լuantities , th C) 18	e proportio ) 12		:24,X,6 A)9	
		- =	, then $\frac{b-}{b+}$	$: \frac{a}{2} = \frac{b}{3},$	<b>3</b> If :
D) $\frac{3}{5}$	3) <del>2</del> 5		В	$\frac{1}{5}$	4
			blems:	y <i>prob</i>	Ssa
	and – 8	ion between	ioqorq elbk	d the midd	1 Find
		n for 3 and 6		d the third	2 Fine
		n for 3 and (		a the tima	
	طبيق التعلم	ناعلي عن	78		•
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$: \frac{a}{c} = \frac{b^2}{c^2}$	nd c , prove tha	tion betwee	iddle propo	is the mid	If b
					••••
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9	ياعة App S أو الليفون www.cryp2day	)#### <b>#</b> 7	****	***	 

<b>3</b>	Mo	thematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term ************************************
# 1	_	
# #	4	If b is the middle proportion between a and c, prove that : $\frac{a+b}{b+c} = \frac{a}{b}$
<b>33</b>		
# #		
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**************************************		
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<b>33</b>		
# #		
	_	
<b>33</b>	5	If b is the middle proportion between a and c, prove that: $\frac{a^3 + b^3}{b^3 + c^3} = \frac{a^2}{cb}$
<b>33</b>		
<b>33</b>		
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<b>3</b>		
## ##		
<b>33</b>		
<b>33</b> <b>33</b>	6	If b is the middle proportion between a and c, prove that : $\frac{a^2}{b^2} + \frac{b^2}{c^2} = \frac{2a}{c}$
		b <sup>2</sup> c <sup>2</sup> c
** **		
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** **		
<b>33</b>		تطبيق التعلم التفاعلي عن بعد
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# #		
<b>33</b>	7	If a, b, c and d are in continued proportion prove that: $\frac{ab-cd}{b^2-c^2} = \frac{a+c}{b}$
<b>3</b>		If a , b , c and d are in continued proportion prove that : $\frac{ab-cd}{b^2-c^2} = \frac{a+c}{b}$
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<b>33</b>		<u>8</u>
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		قطبيق مذكرات باهزة للطباعة الطباعة الطباعة عند الطباعة الطباع
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Mathematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term Bushushushushushushushushushushushushushu		
8	If a , b , c and d are in continued proportion prove that : $\frac{a^2 + b^2 + c^2}{b^2 + c^2 + d^2} = \frac{ac}{bd}$	
9	[-3 0.3]	
	If a, b, c and d are in continued proportion prove that : $\sqrt[3]{\frac{5a^3 - 3c^3}{5b^3 - 3d^3}} = \frac{a + c}{b + d}$	
	2024	
	GPS-APP	
	تطبيق التعلم التفاعلي عن بعد	
     <b>##</b>	تطبیق مذکرات جاهزة للطباعة     App Store	

# Direct Variation & Inverse Variation

#### **First** The direct variation

#### **Definition**

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**33** 

8

It is said that y varies directly as X and it is written  $y \propto X$  if | y = m X

*i.e.*  $\frac{y}{x} = m$  (where m is a constant  $\neq 0$ )

If the variable X took the two values  $X_1$  and  $X_2$  and  $Y_2$  and  $Y_3$  and  $Y_4$  and  $Y_2$ 

respectively, then:  $\left| \frac{y_1}{y_2} \right| = \frac{x_1}{x_2}$ 

#### Second The inverse variation

#### Definition

It is said that y varies inversely as X and it is written  $y \propto \frac{1}{x}$  if  $y = \frac{m}{x}$ 

*i.e.* x y = m, where (m is a constant  $\neq 0$ )

If the variable X took the two values  $X_1$ ,  $X_2$  and as a result for that y took the two values

 $y_1$  and  $y_2$  respectively, then:  $\frac{y_1}{y_2} = \frac{x_2}{x_1}$ 

## Choose the correct answer:

The relation which represents the direct variation between X and y is .........

A) 
$$\frac{X}{2} = \frac{y}{3}$$

B) 
$$Y = X + 3$$

C) 
$$Xy = 3$$

D) 
$$\frac{X}{2} = \frac{3}{y}$$

The relation which represents the direct variation between X and y is ......

A) 
$$Xy = 4$$

B) 
$$Y = X + 7$$

C) 
$$\frac{X}{2} = \frac{5}{v}$$

B) 
$$Y = X + 7$$
 C)  $\frac{X}{2} = \frac{5}{y}$  D)  $\frac{X}{3} = \frac{y}{8}$ 

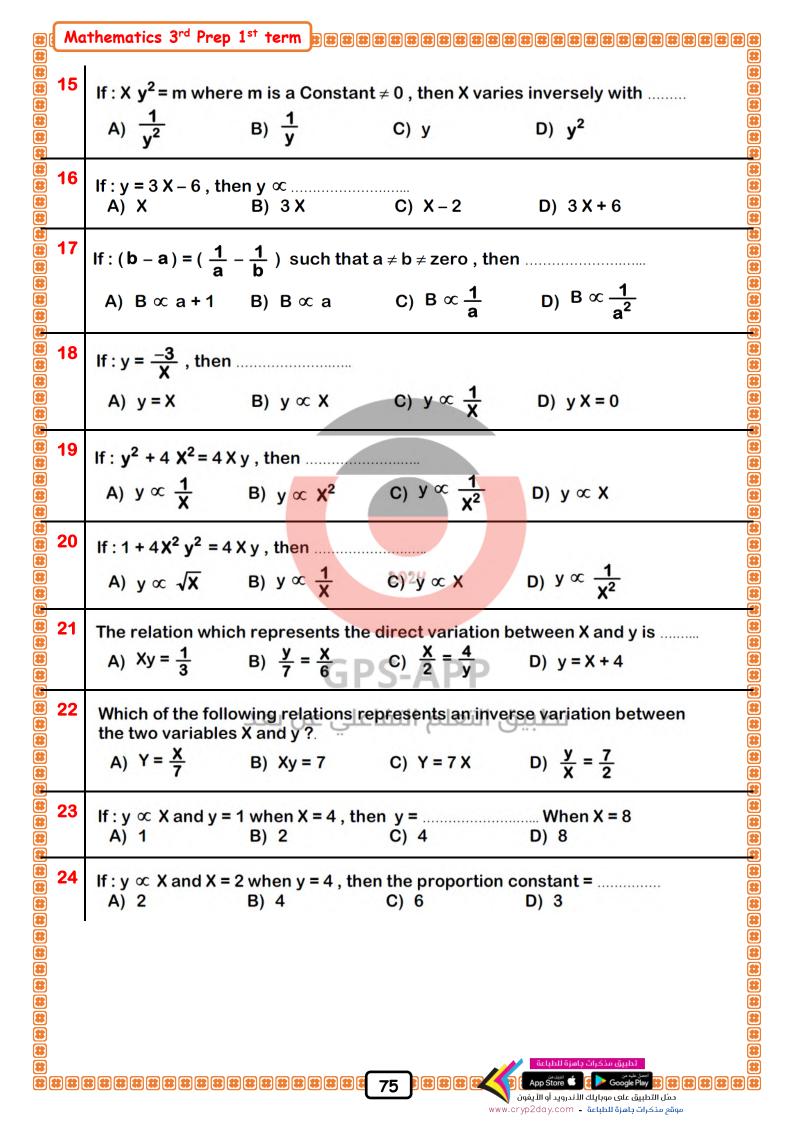
The relation which represents the direct variation between X and y is .........

A) 
$$Xy = 7$$

B) 
$$y = X + 2$$

C) 
$$\frac{X}{3} = \frac{4}{y}$$

Ma Ma	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>B####################################</b>
4	The relation which represents the direct variation between X and y is
**	A) $y^2 = 2X$ B) $\frac{X}{y} - X = 2$ C) $Xy = 3$ D) $\frac{Y}{X} - 9 = 5$
5	Which of the following relations represents an inverse variation between the two variables X and y?
	A) $y = X + 2$ B) $Y = 4X$ C) $\frac{X}{y} = \frac{5}{7}$ D) $Xy = 11$
6	If: $y \propto X$ and $y = 1$ when $X = 3$ , then $y = \dots$ When $X = 6$ A) 18 B) 6 C) 2 D) 1
7	If: $y \propto X$ and $y = 5$ when $X = 3$ , then: the constant proportional =
	A) 15 B) 5 C) 3 D) $\frac{5}{3}$
8	If : $y \propto X^2$ and $X = 1$ as $y = 2$ , then the constant variation is
	A) $\frac{1}{2}$ B) 1 C) 2 D) 32
9	If y varies inversely with X, and X = $\sqrt{3}$ when y = $\frac{2}{\sqrt{3}}$ , then: the
	constant proportion =
	A) $\frac{1}{2}$ B) $\frac{2}{3}$ C) 2 D) 6
10	If y varies inversely as X <sup>2</sup> , k is a constant, then:
	A) $y = k X^2$ B) $Y = k - X^2$ C) $y = \frac{kX}{X^2}$ D) $y = \frac{k}{X^2}$
1 1	If: $\frac{y}{x} = 5$ , then $y \propto$
	If: $\frac{y}{x} = 5$ , then $y \propto \frac{CPS-APP}{B}$ A) $X = \frac{1}{x} = \frac{1}{x}$ B) $\frac{1}{x} = \frac{1}{x}$ B) $\frac{1}{x} = \frac{1}{x}$ C) $\frac{1}{x^5}$
12	If: X y = 5, then: y ∞
	A) $\frac{1}{X}$ B) X-5 C) X D) X+5
13	If: 3 X y = 10, then: $X \propto$
	If: X y = 5, then: y $\infty$
14	If: 5 X y = 6, then
11 12 13 14	If: $5 \times y = 6$ , then
	تطبيق مذكرات جاهزة للطباعة
<b>388</b>	### #################################



<b>æ</b> (	Mat	thematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term	<b>*</b>
<b>₩</b>			
	F.c.	say problems:	
		say prootents.	88
	1	If : y ∝ X and y = 14 when X = 42 , Find :	
** **			<b>33</b>
<b>**</b>		1) the relation between X and y	
		2) the value of y when X = 60	
		, , , , , , , , , , , , , , , , , , ,	<b>33</b>
** **			88
<b>88</b>			<b>83</b>
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			<b>88</b>
<b>**</b>			<b>**</b>
** ***			***
<b>33</b>	2	15 the moutiful active inventor state and active in the motories.	<b>88</b>
<b>88</b>		If : y $\infty$ the multiplicative inverse of the expression $\frac{1}{\chi^2}$ , Find the relation	<b>88</b>
		between X and y, if $y = 4$ as $X = 3$ , then find the value of y when $X = 9$	
<b>88</b>		2024	
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			## ##
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<b>33</b>		تعبيق التعلم الشاعلي عن بعد	<b>**</b>
<b>**</b> _	3		
	J	If : $y \propto (X + 1)$ and $X = 3$ when $y = 2$ , then Find the relation between X and y	
			<b>33</b>
<b>33</b>			<b>88</b>
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<b>B</b> (	Mat	thematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term ####################################	<b>33</b>
**			## ##
<b>33</b>	4	If: $\frac{21 X-y}{7 X-z} = \frac{y}{z}$ , then prove that: $y \propto z$	<b>88</b>
<b>33</b>		7X-z z, then prove that: y & z	8
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**			8
# #			88
**			
# #			88
<b>33</b>			
**			<b>33</b>
# #	5	If: $X^4 y^2 - 14 X^2 y + 49 = 0$ , then prove that: $y \propto \frac{1}{X^2}$	
**		X <sup>2</sup>	<b>3</b>
# #			<b>**</b>
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# #		تطبيق التعلم التفاعلي عن بعد	<b>88</b>
# #	6	If y = a – 9 and y $\propto \frac{1}{\chi^2}$ and a = 18 when X = $\frac{2}{3}$ , find the relation between y	
# #			## ##
**		and X , then deduce the value of y when X = 1	88
**			<b>3</b>
**			<b>88</b>
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**		تطبيق مذكرات حاهزة للطباعة	
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		حمَل التطبيق على موبايلك الأندرويد أو الأيفون موقع مذكرات باهزة للطباعة  - www.cryp2day.com	

<b>\$</b> ( Ma	thematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>3333333333333333333333333333333</b>
# 7 # 7 # # # # # # # # # # # # # # # #	A car moves with a uniform velocity where the distance varies directly with the time (t). If the car covered a distance of 150 km. in 6 hours, find the distance covered by that car in 10 hours.
## ## ## ## ## ## ## ## ## ## ## ## ##	
***	
** ** ** ** ** **	If the number of hours (n) needed for carrying out a work varies inversely as
***	the number of workers (X) who carry out this work. If the work is carried out by 6 workers within 4 hours, what is the needed time for carrying out the work by 8 workers
######################################	2.024
8	GPS-APP
# # # Cla	ق تصبیق التعلم التقاعلي عن بعد
	The relation which represents the direct variation between a and b is  A) $ab = 3$ B) $\frac{a}{5} = \frac{2}{b}$ C) $A + b = 5$ D) $\frac{a}{4} = \frac{b}{7}$
** 2	The relation represents the direct variation between X and y which is
# 3 # 3	The relation which represents the direct variation between X and y is
** ** ** ** ** ** **	الله الله الله الله الله الله الله الله

<b>₩</b> ( Ma	thematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term
# 4	Which of the following relations represents an inverse variation between the two variables X and y?
**	A) $Y = \frac{X}{7}$ B) $Xy = 7$ C) $Y = 7X$ D) $\frac{y}{X} = \frac{7}{2}$
5	If: $y \propto X$ and $y = 1$ when $X = 4$ , then $y = $ When $X = 8$ A) 1 B) 2 C) 4 D) 8
6	If: $y \propto X$ and $X = 2$ when $y = 4$ , then the proportion constant =
# 7 # **	If: y $\propto$ X and y = 6 at X = 2, then y =
8	If y varies inversely with X , and X = $\sqrt{2}$ when y = $\frac{3}{\sqrt{2}}$ , then : the relation
***	between X and Y is
<b>3</b> 9	If y varies inversely with X, and $X = \sqrt{5}$ when $y = \frac{3}{\sqrt{5}}$ , then: the relation
	between X and Y is  A) $Y = 3 X$ B) $X y = \frac{5}{3}$ C) $X y = 3$ D) $y = \frac{5}{3} X$
10	-/٧
	A) Directly as y <sup>2</sup> b) Inversely as y <sup>2</sup>
**	c) Inversely as y d) Inversely as √y
# 11 # 11	b 5, and a 13-APP
**	A) B
12	If: Xy = m where m ≠ 0, then y varies inversely with
***	A) X B) m + X C) $\frac{1}{X}$ D) $\frac{m}{X}$
13	If:3 X y = 8, then:
**	A) $X \propto y$ B) $y \propto X$ C) $3X \propto 8y$ D) $X \propto \frac{1}{y}$
# 14	If: X y <sup>5</sup> = Constant, then X varies inversely as
***	A) $\frac{1}{5}$ B) $y^5$ C) y D) $y^2$
# 15	If: $\frac{y+3}{y} = \frac{X+2}{X}$ where $X \neq y \neq zero$ , then: $y \propto$
***	A) X B) $\frac{1}{X}$ C) X+2 D) X+5
# ####	######################################

Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term REE 16 If:  $y - X = \frac{1}{X} - \frac{1}{V}$  where  $X \neq y \neq zero$ , then ..... **33 33** A)  $y \propto X + 1$ B)  $y \propto X$ 17 If: y = 5 X, then  $y \propto$  ..... D)  $\frac{1}{X^2}$ C)  $\frac{1}{X}$ 8 A) X B) X + 5 8 18 If:  $v^2 - 4 \times v + 4 \times^2 = 0$ , then ..... 8 B)  $y \propto \chi^2$  C)  $y \propto \frac{1}{\chi}$ D)  $y \propto \frac{1}{x^2}$ 8 A)  $y \propto X$ **88** 19 If:  $y^2 + 9 X^2 = 6 X y$ , then ..... B)  $y \propto \chi^2$  C)  $y \propto \frac{1}{\chi}$ D)  $y \propto \frac{1}{y^2}$ A)  $y \propto X$ 8 20 If the total cost of a trip is (y), some of it is constant (a) and the other is 88 directly proportional with the number of participants (X), then ..... **33** A) y = a Xc)  $y=a+\frac{m}{x}$  (m is constant  $\neq 0$ ) d) y=a+m X (m is constant  $m \neq 0$ ) Essay problems: 2024 If:  $y \propto \frac{1}{x}$  and y = 3 when X = 2, Find: 1) the relation between X and y 2) the value of y when x = 9.5 التفلم التفاه

M	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>B####################################</b>	)[
2		
	If: $y^2 \propto X^3$ , Find the relation between X and y where y = 3 as X = 2	
		<b>1</b>
3	If: $\frac{a+b}{3} = \frac{2b+c}{6}$ , then prove that: $c \propto a$	
	3 6 ,	
4	If: $X^2 y^2 - 6 X y + 9 = 0$ , then prove that: y varies inversely as X	
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	تطبيق التعلم التفاعلي عن بعد	
<u> </u>		<b>8</b>
5	If: $X = z + 8$ and z varies inversely as y and $z = 2$ as $y = 3$ , Find y as $X = 3$	
=		
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	حمَّل التطبيق على موبايلك الأندرويد أو الأيفون موقع مذكرات باهزة للطباعة <b>-</b> www.cryp2day.com	

Mat	thematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term ************************************
6	If ( h ) the height of a right circular cylinder (its volume is constant) varies inversely as the square of radius length (r) and h = 27 cm. when $r = 10.5$ ,
	Find h when $r = 15.75$ cm.
7	If the weight of a body on the moon (W) is directly proportional with its weight on the ground (R) If the body weighs 84 kg., on the ground and its weight on the moon is 14 kg. What will its weight be on the moon if its weight
	on the ground is 144 kg?
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8	If the value of speed v that water passes through a hose nuzzle inversely changes with the square of the hose nuzzle radius length r and v = 5 cm./s.
	when $r = 3$ cm., find v when $r = 2.5$ cm.
•	
	تطبيق مذكرات باهزة للطباءة
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Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term

## Sheet (9)

## Mean & Standard Deviasion

### Mean:-

#### Remember that



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The total of values The mean of a set of values =Number of values

#### For example:

- If the marks of 5 pupils are: 25, 23, 21, 22, 24
- Then the mean of marks =  $\frac{25 + 23 + 21 + 22 + 24}{5}$  = 23 marks.

#### Notice that:

$$23 \times 5 = 25 + 23 + 21 + 22 + 24$$

#### Finding the mean of data from the frequency table with sets

#### Example

The following table shows the distribution of the marks of 50 pupils in mathematics:

Sets	10 –	20 –	30 -	40 –	50 -	Total
Frequency	. 8	12	2024	9	7	50

Find the mean of these marks.

#### Solution

1 Determine the centres of sets according to the rule:

The centre of a set = 
$$\frac{\text{the lower limit} + \text{the upper limit}}{2}$$

### 2 Form the vertical table:

Set	Centre of the set « X »	Frequency « f »	$X \times f$
10 –	1	8	
20 –	11.9 1.0	12	
30 –	1 4 6 1	14	
40 – 50 –	1 1	9	
50 –		7	
	Total		

The mean = 
$$\frac{\text{The sum of } (X \times f)}{\text{The sum of } f}$$
 =

### Median : -

Remember that



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The median is the middle value in a set of values after arranging it ascendingly or descendingly, such that the number of values which are less than it is equal to the number of values which are greater than it.

• To find the median of a set of values • we do as follows:

## We arrange the values ascendingly or descendingly

If the values number is odd, then

If the values number is even, then

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The median is the value lying in the middle exactly.

The median

The sum of the two values lying in the middle

For example:

If the values are

42, 23, 17, 30 and 20

We arrange them ascendingly as follows

17,20,23,30,42

The median = 23

For example :

If the values are

27, 13, 23, 24, 13, 21

We arrange them ascendingly as follows

The median =  $\frac{21 + 23}{2} = 22$ 

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Mode : -

#### Remember that

The mode of a set of values is the most common value in the set, or in other words, it is the value which is repeated more than any other values.

For example:

The mode of the set of the values: 7, 3, 4, 1, 7, 9, 7, 4 is 7

#### Dispersion of a set of values

It means the divergence or the differences among its values.

- The dispersion is small if the difference among the values is little while the dispersion is great if the difference among the values is great, the dispersion is zero if all the values are equal.
- **i.e.** The dispersion is a measure that expresses how much the sets are homogeneous.

## Remark

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## lefathIf all values ( individuals ) are equal then the dispersion ( $\sigma$ ) is zero

• If the standard deviation equals zero that means the all values are equal, it is the perfect homogeneous case (the vanished dispersion).

## **Dispersion measurements**

The range (the simplest measure of dispersion):

It is the difference between the greatest value and the smallest value in the set.

The range = the greatest value – the smallest value

#### ¥ For example :

- If the values of set A are 60, 58, 62, 61 and 59
- $\therefore$  The range = 62 58 = 4
- If the values of set B are 72, 78, 46, 65 and 39
- $\therefore$  The range = 78 39 = 39

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So the set B is more divergent than the set A

2 Standard deviation:

## First: Calculating the standard deviation of a set of values:

The standard deviation 
$$\sigma = \sqrt{\frac{\sum (x - \overline{x})^2}{n}}$$

Where:

X denotes a value of the values,

 $\overline{x}$  denotes the mean of the values and it is read as x bar,

n denotes the number of values,

 $\Sigma$  denotes the summation operation.

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Firstly: Calculating the SD of a set of value:

$$\overline{x} = \frac{\sum x}{n}$$

$$\sigma = \sqrt{\frac{\sum (x - \overline{x})^2}{n}}$$

Ex. (1): Calculate the standard deviation of the values: 8, 9, 7, 6 and 5

X	$x-\overline{x}$	$(x-\overline{x})^2$
Total		

Secondly: Calculating the SD of a frequency distribution:

$$\overline{x} = \frac{\sum (x \times k)}{\sum k}$$

$$\sigma = \sqrt{\frac{\sum (x - \overline{x})^2 k}{\sum k}}$$

Second: Calculating the standard deviation of a frequency distribution:

For any frequency distribution:

The standard deviation 
$$\sigma = \sqrt{\frac{\sum (x - \overline{x})^2 k}{\sum k}}$$

Where:

تطبيق التعلم التفاعلي عن بعد X represents the value or the centre of the set,

k represents the frequence of the value or the set,

 $\sum$  k is the sum of frequences and  $\overline{\chi}$  (the mean) =  $\frac{\sum (\chi \times k)}{\sum k}$ 

Secondly: Calculating the SD of a frequency distribution:

$$\overline{x} = \frac{\sum (x \times k)}{\sum k}$$

$$\sigma = \sqrt{\frac{\sum (x - \overline{x})^2 k}{\sum k}}$$

Ex. (2): The following table shows the distribution of ages of 20 persons in years:

Age	15	20	22	23	25	30	Total
Persons	2	3	5	5	1	4	20

Find the standard deviation of the age.

x	k	$x \times k$	$x - \overline{x}$	$(x-\overline{x})^2$	$(x-\overline{x})^2 \times k$
Total					

$$\bar{x} =$$

$$\sigma =$$

Thirdly: Calculating the SD of a frequency distribution of sets:

$$\overline{x} = \frac{\sum (x \times k)}{\sum k}$$

$$\sigma = \sqrt{\frac{\sum (x - \overline{x})^2 k}{\sum k}}$$

**Which:** X is the center of the set and get from:  $x = \frac{lower\ limit + upper\ limit}{2}$ 

Ex. (2): Calculate the standard deviation for the following frequency distribution:

Sets	0 –	2 –	4 –	6 –	8 –	Total
Frequency	5	9	15	15	6	50

Sets	x	k	$x \times k$	$x-\overline{x}$	$(x-\overline{x})^2$	$(x-\overline{x})^2 \times k$
Total						

$$\bar{x} =$$

[2] A school has 300 male students and 500 female students wanted to do a survey on a sample of 24 students representing each layer according to its size.  The total number of the students =
The total number of the students =
The number of 1 <sup>st</sup> grade student in the sample =
The number of 1 <sup>st</sup> grade student in the sample =
The number of 1 <sup>st</sup> grade student in the sample =
The number of 2 <sup>nd</sup> grade student in the sample =
The number of 2 <sup>nd</sup> grade student in the sample =
<ul> <li>[4] Complete: <ul> <li>(1) Dispersion measurements are</li></ul></li></ul>
<ul> <li>(1) Dispersion measurements are</li></ul>
<ul> <li>(2) The simplest measure of the dispersion is</li></ul>
<ul> <li>(2) The simplest measure of the dispersion is</li></ul>
values from their mean is called
<ul> <li>(4) If the standard deviation equals zero, then</li></ul>
<ul> <li>(5) The dispersion to any set equally values equals</li></ul>
<ul> <li>(6) The mean of the set of the values 7, 5, 9, 11, 3 is</li></ul>
<ul> <li>(7) The range of the set of the values 6, 5, 9, 4, 12 is 9</li></ul>
<ul> <li>(8) If the standard deviation for nine of the values is 3, then ∑(x-x̄)² =</li></ul>
(9) The suitable statistical method for examining products of a factory is  [5] Choose the correct answer:  (1) The most repeated value in a set of values represents the
[5] Choose the correct answer:  (1) The most repeated value in a set of values represents the
<ul> <li>(1) The most repeated value in a set of values represents the</li></ul>
a) median b) range c) mode d) mean  (2) The difference between the greatest value and the smallest value in a set of values is called  a) median b) range c) mode d) mean
(2) The difference between the greatest value and the smallest value in a set of values is called
a) median b) range c) mode d) mean
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	lathematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>3888888888888888888888888888888888888</b>
C	hoose the correct answer :
1 1 2 2 2	The most repeated value in a set values represents  A) Median  B) Range  C) Mode  D) measn
# 2 # 2	The mean for the values: 2, 5, 6 and 7 is
# 3 # 3	The arithmetic mean for the values: 3, 4, 6 and 7 equals
# 4 # # # # # # # # # # # # # # # # # #	The arithmetic mean for the values: 3,5,6,7 and 9 is
\$ 5 \$ \$	The arithmetic mean for the values : 4 , 13 , 18 , 25 , 30 is
## 6 ##################################	The mean for the values: 5, 4, 2, 6, 10 and 3 equals
* 7 * *	The arithmetic mean for the set of values :7, 3, 6, 9 and 5 is
## 8 ## ## ## ## ## ## ## ## ## ## ## ## ##	The mean for : 30 , 20 , 50 , 60 is
# 9 # 9	The arithmetic mean for the values: 37, 10, 23, 24 and 16 is
## 10 ## ##	If The mean for the values: a, 5, 8, 7, 6 equals 6 then a =
# 11 # 11	If the mean for the numbers : 12 , 17 , 19 , X , 14 is 15 , then X =A) 10 B) 12 C) 13 D) 15
## 12 ## ## ## ## ## ## ## ## ## ## ## ## ##	The difference between the maximum and minimum value for a set of data represents
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13	The difference between the greatest and smallest value for a set of data represents
## 14 ##################################	The range for the values 2, 13, 12, 16 and 14 is
15 15	If the range for the values: 2, 7, a, 6 is 8 where a > 0, then a =
16	The range for the values: 3, 8, 5, 20, 12 is
17	The range for the values: 5, 2, 8, 12 and 9 is
18	The range for the values : 6 , 8 , 4 , 10 , 2 is
19	The range for the values: 7, 3, 6, 9, 5 is
# 20 # #	The range for the values: 7, 4, 9, 5 and 13 is
# 21 # 21	The range for the values : 7 , 8 , 11 , 13 , 6 is
# 22 # 8	The range for the values: 7, 13, 16, 9 and 5 is
# 23 # 23	The range for the values : 7 , 13 , 15 , 8 , 6 is
# 24 # 24	The range for the values: 8,3,4,5 and 9 is
25 ####################################	The range for the values: 8, 5, 10, 6 and 14 is
## ## ## ## ##	قطبيق مذكرات داهزة للطباعة ق \$
	حمّل التطبيق على موبايلك الأندرويد أو الأيفون موقع مذكرات جاهزة للطباعة <b>-</b> www.cryp2day.com

# (M	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>333333333333333333333333333333333333</b>
# 26 # 28	The range for the values: 11, 2, 3, 6 and 8 is
** 27 ** 27	The range of : 15 , 7 , 23 , 35 and 10 is
# 28 # 28	The range for the values : 17 , 13 , 16 , 19 and 15 is
# 29 # 29	The range for the values: 18, 3, 8, 23 and 13 is
# 30 # 30	The range of the set of the values : 43 , 51 , 55 , 47 , 60 is
# 31 # 31	The most common measure of dispersion is
* 32 * 32	The most common measure of dispersion and the most accurate is
## 33 ## ## ## ## ## ## ## ## ## ## ## ## ##	From the measures of dispersion is the
34 38 38	One of the dispersion measurements is  A) Mean B) Range C) median D) Mode
35 38 38	The simplest and easiest dispersion measure is the
36 38 38	The common measure of dispersion is
# 37 # 38	The standard deviation for the values: 7, 7, 7 equals
38	If the set of quantities are equal in values , then A) $\sigma = 0$ B) $\overline{\mathbf{X}} = 0$ C) $\mathbf{X} - \overline{\mathbf{X}} > 0$ D) $\mathbf{X} - \overline{\mathbf{X}} < 0$
<b>39</b>	If all the individuals are equals in values, then
# # # # ## # ##	المبيق مذكرات باهزة للطباعة و الطباعة و الطباعة و الفيفون (

Mathematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>333333333333333333333333333333333333</b>
If: $\sum_{\alpha} (X - \overline{X})^2 = 36$ for a set of values whose number is 9, then $\sigma = \dots$ A) 2 B) 4 C) 18 D) 27
Selecting a sample of layers of a statistical society is called sample  A) Random B) bunch C) Deliberate D) Class (layer)
If 18 is greatest individual of a set of individuals and its range is 6, then the smallest individual of this set =
The positive square root of the average of squares of deviations of values form its arithmetic mean is called
Essay problems:
Calculate the standard deviation for the next data : 16, 32, 5, 20, 27 $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
If 5 , 6 , 7 , 8 and 9 are marks of pupil in the math. Exams for 5 months , find the mean and the standard deviation. $ x                                  $
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The following frequency distribution shows the number of children of \* some families in a new city: Number of children Number of families Calculate the mean and the standard deviation of the number of children 

х	k	$x \times k$	$x-\overline{x}$	$(x-\overline{x})^2$	$(x-\overline{x})^2 \times k$
Total					

 $\overline{x} = \sigma =$ 

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 The following are fr<mark>eque</mark>ncy distribution for a number of defective units found in 100 boxes of manufactured units:

Number of defective units	0	1	2	3	4	5
Number of boxes	3	16	17	25	20	19

Find the standard deviation of the defective units.

X	krai	υ£×klc	تع <del>ل</del> ام لاتف	$(x + \overline{x})^2$	$(x-\overline{x})^2 \times k$
Total					

 $\overline{x} = \sigma =$ 

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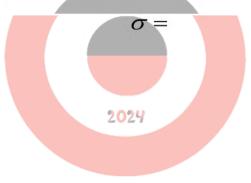
### The following frequency distribution shows the ages of 10 students:

Age in years	5	8	9	10	12	Total
Number of families	1	2	3	3	1	10

#### Calculate the standard deviation to ages in years

x	k	$x \times k$	$x - \overline{x}$	$(x-\overline{x})^2$	$(x-\overline{x})^2 \times k$
Total					

 $\bar{x} =$ 



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# **Sheet (10)**

## The main trigonometrical ratios of the acute angle

The relation between each of the degrees, the minutes and the seconds

• The degree = 60 minutes.

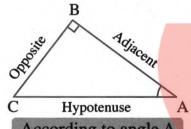
- The minute = 60 seconds
- **i.e.** The degree =  $60 \times 60 = 3600$  seconds.

## The main trigonometrical ratios of the acute angle

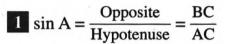
The trigonometrical ratio of the acute angle

It is the ratio between two side lengths of the right-angled triangle that contains this angle.

**i.e.** If  $\triangle$  ABC is a right-angled triangle at B, then:

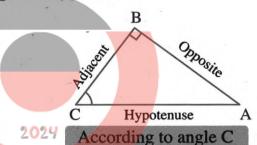


According to angle A



$$2 \cos A = \frac{Adjacent}{Hypotenuse} = \frac{AB}{AC}$$

$$3 \tan A = \frac{\text{Opposite}}{\text{Adjacent}} = \frac{A}{AB}$$



 $1 \sin C = \frac{\text{Opposite}}{\text{Hypotenuse}} = \frac{\text{AB}}{\text{AC}}$ 

$$2 \cos C = \frac{\text{Adjacent}}{\text{Hypotenuse}} = \frac{\text{BC}}{\text{AC}}$$

$$3 \tan C = \frac{Opposite}{Adjacent} = \frac{AB}{BC}$$

#### ¥ For example

In the opposite figure:

If  $\triangle$  ABC is a right-angled triangle at B,

AB = 3 cm., BC = 4 cm. and AC = 5 cm., then:



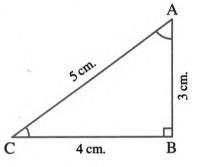
$$2 \cos A = \frac{3}{5}$$

$$3 \tan A = \frac{4}{3}$$

$$1 \sin C = \frac{3}{5}$$

$$\cos C = \frac{4}{5}$$

$$3 \tan C = \frac{3}{4}$$



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## We can deduce that:

The sine of any angle equals the cosine of its complementary and vice versa

**i.e.** If  $\angle A$  and  $\angle B$  are acute angles, and  $\sin A = \cos B$ 

then:  $m (\angle A) + m (\angle B) = 90^{\circ}$ 

## Generally

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The tangent of the angle =  $\frac{\text{The sine of the angle}}{\text{The cosine of the angle}}$ 

## Choose the correct answer:

1 For any acute angle A,  $\tan A = \dots$ 

sin A (d) sin A + cos A

- (a)  $\frac{\cos A}{\sin A}$
- (b) sin A cos A
- (c)  $\frac{\sin A}{\cos A}$
- (d)  $\sin A + \cos A$

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- 2 If  $\triangle$  ABC is a right-angled at B, then:  $\sin A + \cos A$ .....
  - (a) equals 0
- (b) equals 1
- (c) is less than 1
- (d) is more than 1
- 3 If:  $\sin A = \cos A$ , then measure angle A = 24......
  - (a)  $30^{\circ}$
- (b) 45°
- (c) 60°
- (d) 90°

- 4  $\tan H \times \cos H = \cdots$ 
  - (a) cos H
- (b)  $\frac{1}{\cos H}$
- (c)  $\frac{1}{\sin H}$
- (d) sin H

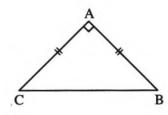
5 In the opposite figure :

ABC is a right-angled triangle at A,

AB = AC,  $tan C = \cdots$ 

(a) 1

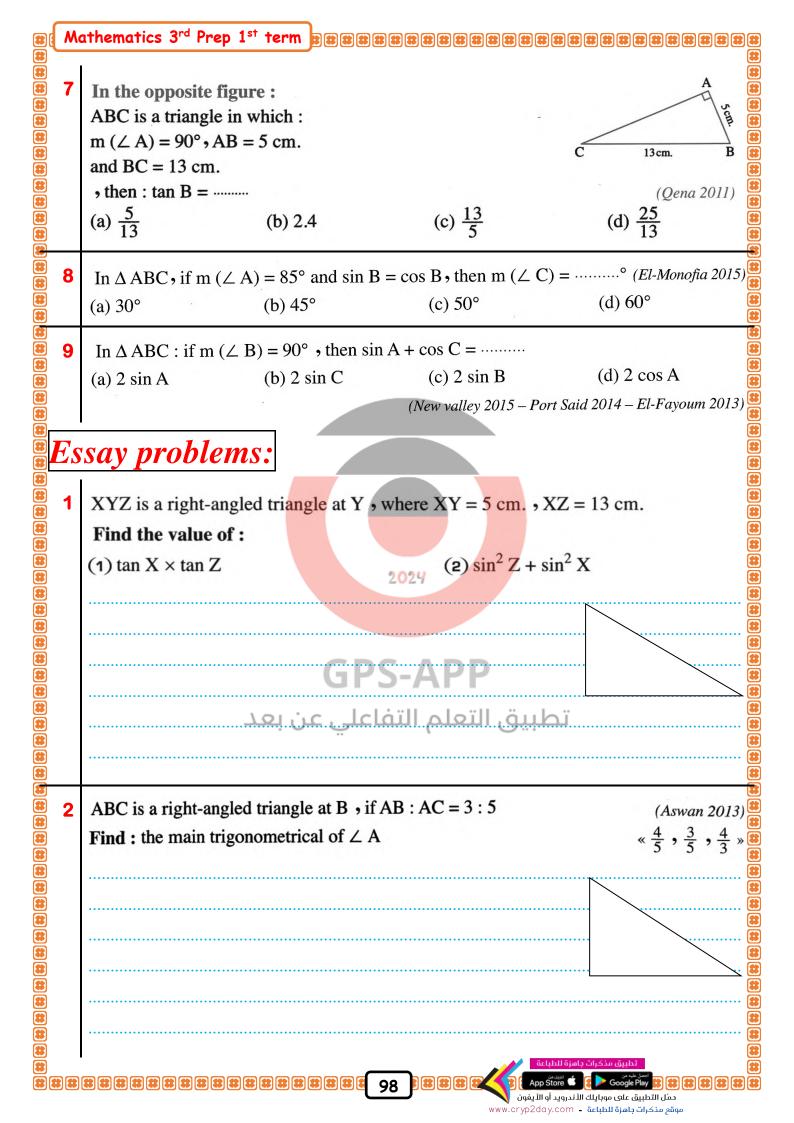
- (b)  $\frac{1}{2}$
- (c)  $\frac{\sqrt{3}}{2}$
- (d)  $\frac{1}{\sqrt{3}}$

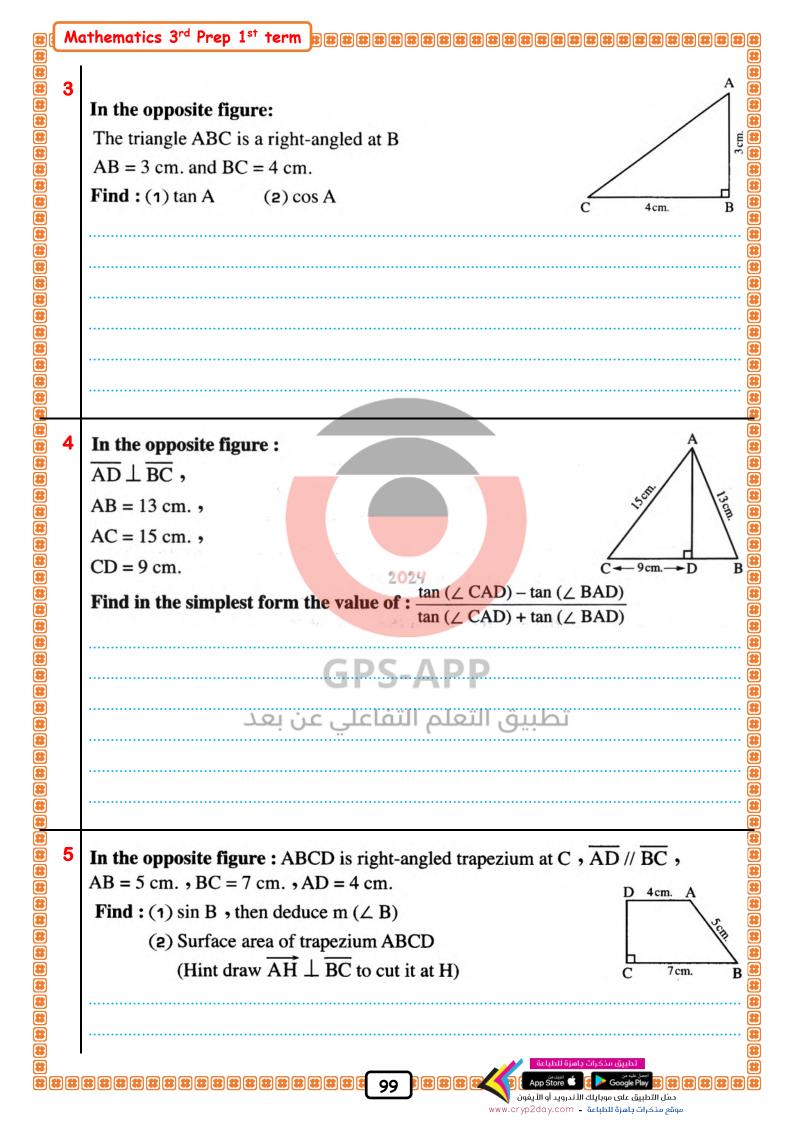


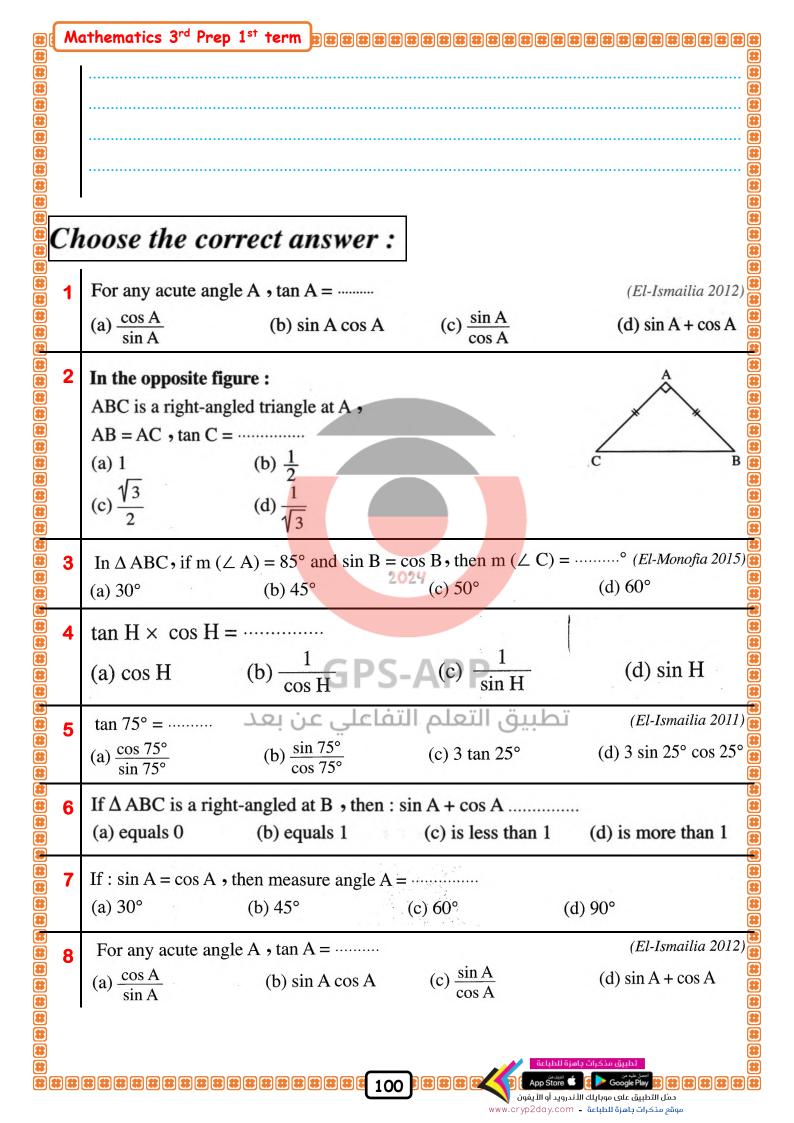
6  $\tan 75^{\circ} = \dots$ 

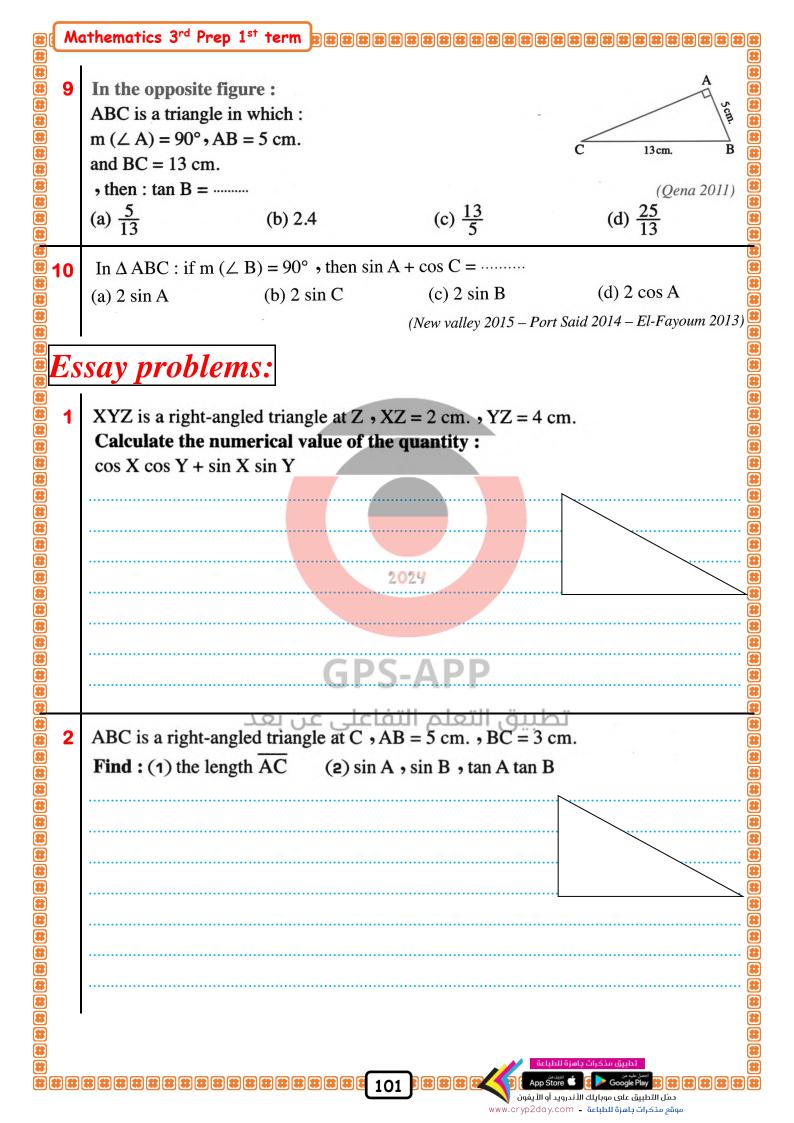
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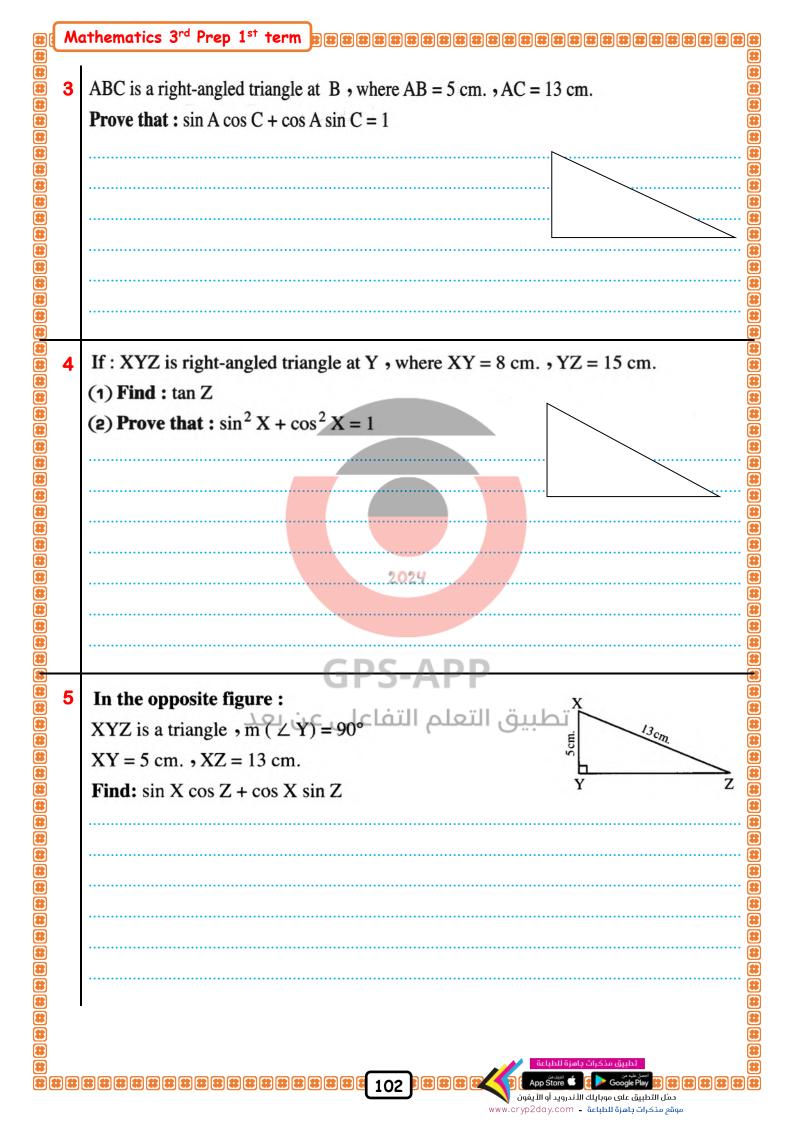
- $(a) \frac{\cos 75^{\circ}}{\sin 75^{\circ}}$
- (b)  $\frac{\sin 75^{\circ}}{\cos 75^{\circ}}$
- (c) 3 tan 25°
- (d) 3 sin 25° cos 25°

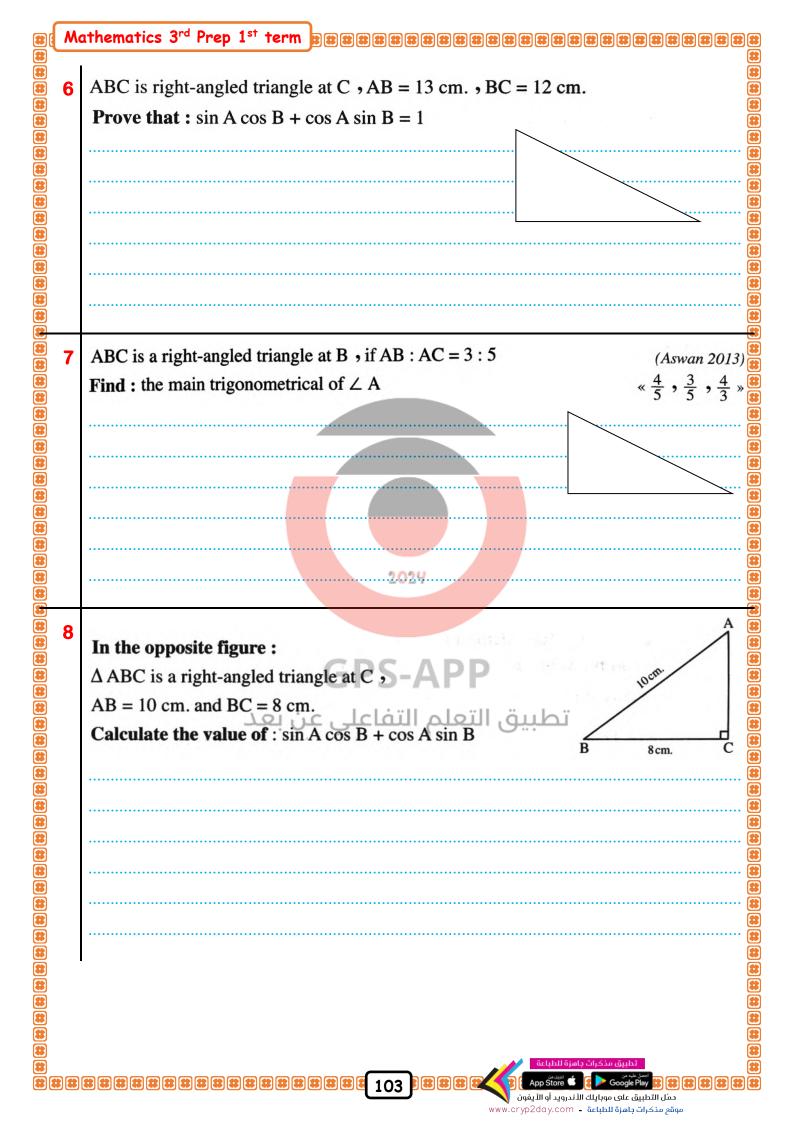


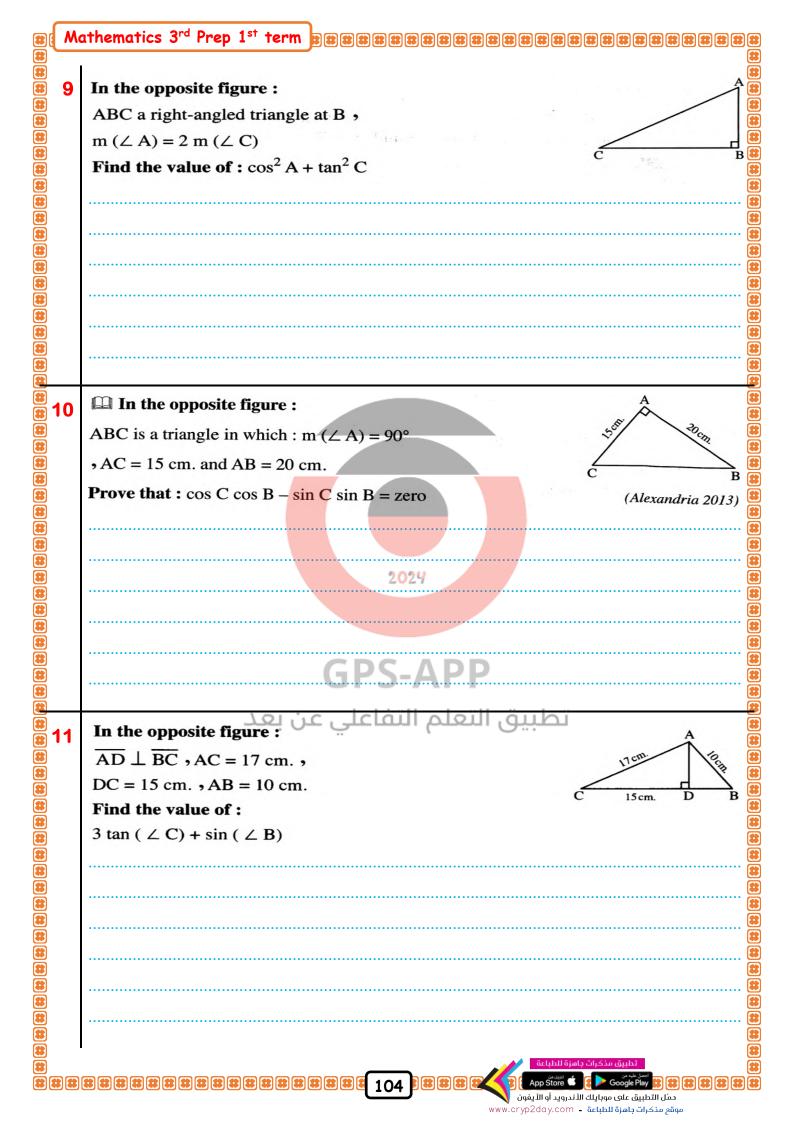




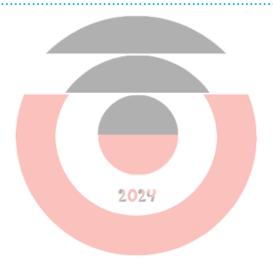








Mo	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>B################</b>				
12	In the opposite figure: ABCD is right-angled trapezium at $C \cdot \overline{AD} // \overline{BC}$ ,				
	AB = 5  cm., $BC = 7  cm.$ , $AD = 4  cm.$	D 4cm. A			
	<b>Find</b> : (1) sin B	72			
	(2) Surface area of trapezium ABCD	/sp			
	(Hint draw $\overrightarrow{AH} \perp \overrightarrow{BC}$ to cut it at H)	C 7cm. B			



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## **Sheet (11)**

## The main Trigonometrical Ratios of Some Angles

The following table summarizes the trigonometrical ratios of the angles measuring  $30^{\circ}$ ,  $60^{\circ}$  and  $45^{\circ}$ :

The measure of the angle	30°	60°	45°
sin	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$
cos	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$
tan	$\frac{1}{\sqrt{3}}$	1/3	1

Using the calculator

First Finding the main trigonometrical ratios of a given angle :

In the calculator, there are three keys: sin 2,2 cos, ton

- 1 The key in means sine.
- 2 The key cos means cosine.
- 3 The key means tangent.

Example 4 By using the calculator, find the value of each of the following approximated to the nearest 4 decimals:

- 1 sin 36°
- 2 cos 72° 35

3 tan 50° 46 25

Solution

Use the keys of the calculator as the following sequence from left:

1 sin 3 6 =

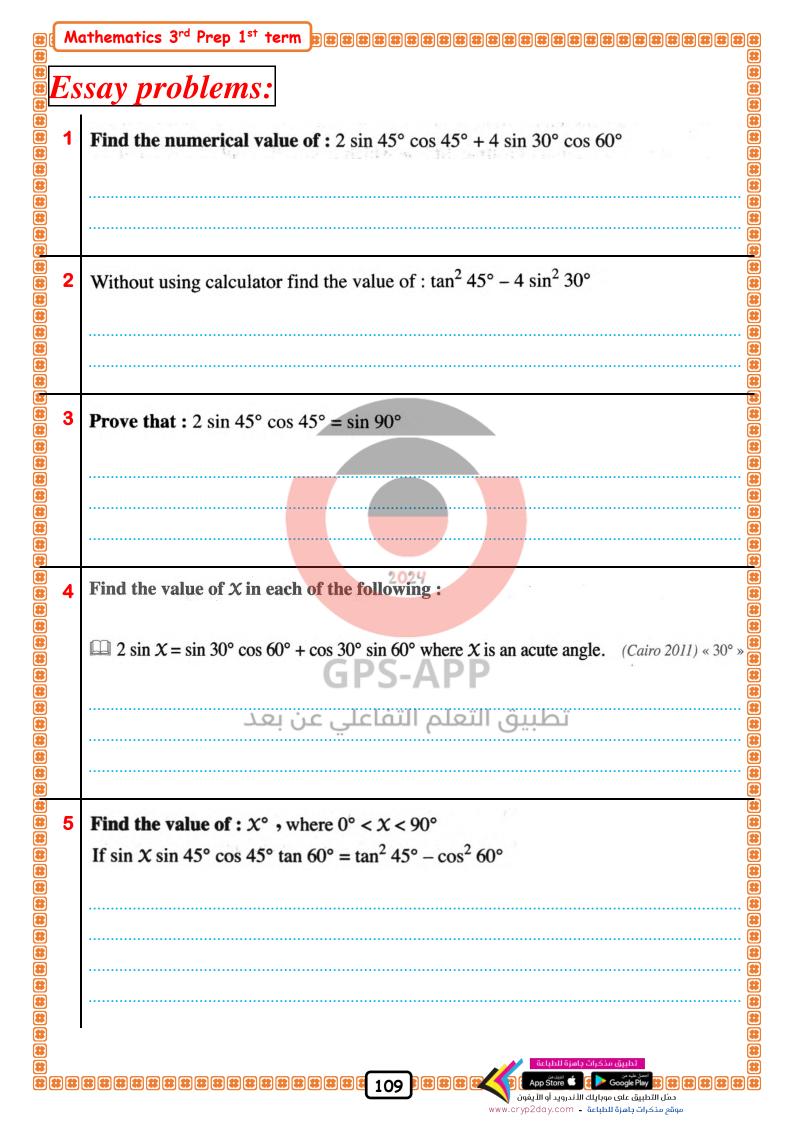
- $\therefore \sin 36^{\circ} \simeq 0.5878$
- 2 05 7 2 05 3 5 05 =
- $\therefore \cos 72^{\circ} \ 3\dot{5} \simeq 0.2993$
- 3 tan 5 0 0; 4 6 0; 2 5 0; =
  - ∴  $\tan 50^{\circ} 4\hat{6} 2\hat{5} \approx 1.2250$

Second Finding the measure of the angle if one of its trigonometrical ratios is given:

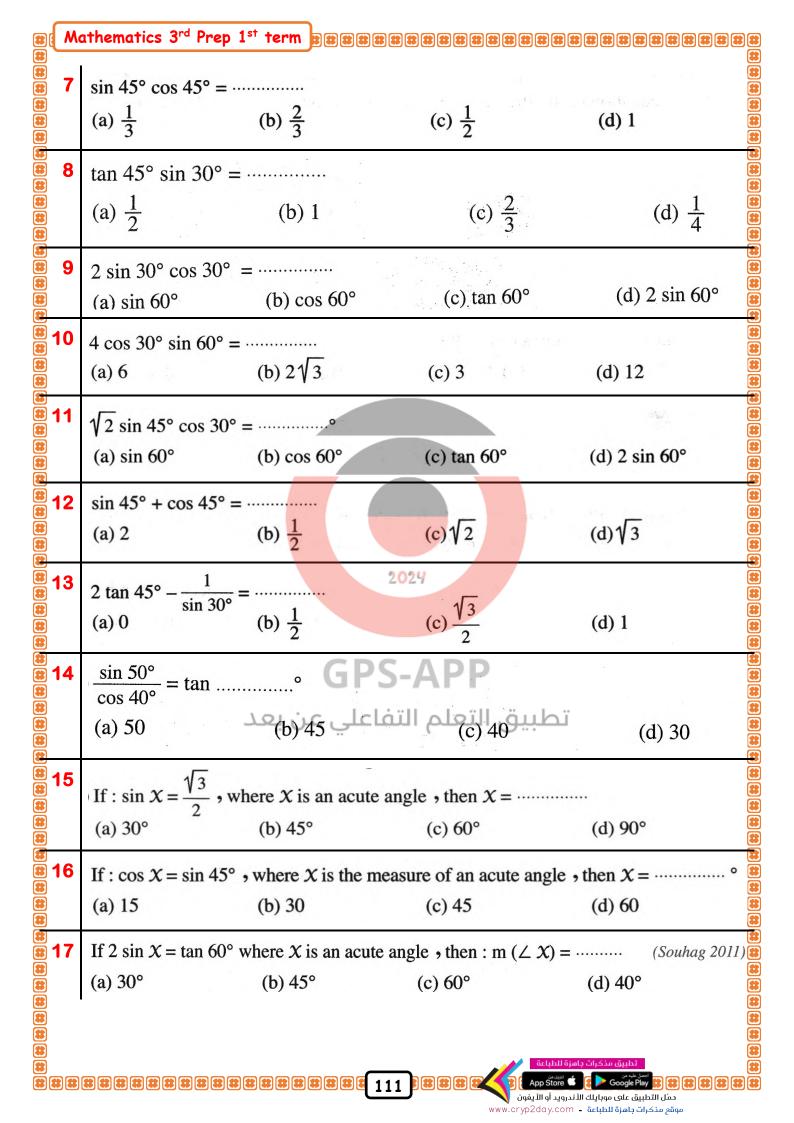


Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term Example [5] Find A in each of the following, where A is the measure of an acute angle:  $1 \sin A = 0.8$  $2 \cos A = 0.7152$ 3  $\tan A = 1.5156$ Solution Use the keys of the calculator as the following sequence from left:  $\therefore A \simeq 53^{\circ} \hat{7} \hat{48}$  $\therefore A \simeq 44^{\circ} \ 20^{\circ} \ 25^{\circ}$  $\therefore A \simeq 56^{\circ} 3\mathring{4} 5\mathring{9}$ Choose the correct answer:  $\tan 75^{\circ} = \dots$ (El-Ismailia 2011 (a)  $\frac{\cos 75^{\circ}}{\sin 75^{\circ}}$ (b)  $\frac{\sin 75^{\circ}}{\cos 75^{\circ}}$ (d) 3 sin 25° cos 25° (c) 3 tan 25° 8  $\sin 60^{\circ} + \cos 30^{\circ} - \tan 60^{\circ} = \cdots$ (c)  $2\sqrt{3}$  $(b)\sqrt{3}$ (a) zero (d) 1  $\sin^2 45^\circ + \cos^2 45^\circ = \cdots$ (a)  $2\sqrt{2}$ (b) 0(c) - 1(d) 1 **33** If X is the measure of an acute angle and  $\sin x = \frac{1}{2}$ , then:  $\sin 2x = \dots (El-Ismailia\ 2012)$ (c)  $\frac{\sqrt{3}}{2}$ ## ## (b)  $\frac{1}{4}$ (d)  $\frac{1}{2}$ (a) 1 If  $\sin 30^{\circ} = \cos \theta$ , where  $\theta$  is an acute angle, then m ( $\angle \theta$ ) = ......° تطبيق ال19(ع) التفاعلي عر45(d)د (a) 60  $\cos (3 X + 6^{\circ}) = \sin 30^{\circ}$  such that  $(3 X + 6^{\circ})$  is an acute angle, then the value of  $X = \cdots$ **3** (a)  $60^{\circ}$ (d) 18° (b) 54° (c) 36° If:  $2 \sin x = 1$  where  $0^{\circ} < x < 90^{\circ}$ , then m ( $\angle x$ ) = ...... (a) 60 (b) 45 (c) 30 (d) 50 If:  $\sin \frac{x}{2} = \frac{1}{2}$  such that  $\left(\frac{x}{2}\right)$  is the measure of an acute angle, then  $\tan x = \dots$ (b)  $\frac{1}{\sqrt{3}}$  $(c)\sqrt{3}$ (a)  $\frac{1}{\sqrt{2}}$ وقع مذكرات طهزة للطباعة - www.crvp2dav.com

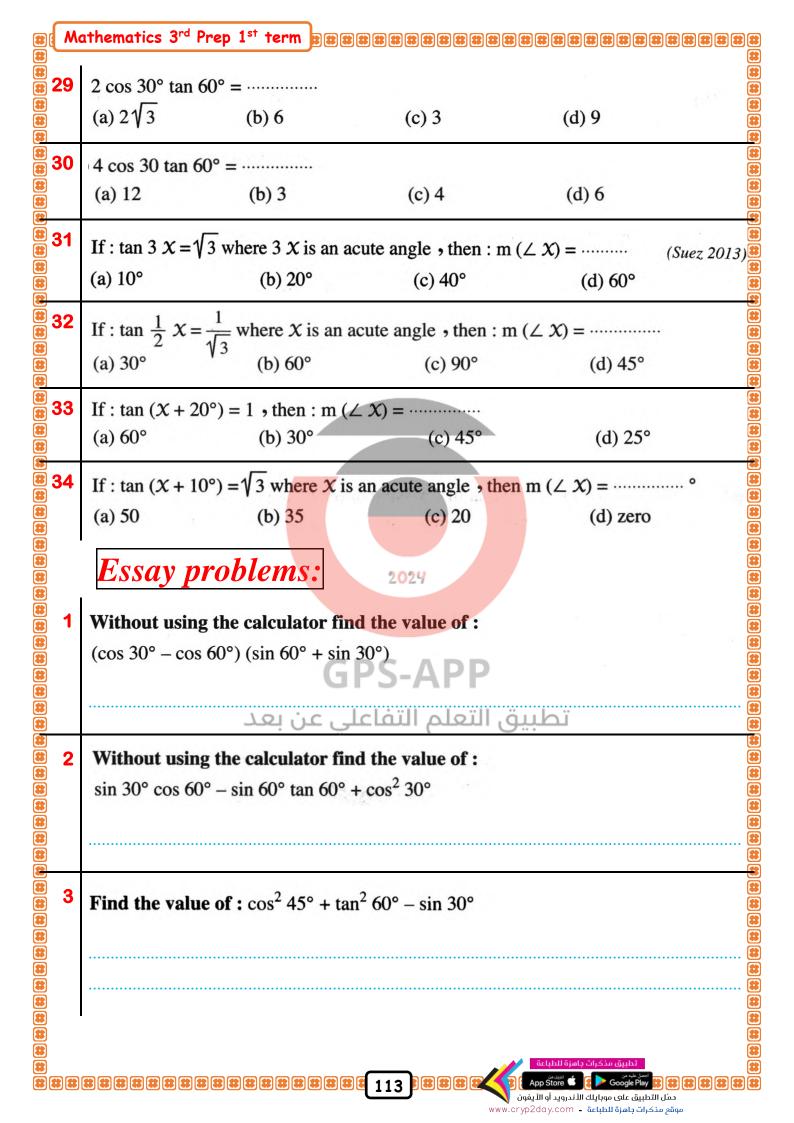
## (M	Mathematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term							
<b>8</b> 9	If: $\sqrt{2} \cos 3 x$	Z = 1, where $X$ is n	neasure of an acute ang	le, then $X = \cdots$				
<b>*</b>	(a) 15	(b) 30	(c) 45	(d) 60				
# # 10	If: $\tan x = 2 \sin 60^{\circ}$ , where $0^{\circ} < x < 90^{\circ}$ , then $x = \dots \circ$							
<b>8</b>	(a) 60	(b) 45	(c) 30	(d) 15				
<b>8</b> <b>9</b> 11	If: $\cos x = \frac{1}{2}$ where x is an acute angle, then: $m (\angle x) = \dots$ (Cairo 2013)							
# # #	(a) 90°	(b) 60°	(c) 45°	(d) 30°				
# # 12	If $\sin x = \frac{1}{2}$ where x is an acute angle, then m ( $\angle x$ ) = (Cairo 2013)							
<b>*</b>	(a) 90°	(b) 60°	(c) 45°	(d) 30°				
<b>8</b> 13	If $2 \sin x = \tan x$	$60^{\circ}$ where $X$ is an according to $10^{\circ}$	cute angle, then m ( $\angle X$ )	= (Souhag 2011)				
# # #	(a) 30°	(b) 45°	(c) 60°	(d) 40°				
14	If $\tan 3 x = \sqrt{3}$ where 3 x is an acute angle, then $m (\angle x) = \dots$ (Ismailia 2015)							
# #	(a) 20°	(b) 30°	(c) 45°	(d) 60°				
# # 15	If $\sin 2x = \frac{\sqrt{3}}{2}$	then $X = \cdots $	where 2 X is an acute an	igle) (Giza 2011)				
# # #	(a) 20°	(b) 30°	(c) 45°	(d) 60°				
# # 16	If $\cos(x + 10^\circ) = \frac{1}{2}$ where $(x + 10^\circ)$ is an acute angle, then $x = \cdots$ (El-Fayoum 2011)							
# **	(a) 30°	(b) 40°	(c) 50°	(d) 70°				
# # 17	If $\sin (x + 5^{\circ}) = \frac{1}{2}$ where $(x + 5^{\circ})$ is the measure of an acute angle							
## ##	, then tan $(x + 20^\circ)$ عن يعبد (El-Dakahlia 2011)							
<b>*</b>	(a) $\frac{\sqrt{2}}{2}$		7					
# # **	(a) <del>'</del> 2	(b) $\frac{1}{2}$	(c) $\frac{\sqrt{3}}{2}$	(d) 1				
18	If $X$ and $y$ are complementary angles where $X : y = 1 : 2$ , then $\sin X + \cos y = \dots$							
<b>*</b>	$(a)\frac{1}{2}$	$(b)\frac{1}{4}$	(c) $\frac{\sqrt{3}}{2}$	(d) 1				
<b>*</b>	0		7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	(El-Beheira 2015)				
## ## ##								
## ## ##								
<b>**</b>								
<b>*</b>			ا <u>۵</u> ۵	تطبيق مذكرات جاهزة للطباعة				
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				موقع مذكرات جاهزة للطباعة  - 2day.com				



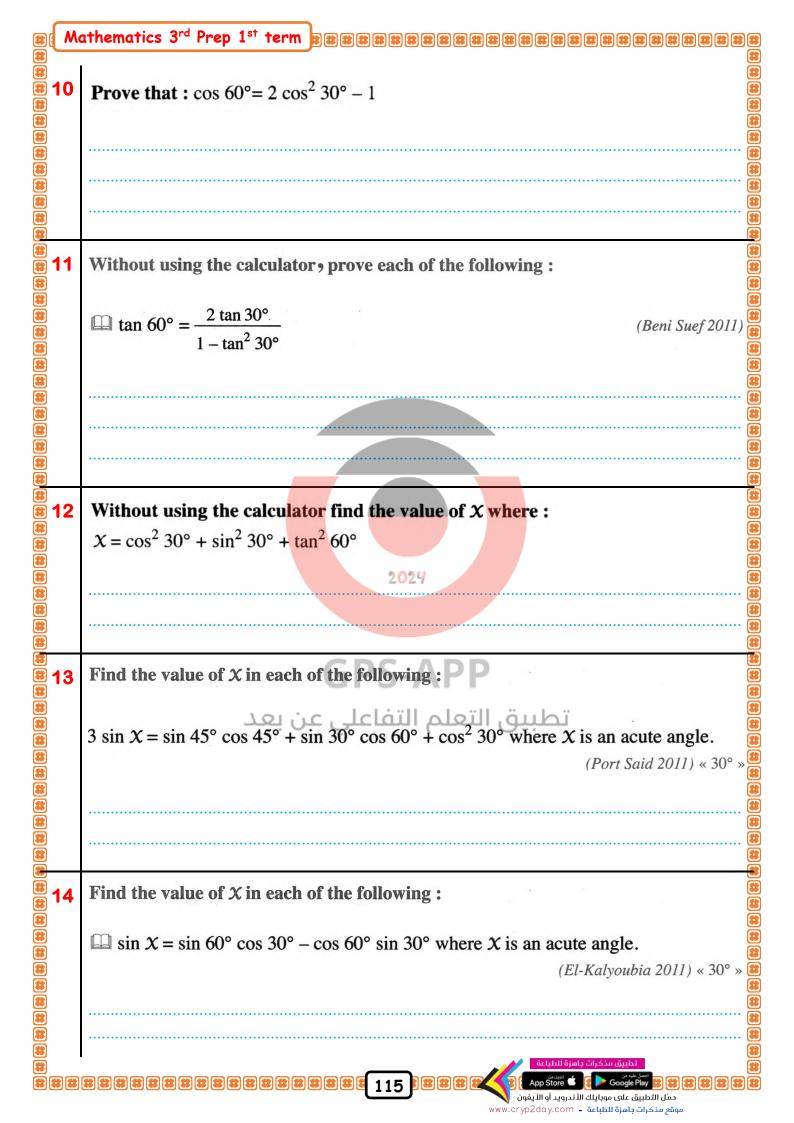
Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term | 1 st 8 Find the value of: A (Where A is an acute angle) which satisfies  $2 \sin A = \tan^2 60^\circ - 2 \tan 45^\circ$ Without using the calculator . **Prove that :**  $\cos 60^{\circ} + 2 \sin^2 45^{\circ} = \sin 30^{\circ} + 3 \tan^2 30^{\circ}$ Choose the correct answer: tan 45° = .....  $(a)\sqrt{3}$ (b)  $\frac{1}{2}$ (c) 1 tan 75° = ..... (El-Ismailia 2011) **88** (b)  $\frac{\sin 75^{\circ}}{\cos 75^{\circ}}$ (a)  $\frac{\cos 75^\circ}{\sin 75^\circ}$ (d) 3 sin 25° cos 25° (c) 3 tan 25° The value of :  $\sin^2 30^\circ + \cos^2 30^\circ =$ (c)  $\frac{1}{2}$  (c)  $\frac{1}{2}$  (c) التعلم التفاعل  $\frac{4}{3}$ (d) 1 (a) zero  $\sin^2 60^\circ + \cos^2 30^\circ - \tan 45^\circ = \cdots$ (b)  $\frac{1}{2}$ (a) zero (c) 2 (d) 3  $\sin^2 60^\circ - \cos^2 60^\circ = \cdots$ (b)  $\frac{1}{4}$ (a) zero (d) 1  $\sin 60^{\circ} = \cdots$ (c)  $\frac{1}{2}$ (a) 1



Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term Rep If sin 2  $x = \frac{\sqrt{3}}{2}$ , then :  $x = \dots$  (where 2 x is an acute angle) (Giza 2011 (a) 20° (b) 30°  $(c) 45^{\circ}$ (d) 60° If:  $\sin (X + 5^\circ) = \frac{1}{2}$ , where  $(X + 5^\circ)$  is an acute angle, then:  $X = \cdots$ (c) 25(d) 30 (b) 10 If  $\sin (x + 5^\circ) = \frac{1}{2}$  where  $(x + 5^\circ)$  is the measure of an acute angle **20** • then :  $\tan (x + 20^{\circ}) = \dots$ (El-Dakahlia 2011 (a)  $\frac{\sqrt{2}}{2}$ (c)  $\frac{\sqrt{3}}{2}$ (b)  $\frac{1}{2}$ (d) 1 If:  $\sin (y + 7^{\circ}) = 0.5$ , then  $y = \dots \circ$ (c) 53 (a) 23 (b) 30 (d) 7 If:  $\sin x = 2 \cos 60^{\circ} \sin 30^{\circ}$  where x is acute angle, then m ( $\angle x$ ) = ......° (c)45(a) 30 (b) 60 (d)75**23** If:  $\cos 2 x = \frac{1}{2}$  where x is an acute angle, then m ( $\angle x$ ) = ..... <sup>2024</sup> (c) 45° (a) 15° (b) 30° (d) 60° ) If  $\cos 3 x = \frac{1}{2}$  where (3 x) is an acute angle, then:  $x = \dots$ (a) 5(b) 10 (d) 20 If:  $\cos(x+5) = \frac{1}{2}$  where (x+5) is an acute angle, then  $x = \dots \circ$ (a) 10 (c) 25 (b) 55 (d) 30 **26** If  $\cos (X + 10^\circ) = \frac{1}{2}$  where  $(X + 10^\circ)$  is an acute angle, then:  $X = \dots$ (El-Fayoum 2011 (a) 30° (b) 40°  $(c) 50^{\circ}$ If:  $\cos(x + 20^\circ) = \frac{1}{2}$  where x is an acute angle, then: m ( $\angle x$ ) equals ..... (a) 10 (b) 25(d) 60(c) 4028 If:  $\cos \frac{x}{2} = \frac{\sqrt{3}}{2}$ , then  $x = \dots$ (a) 30 (b) 45 (c) 60 (d) 90



	Mathematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term passassassassassassassassassassassassass				
	4	Without using calculator • find the numerical value of the expression :  cos 60° sin 30° – sin 60° cos 30°			
	•	<b>Prove that :</b> $\sin 45^{\circ} \cos 45^{\circ} + \sin 30^{\circ} \cos 60^{\circ} = \cos^2 30^{\circ}$			
	5	## Prove that: \$\text{sin 45} \cos 45 \tau \text{sin 50} \cos 60 \text{ = cos 50}			
	6	Without using a calculator, prove that:			
	•	$\sin 30^{\circ} \cos 60^{\circ} + \cos^2 30^{\circ} + 2 \tan 45^{\circ} = 6 \sin^2 45^{\circ}$			
	7	Without using calculator, prove that: $\sin^2 60^\circ = 5 \sin^2 30^\circ - \sin^2 45^\circ$			
		GPS-APP تطبيق التعلم التفاعلي عن بعد			
	8	) Without using calculator ، prove that :			
	0	$\frac{1}{2}\sin^2 45^\circ \tan^2 60^\circ - 3\sin^2 60^\circ \tan^2 30^\circ = 0$			
	6	<b>Prove that:</b> $\cos 60^{\circ} = \cos^2 30^{\circ} - \sin^2 30^{\circ}$			
<b>**</b>	<b>B 48</b>	تطبیق مذکرات باهزة للطباعة ﴿ App Store ﴿ وَ الطباعة ﴿ App Store ﴿ وَ الطباعة ﴿ App Store ﴿ وَ الطباعة ﴿ App Store ﴿ وَ الطبيق على موبايلك الأندرويد أو الأيفون ﴿ www.cryp2day.com - موقع مذکرات باهزة للطباعة - www.cryp2day.com			



Mathematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term ####################################			
15	Find the value of E where: $2 \cos E = 4 \sin^2 60^\circ - 2 \tan 45^\circ$ where: E is an acute angle.		
16	If : $\cos x = \tan 45^{\circ} \cos^2 30^{\circ} - \sin^2 30^{\circ}$ Find the value of : $x$ where $0 < x < 90^{\circ}$		
17	Find the value of X that satisfies that: $\cos X = \frac{\sin 60^{\circ} \sin 30^{\circ}}{\tan 45^{\circ} \sin^2 45^{\circ}}$		
	where $X$ is the measure of an acute angle.		
18	Prove that : $\sin 60^\circ = 2 \sin 30^\circ \cos 30^\circ$		
	2024		
	GPS-APP  Find the value of Vin each of the following		
19	Find the value of $X$ in each of the following: $\tan X = 4 \sin 30^{\circ} \cos 60^{\circ}$ where $X$ is an acute angle.  (Assiut 2011) « 45° »		
20	If: $\cos N = \frac{(\sin 60^\circ)^2 - \sin 30^\circ}{3(\cos 45^\circ)^2 + 1}$ , where $0 < N < 90^\circ$		
	Find: $m (\angle N)$ in degrees.		
     <b> </b>   <b> \$</b>	تطبيق مذكرات وامزة للطباعة ( App Store ( ) ( ) ( ) ( ) ( ) ( ) ( ) ( ) ( ) (		

## **Sheet (12)**

### **Distance Between Two Points**

*i.e.* The distance between the two points M and N equals  $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$  and we know that :

$$(X_2 - X_1)^2 = (X_1 - X_2)^2$$
, and similarly:  $(y_2 - y_1)^2 = (y_1 - y_2)^2$ , therefore:

The distance between the two points M and N equals also  $\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$ 

Generally: The distance between two points =

 $\sqrt{\text{square of the difference between }x-\text{coordinates} + \text{square of the difference between }y-\text{coordinates}}$ 

### For example:

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# #

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• The distance between the two points M (3,6) and N (-1,4) is:

$$MN = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = \sqrt{(-1 - 3)^2 + (4 - 6)^2} = \sqrt{(-4)^2 + (-2)^2}$$

$$=\sqrt{16+4} = \sqrt{20} = 2\sqrt{5}$$
 length unit.

8

**33** 

#

## Remark 1

To prove that three given points are collinear (*i.e.* they lie on one straight line) we can find the distance between each two of these points, then prove that the greatest distance equals the sum of the two other distances.

## Remark 2

- To prove that the points: A, B and C are vertices of a triangle, we can find AB, BC and AC, then prove that the sum of the smaller two lengths is greater than the third length.
- To determine the type of the triangle ABC according to its angle measures (where  $\overline{AC}$  is the longest side of the triangle ABC)

We compare between  $(AC)^2$  and  $(AB)^2 + (BC)^2$  as the following:

- 1 If  $(AC)^2 > (AB)^2 + (BC)^2$
- , then the triangle is obtuse-angled at B
- 2 If  $(AC)^2 = (AB)^2 + (BC)^2$
- , then the triangle is right-angled at B
- 3 If  $(AC)^2 < (AB)^2 + (BC)^2$
- , then the triangle is acute-angled.

## Remark 3

If ABCD is a quadrilateral:

- 1 To prove that ABCD is a parallelogram, we prove that : AB = CD, BC = AD
- 2 To prove that ABCD is a rhombus, we prove that : AB = BC = CD = DA

Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term 3 To prove that ABCD is a rectangle, we prove that : AB = CD, BC = AD, AC = BD4 To prove that ABCD is a square, we prove that : AB = BC = CD = DA, AC = BD8 Remark 4 • To prove that: Three points as A, B and C lie on a same circle of centre M we prove that : MA = MB = MC8 • If A  $\subseteq$  the circle M, then the radius length of this circle (r) = MA Remember that : - Circumference of the circle =  $2 \pi r$ - Area of the circle =  $\pi r^2$ Choose the correct answer: The length of the line segment drawn from the point (0,0) to the point (-4,3)8 equals ..... units of length. 8 (c) \ 7 8 (a) 3 (d)5(b) 4The distance between the two points (5,0) and  $(0,-12) = \dots$  length units. 2024 **33** (a) 7(d) 10 (b) 13 (c) 17 **33 33** If: C(-6,0), D(0,8), then  $CD = \dots$  length unit. **33** (b) 10 GPS-A(c) 5 (a) 14 (d) 2**88** The distance between the point (2, -3) and the x-axis equals ..... units length **33** (a) 2 (c) -3(b) 3(d) -2\* **3** The distance between the point (2, -5) and the  $\mathcal{X}$ -axis = ..... length unit. (a) 5(b) 2 (c) - 5(d) - 3**33** The distance between the point (3, -5) and X-axis is ..... length units. (Cairo 2012) **33**  $(d) \sqrt{34}$ (a) 3 (b) - 5(c) 5The distance between the point (4, -3) and the  $\mathcal{X}$ -axis = .....length unit. 8 (a) -3(b) 3(c) 4 (d) 5118 حمَل التطبيق على موبايلك الأندرويد أو الأيفون وقع مذكرات جاهزة للطباعة - www.cryp2day.com

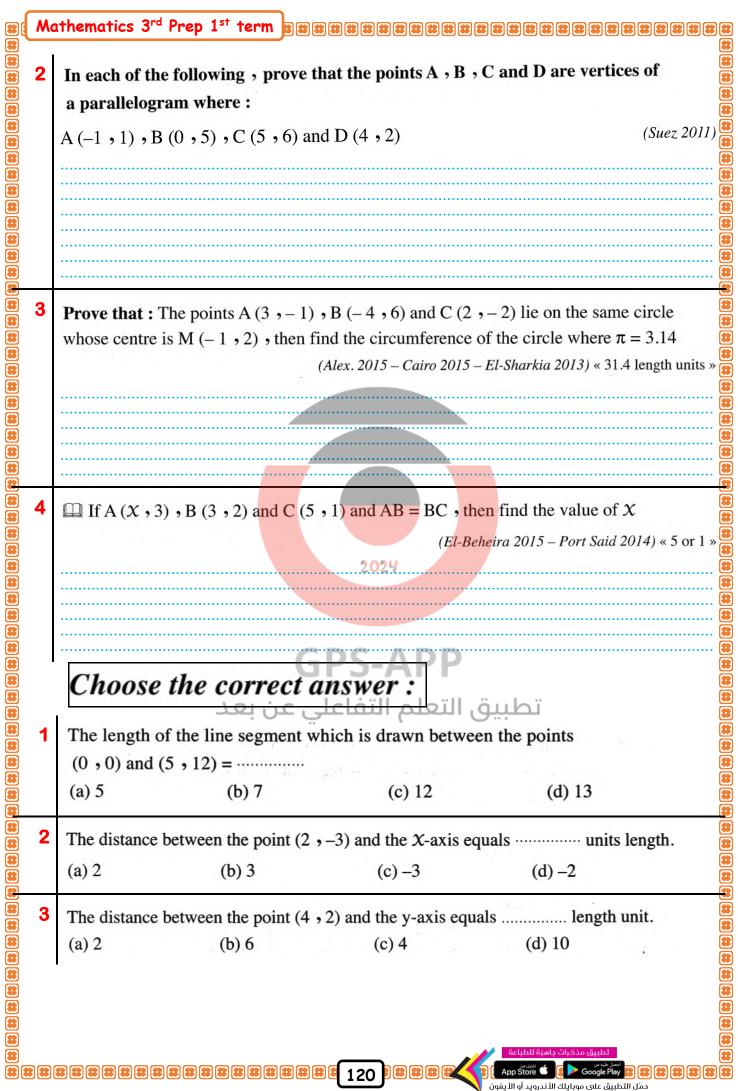
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Mathematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>333333333333333333333333333333333333</b>				
8	The distance between the point (4, 2) and the y-axis equals length unit.  (a) 2 (b) 6 (c) 4 (d) 10			
	Distance between point $(2, -3)$ and y-axis = length units. (a) 2 (b) -3 (c) $\sqrt{13}$ (d) $\sqrt{5}$			
10	The distance between the point (3, 4) and the origin point equals			
11	The distance between the point $(\sqrt{5}, -2)$ and origin point is length unit.  (a) 2 (b) -2 (c) 3 (d) 8			
12	A circle its centre is the origin and its radius length is 2 length units, which of the following points belongs to the circle?  (a) $(1,2)$ (b) $(-2,1)$ (c) $(\sqrt{3},1)$ (d) $(\sqrt{2},1)$			
13	In the Cartesian coordinates plane, the point that is at a distance 2 length units from the origin may be			
14	If the origin point is a centre of a circle of radius 3 length units, then the point which belonges to the circle is:			
15 	The radius length of the circle of center (7,4) passing through the point (3,1) equals			
1	is a right-angled triangle at B , then calculate its area.  (Beni Suef 2013 – El-Monofia 2014) « 120 square unit » و المعلق الم			



Mathematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term				
4	* The distance between the point (10,0) and the origin point equalslength unit.  (a) 3 (b) 6 (c) 8 (d) 10			
	A circle its centre is the origin and its radius length is 2 length units, which of the following points belongs to the circle?  (a) $(1,2)$ (b) $(-2,1)$ (c) $(\sqrt{3},1)$ (d) $(\sqrt{2},1)$			
6	The length of the line segment which is drawn between the two points $(0,0)$ and $(6,8) = \cdots$ length unit.  (a) 6 (b) 8 (c) 10 (d) 14			
7	The distance between the point $(\sqrt{5}, -2)$ and origin point is length unit.  (a) 2 (b) -2 (c) 3 (d) 8			
	If: $C(-6,0)$ , $D(0,8)$ , then $CD =$ length unit. (a) 14 (b) 10 (c) 5 (d) 2			
9	The distance between the point (a, 0) and the point (0, -1) equals $\sqrt{5}$ , then a =			
	If the origin point is a centre of a circle of radius 3 length units, then the point which belonges to the circle is:			
	The length of the line segment that drawn between the two points $(3, 2)$ and $(-1, 5) = \cdots$ length unit.  (a) 15 (b) 3 (c) 5 (d) 10			
12	The distance between the point (3, 4) and the origin point equals			
13	The distance between the two points $(a, 0)$ , $(0, 1)$ is one length unit, then $a = \dots$ $(a) - 1$ $(b) 0$ $(c) 1$ $(d) \pm 1$			
13	The radius length of the circle of center (7,4) passing through the point (3,1) equals unit length.  (a) 7 (b) 6 (c) 5 (d) 4			
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M	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>233333333333333333333333333333</b>
	Essay problems:
ı	Essay provients.
1	$\square$ Prove that the triangle with vertices of points : A (5, -5), B (-1, 7) and C (15, 15)
	is a right-angled triangle at B, then calculate its area.
	(Beni Suef 2013 – El-Monofia 2014) « 120 square unit
2	If A $(-1, -1)$ , B $(2, 3)$ and C $(6, 0)$
	<b>Prove that :</b> $\triangle$ ABC is a right-angled triangle, then find its area.
	(Alexandria – Beni Suef 2011) « 12.5 square units
	(Mexunul a Bent Buej 2011) will be equal business
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	2021
	GPS-APP
3	In each of the following, prove that the points A, B, C and D are vertices of
•	In each of the following, prove that the points A, B, C and D are vertices of
	a parallelogram where:
	A(-1, 1), B(0, 5), C(5, 6)  and  D(4, 2) (Suez 201)
	تطبيق مذكرات جاهزة للطباعة

	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term	) <b>(</b>
9 8 <b>4</b>	In each of the following, prove that the points A, B, C and D are vertices of	4
	a parallelogram where:	
	A $(-2, 4)$ , B $(5, -3)$ , C $(7, 1)$ and D $(0, 8)$ (Souhag 2008)	
5	<b>Prove that :</b> The points A $(3, -1)$ , B $(-4, 6)$ and C $(2, -2)$ lie on the same circle	
	whose centre is M $(-1, 2)$ , then find the circumference of the circle where $\pi = 3.14$	8
	(Alex. 2015 – Cairo 20 <mark>15 – El</mark> -Sharkia 2013) « 31.4 length units »	
	2024	
	GPS_APP	9
	تطبيق التعلم التفاعلي عن بعد	
6	If A (2, $x$ ) and B (3, -1), AB = $\sqrt{17}$ length units, then find: $x$	
	(El-Dakahlia 2013) « 3 or – 5 »	
	(Li Danamu 2013) «3 01 3 »	
3		
	تطبیق مذکرات دِاهِرَة الطباعة و الطباعة العلامة العالمة العال	
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Ma	thematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>3888888888888888888888888888888888888</b>	3
_		
7	☐ Find the value of a in each of the following cases:	
	If the distance between the two points $(a,7), (-2,3)$ equals 5 length unit.	
	(Luxor 2013) « 1 or –	5
		•
		• •
		• •
		• •
		••
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-		_
8	$\square$ If A ( $\chi$ , 3), B (3, 2) and C (5, 1) and AB = BC, then find the value of $\chi$	
	(El <mark>-Behei</mark> ra 2015 – Port Said 2014) « 5 on	
	(Di Benerita Bollo I oli bana Boll) in oli	
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<b>33</b>	\$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$	<b>3</b> ]

# Midpoint Of A Line Segment

If the First point: A (  $X_1$  ,  $y_1$  ),

Second point: B (  $\mathbf{X_2}$  ,  $\mathbf{y_2}$  )

Then the Midpoint point: M (  $\mathbf{m}_{\mathbf{x}}$  ,  $\mathbf{m}_{\mathbf{y}}$  ) then

$$M \ ( \ m_x \ , \ m_y \ ) = (\frac{X_1 + X_2}{2} \ , \ \frac{y_1 + y_2}{2} \ ) \ ,$$

$$X_1 = m_x X 2 - X_2$$

$$y_1 = m_y X 2 - y_2$$

## For Example : -

• If A (1,5), B (3,1) and M is the midpoint of  $\overline{AB}$ , then:

$$M = \left(\frac{1+3}{2}, \frac{5+1}{2}\right) = (2,3)$$

• If X(3, -2), Y(-1, -4) and M is the midpoint of  $\overline{XY}$ , then:

$$M = \left(\frac{3 + (-1)}{2}, \frac{-2 + (-4)}{2}\right) = (1, -3)$$

## Remark: -

If  $\overline{AB}$  is a diameter in a circle of centre M, then M is the midpoint of  $\overline{AB}$ 

## Choose the correct answer:

- - (a) (-2, 1)

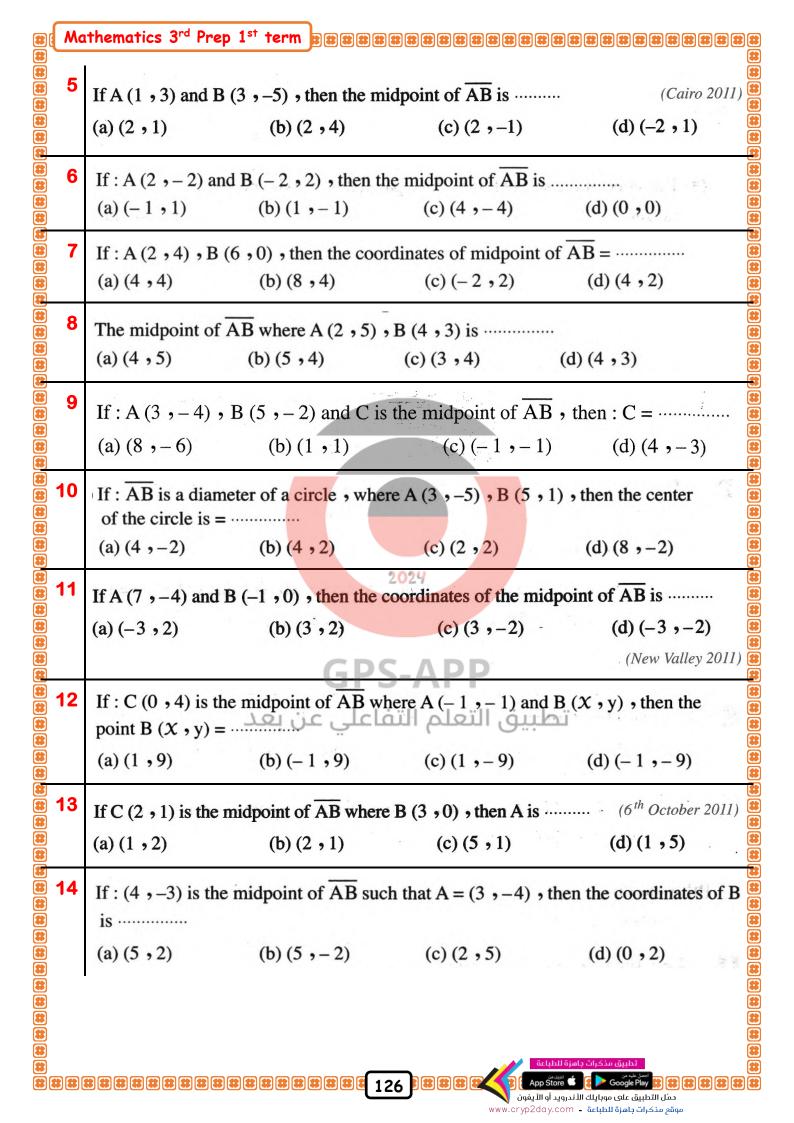
**3** 

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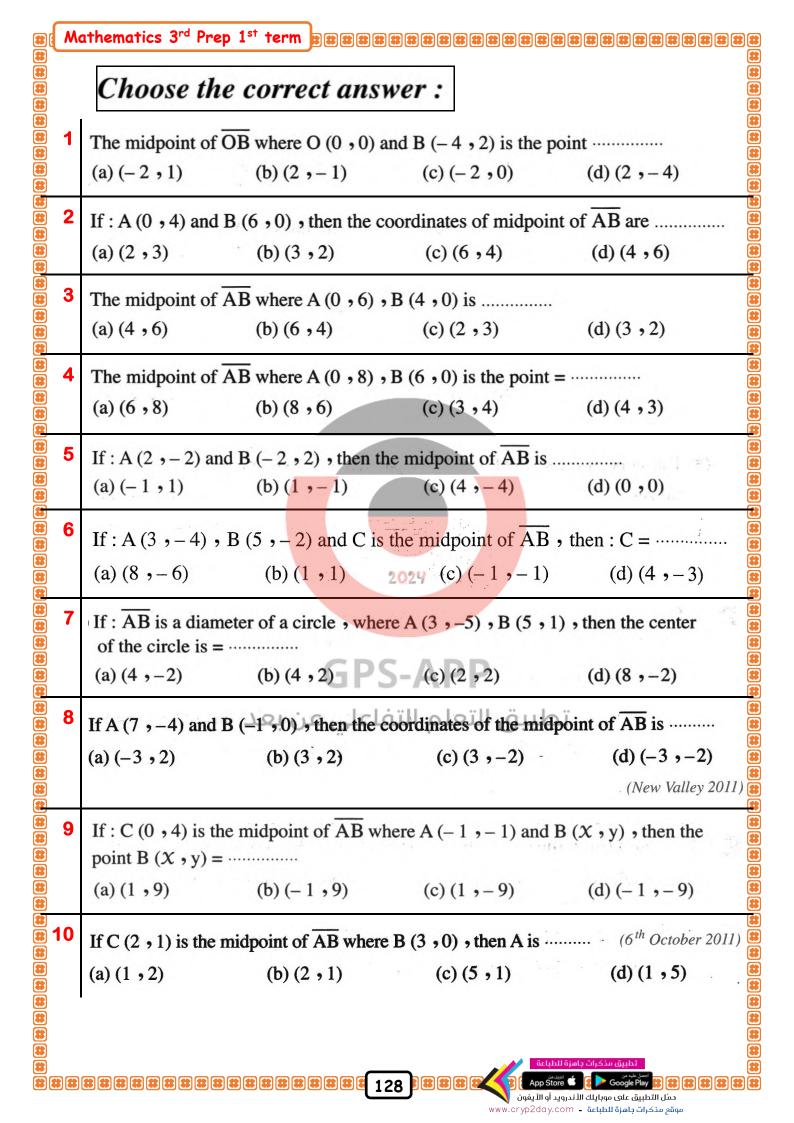
- (b) (2, -1)
- (c)(-2,0)
- (d) (2, -4)
- If: A (0, 4) and B (6, 0), then the coordinates of midpoint of  $\overline{AB}$  are .....

2024

- (a) (2,3)
- (b) (3, 2)
- (c)(6,4)
- (d)(4,6)
- The midpoint of  $\overline{AB}$  where A (0, 6), B (4, 0) is .....
  - (a) (4, 6)
- (b) (6,4)
- (c)(2,3)
- (d)(3,2)
- The midpoint of  $\overline{AB}$  where A (0, 8), B (6, 0) is the point = .....
  - (a) (6, 8)
- (b)(8,6)
- (c)(3,4)
- (d)(4,3)



Ma	thematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term
	Essay problems:
	Essay provients.
1	If C (4,6) is the midpoint of $\overline{AB}$ where A ( $\chi$ , 3) and B (6, y), then find the value of
	each of: X and y (Cairo 2015) « 2 , 9 »
2	$\square$ If C is the midpoint of $\overline{AB}$ , then find X, y in each of the following cases:
	A(x,3), $B(6,y)$ , $C(4,6)$ (Luxor 2013) «2,9
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3	AD in a diameter ' ' 1 M 'CD (0 11) 124 (5 5) 70 7
9	AB is a diameter in a circle M, if B (8, 11) and M (5, 7) Find:  (1) The coordinates of A
	(2) The perimeter of the circle. where $(\pi = 3.14)$ (Assiut 2014) « A (2, 3), 31.4 length unit
<b>.</b>	تطبیق مذکرات باهزة للطباعة
	\$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$



M	athematics 3 <sup>rd</sup> Pr	rep 1 <sup>st</sup> term <b>B 33 33</b>		
11	If: $(4, -3)$ is th	e midpoint of $\overline{AB}$ suc	h that $A = (3, -4)$ ,	then the coordinates of B
	is			
	(a) $(5, 2)$	(b) $(5, -2)$	(c) $(2,5)$	(d) (0 , 2)
12	* If the point of	the origin O (0,0) is	s the midpoint of the	line segment AB where
	A(5,-2), th	en the coordinates of	the point B is	
	(a) $(-5, 2)$	(b) $(5, -2)$	(c) $(-2,5)$	(d) (0,5)
F	say probl	oms.		
LS	<u>say provi</u>	ems.		
1	If $C^{(6)} \cdot -4$ is the	he midpoint of $\overline{AB}$ wh	ere A $(5, -3)$	
	Find the coordin	ates of the point B	(Beni Suef 2	2014 – El-Beheira 2013) « (7 • – :
			2024	
			2021	
		GP	S-APP	
			1:::11 1 ::11 "	1 "
2	Find the value of	each of a and b that s	atisfies that $(2 a - 3)$	(a - b) is the midpoint of the
		ose terminals $(7, -1)$		(EL-Fayoum 2012) « 4 ,
		••••••	••••••	
	I	_		تطبيق مذكرات باهزة للطباعة



# **Sheet (14)**

## The Slope of the Straight Line

#### **Prelude**

You studied before the slope of the straight line given two points on it.

If A and B are two points in the coordinates plane where A  $(X_1, y_1)$  and B  $(X_2, y_2)$ , then:

The slope of the straight line 
$$\overrightarrow{AB} = \frac{y_2 - y_1}{x_2 - x_1}$$
 where  $x_1 \neq x_2$ 

## The positive measure and the negative measure of an angle

#### In the opposite figure:

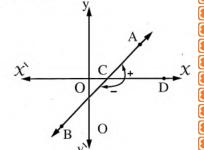
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8

8

If AB intersects the X-axis at the point C, then AB makes two angles with the positive direction of the X-axis.



#### The slope of the straight line

#### Definition

The slope of the straight line is the tangent of the positive angle which this straight line makes with the positive direction of the X-axis.

1.e. The slope of the straight line =  $\tan \theta$  where  $\theta$  is the measure of the positive angle which the straight line makes with the positive direction of the x-axis.

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Notice that

The straight line passes through the two points (2,0) and (7,5), then:

the slope of the straight line 
$$L = \frac{y_2 - y_1}{x_2 - x_1} = \frac{5 - 0}{7 - 2} = \frac{5}{5} = 1$$

Mathematics 3<sup>rd</sup> Prep 1<sup>st</sup> term Rep

#### Remark

8

The angle which the straight line L makes with the positive direction of the x-axis takes one of the following cases:

1 Acute angle	2 Obtuse angle	3 Zero angle	4 Right angle	
x' Ol x	L Y B X	x x	x L x	
The slope is positive	The slope is negative	The slope is zero	The slope is undefined	

## The relation between the two slopes of the two parallel straight lines

Also, we can deduce the opposite:

If 
$$[m_1 = m_2]$$
, then  $[L_1 // L_2]$ 

i.e. If the two straight lines have equal slopes, then the two straight lines are parallel.

### The relation between the slopes of the two perpendicular (orthogonal) straight lines

If  $L_1$  and  $L_2$  are two straight lines of slopes  $m_1$  and  $m_2$  respectively and  $L_1 \perp L_2$ , then  $m_1 \times m_2 = -1$ , unless one of them is parallel to one of the coordinate axes.

*i.e.* The product of the slopes of the perpendicular straight lines = -1تطبيق التعلم التفاعلي عن بعد

and vice versa:

Remark

If  $L_1 \perp L_2$ , the slope of  $L_1$  is  $m_1$  and the slope of  $L_2$  is  $m_2$ , then  $m_2 = \frac{-1}{m_1}$ ,  $m_1 = \frac{-1}{m_2}$ 

#### For example:

- If the slope of the straight line L is 2, then the slope of the perpendicular to it =  $-\frac{1}{2}$
- If the slope of the straight line L is  $-\frac{2}{3}$ , then the slope of the perpendicular to it =  $\frac{3}{2}$

Mo	thematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term
3 	Remarks to solve the problems on quadrilateral
_	To prove that a quadrilateral is a trapezium, we prove that:  Two opposite sides are parallel and the other two sides are not parallel.
2	To prove that a quadrilateral is a parallelogram, we prove only one of the following properties:
	1 Each two opposite sides are parallel.
	2 Each two opposite sides are equal in length.
	3 Two opposite sides are parallel and equal in length.
	4 The two diagonals bisect each other.
	To prove that a quadrilateral is a rectangle, rhombus or square, we prove at first that the quadrilateral is a parallelogram, then:
	To prove that the parallelogram is a rectangle, we prove only one of the following two properties:
	1 Two adjacent sides are perpendicular. 2 The two diagonals are equal in length.
3	prove that the parallelogram is a rhombus, we prove only one of the following
tw	o properties :
	Two adjacent sides are equal in length. 2 The two diagonals are perpendicular.
	prove that the parallelogram is a square, we prove only one of the following properties :
	Two adjacent sides are perpendicular and equal in length.
Same Parties	Two adjacent sides are perpendicular and its diagonals are perpendicular.
	Two diagonals are equal in length and perpendicular.
4	Two adjacent sides are equal in length and its two diagonals are equal in length.
Ch	coose the correct answer:
1	تطبيق التعلم التفاعلي عن بعد The slope of straight line which parallel to the X-axis is
	(a) 1 (b) $-1$ (c) 0 (d) unknown
2	The slope of a straight line which makes an angle of measure 45° with the positive
	direction of $X$ -axis =
	(a) 1 (b) $\frac{1}{\sqrt{2}}$ (c) $\sqrt{3}$ (d) otherwise.
3	The slope of straight line which is parallel to the straight line passing through the two points $(2,3), (-2,1)$ equals
	(a) $\frac{1}{4}$ (b) $\frac{1}{2}$ (c) $-4$ (d) $-2$
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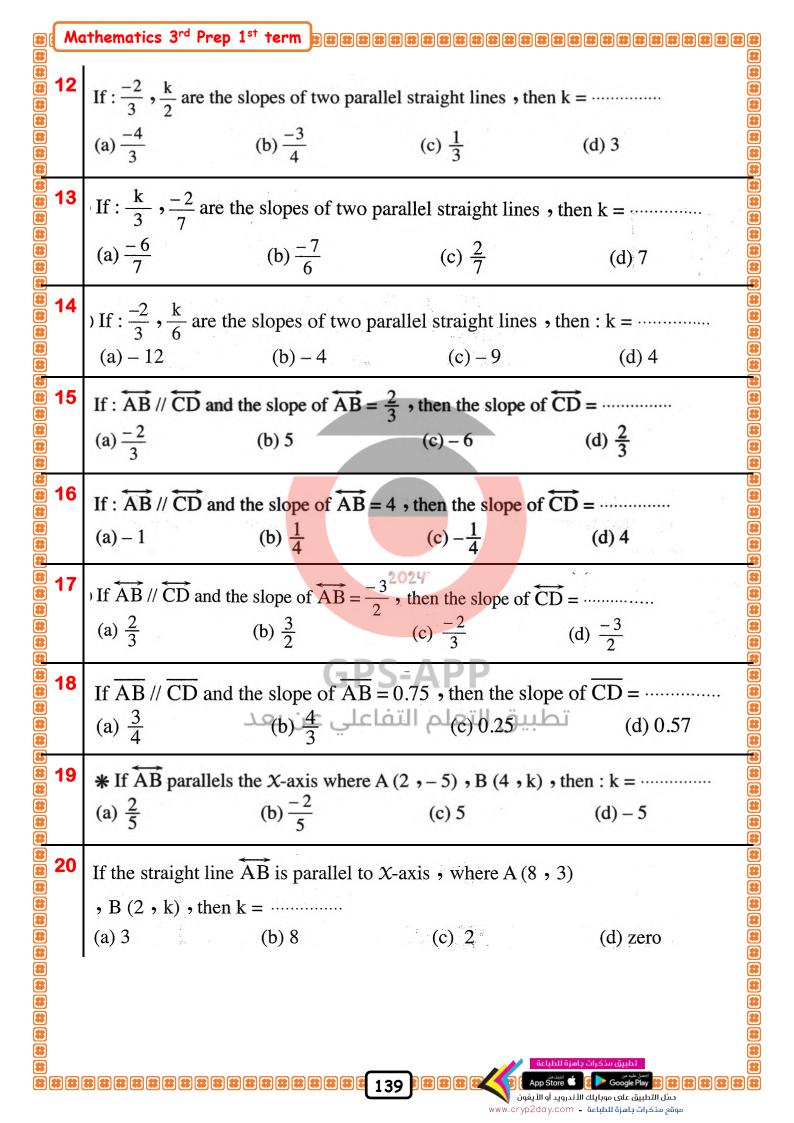
Mathematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term ************************************					
4 4 ***	If the slope of a straight line more than zero, then the type of the positive angle which it makes with the positive direction of X-axis is				
5 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	If : $m_1$ is the slope of the line $L_1$ and $m_2$ is the slope of the line $L_2$ and $L_1$ // $L_2$ , then				
**************************************	If $m_1$ and $m_2$ are two slopes of two straight lines $L_1$ and $L_2$ respectively and $m_1 - m_2 = 0$ , then				
* 7 * 8 * 8 * 8	If $m_1$ and $m_2$ are two slopes of two perpendicular straight lines, then				
** 8 ** **	If: $m_1$ , $m_2$ are the slopes of two perpendicular straight lines, then $m_1 \times m_2 = \cdots$ (a) 1 (b) $\frac{1}{2}$ 2024(c) -1 (d) -2				
<b>3 9 3 3 3 3 3 3 3 3 3 3</b>	The two straight lines whose slopes are $\frac{3}{5}$ and $\frac{-5}{3}$ are				
# 10 # 10	Two parallel straight lines of slopes $m_1$ and $m_2$ If: $m_1 = \frac{-1}{3}$ , then $m_2 = \cdots$ (a) $\frac{1}{3}$ (b) 3 (c) $-3$ (d) $-\frac{1}{3}$				
# 11 # # # # # # # # # # # # # # # # # #	If: $m_1$ , $m_2$ are the slopes of two perpendicular straight lines, $m_1 = 0.75$ , then $m_2 = \cdots$ (a) $-\frac{3}{4}$ (b) $\frac{4}{3}$ (c) $-\frac{4}{3}$ (d) $\frac{3}{4}$				
# 12 # 12 # # # # # # # # # # # # # # # # # # #	If: $\frac{-2}{3}$ , $\frac{k}{2}$ are the slopes of two parallel straight lines, then $k = \dots$ (a) $\frac{-4}{3}$ (b) $\frac{-3}{4}$ (c) $\frac{1}{3}$ (d) 3				
# # # ################################	قطبيق مذكرات باهرة للطباعة - App Store في القطباعة والمساعة والمس				

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# 13 # 13	If: $\frac{k}{3}$ , $\frac{-2}{7}$	are the slopes of two	parallel straight lines	• then k =	
***	(a) $\frac{-6}{7}$	(b) $\frac{-7}{6}$	(c) $\frac{2}{7}$	(d) 7	
# 14 # 14	) If: $\frac{-2}{3}$ , $\frac{k}{6}$ and	re the slopes of two p	parallel straight lines	• then: k =	
** ** **	(a) - 12	(b) - 4	(c) – 9	(d) 4	**************************************
# 15	If: $\overrightarrow{AB} / / \overrightarrow{CD}$	and the slope of $\overrightarrow{AB}$	$=\frac{2}{3}$ , then the slope of	f CD =	<b>3</b>
# # # #	(a) $\frac{-2}{3}$	(b) 5	(c) – 6	(d) $\frac{2}{3}$	
# 16	If: $\overrightarrow{AB}$ // $\overrightarrow{CD}$	and the slope of $\overrightarrow{AB}$	= 4, then the slope o	f CD =	
# # #	(a) – 1	(b) $\frac{1}{4}$	$(c) - \frac{1}{4}$	(d) 4	<b>3</b>
# 17 # 17	^		$\frac{-3}{2}$ , then the slope of $\overline{C}$		
# #	(a) $\frac{2}{3}$	(b) $\frac{3}{2}$	(c) $\frac{-2}{3}$	(d) $\frac{-3}{2}$	
# # 18	If $\overline{AB}$ // $\overline{CD}$	and the slope of AE	B = 0.75, then the slo	ope of $\overline{\rm CD}$ =	8
# # #	(a) $\frac{3}{4}$	(b) $\frac{4}{3}$	(c) 0.25	(d) 0.57	8
# 19	* If $\overrightarrow{AB}$ paral	llels the $\chi$ -axis where	A(2,-5), B(4,k)	• then : $k = \cdots$	
***	(a) $\frac{2}{5}$	علي ع <u>ق 5</u> بعد	بيق الت <mark>غ</mark> ل <sup>م</sup> التفا	(d) – 5	
# 20	If the straight	line $\overrightarrow{AB}$ is parallel to	x-axis, where A (8	, 3)	8
**	, B(2, k), t	hen k =			<b>8</b>
# # #	(a) 3	(b) 8	(c) 2	(d) zero	(E)
# 21 #	If the straight then k = ······	line $\overrightarrow{AB}$ is parallel to	o the $X$ -axis where A	(5, -3) and B $(4, k)$ ,	
***	(a) - 3	(b) 5	(c) 4	(d) 1	
# 22	If: $\overrightarrow{AB}$ ⊥ $\overrightarrow{CD}$	and the slope of $\overrightarrow{AB}$	$=\frac{1}{2}$ , then the slope	of CD =	
**	(a) $\frac{1}{2}$	(b) $-\frac{1}{2}$	(c) 2	(d)-2	8
22]			135		_[

B (Mc	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>Bassassassassassassassassas</b>
23	If: $\overrightarrow{AB} \perp \overrightarrow{CD}$ and the slope of $\overrightarrow{AB} = -\frac{2}{3}$ , then the slope of $\overrightarrow{CD} = \cdots$ (a) $\frac{3}{2}$ (b) $\frac{-3}{2}$ (c) $-\frac{2}{3}$ (d) $\frac{2}{3}$
24 28 28 28	If: $\overrightarrow{AB} \perp \overrightarrow{CD}$ and the slope of $\overrightarrow{AB} = \frac{2}{3}$ , then the slope of $\overrightarrow{CD} = \cdots$ (a) $\frac{3}{2}$ (b) $\frac{-3}{2}$ (c) $\frac{2}{3}$ (d) $\frac{4}{9}$
<b>25</b>	* The straight line that makes with the positive direction of the X-axis an angle of measure $45^{\circ}$ , its slope is
26 28 28 28 28 28 28 28 28 28 28 28 28 28	The straight line which passes through the two points $(1, y)$ , $(3, 4)$ its slope is tan 45°, then $y = \cdots$ (a) 1 (b) 2 (c) -1 (d) 4  Essay problems:
	Find the slope of the straight line which is perpendicular to the straight line which passes through the two points A $(2, -3)$ , B $(3, 5)$ $(Matrouh\ 2009) \ll -\frac{1}{8} \gg 2024$
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	تطبيق التعلم التفاعلي عن بعد
	<b>Prove that :</b> The straight line which passes through the two points $(4, 3\sqrt{3})$ and $(5, 2\sqrt{3})$ is perpendicular to the straight line which makes an angle of measure 30° with the positive direction of $X$ -axis. (El-Beheira 2013)
	تَطبِيقَ مَذَكِراتُ دِاهزَةُ للطباعةُ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$

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3	<b>Prove that :</b> The points A $(1, 1)$ , B $(2, 3)$ and C $(0, -1)$ are collinear. (Cairo 2013)
4	The triangle whose vertices are A $(3,-1)$ , B $(x,3)$ and C $(5,3)$ is a right-angled
	triangle at A, find the value of $X$ (Cairo 2011) « –5 »
8	2024
5	Prove that: The points $A(-1,1)$ , $B(0,5)$ , $C(4,2)$ and $D(5,6)$ are the vertices of the parallelogram ABDC (Luxor 2012)
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	تطبيق التعلم التفاعلي عن بعد
	Choose the correct answer:
1	The slope of straight line which parallel to the $X$ -axis is
2	The slope of a straight line which makes an angle of measure 45° with the positive
1 2	direction of $x$ -axis =
	تطبيق مذكرات باهرة للطباعة ( App Store ( ) ( ) ( ) ( ) ( ) ( ) ( ) ( ) ( ) (

# (Mc	Mathematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term ####################################		
3 3 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	The slope of straight line which is parallel to the straight line passing through the two points $(2,3), (-2,1)$ equals		
## 4 ## ## ##	If the slope of a straight line more than zero, then the type of the positive angle which it makes with the positive direction of X-axis is		
\$ 5	If: $m_1$ is the slope of the line $L_1$ and $m_2$ is the slope of the line $L_2$ and $L_1$ // $L_2$ , then		
8	If $m_1$ and $m_2$ are two slopes of two straight lines $L_1$ and $L_2$ respectively and $m_1 - m_2 = 0$ , then		
# 7 # 8 # # # # # # # # # # # # # # # # # #	If $m_1$ and $m_2$ are two slopes of two perpendicular straight lines, then		
** 8 ** **	If: $m_1$ , $m_2$ are the slopes of two perpendicular straight lines, then $m_1 \times m_2 = \cdots$ (a) 1 (b) $\frac{1}{2}$ (c) $-1$ (d) $-2$		
# 9 # 8 # # #	The two straight lines whose slopes are $\frac{3}{5}$ and $\frac{-5}{3}$ are		
# 10 # #	Two parallel straight lines of slopes $m_1$ and $m_2$ If: $m_1 = \frac{-1}{3}$ , then $m_2 = \cdots$ (a) $\frac{1}{3}$ (b) 3 (c) $-3$ (d) $-\frac{1}{3}$		
## 11 #################################	If: $m_1$ , $m_2$ are the slopes of two perpendicular straight lines, $m_1 = 0.75$ , then $m_2 = \cdots$ (a) $-\frac{3}{4}$ (b) $\frac{4}{3}$ (c) $-\frac{4}{3}$ (d) $\frac{3}{4}$		
# # # ## ##	ق مذكرات داهزة للطباعة - Www.cryp2day.com ومؤم مذكرات اهر ق للطباعة - Www.cryp2day.com ومؤم مذكرات اهر ق للطباعة - Www.cryp2day.com ومؤم مذكرات اهر ق للطباعة - www.cryp2day.com		



Mathematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>BSSSSSSSSSSSSSSSSSSSSSSSSSSSSS</b>				
21 21	then $k = \cdots$			A $(5, -3)$ and B $(4, k)$ ,
	(a) - 3	(b) 5	(c) 4	(d) 1
# 22 #	If: $\overrightarrow{AB}$ ⊥ $\overrightarrow{CD}$	and the slope of AI	$\vec{B} = \frac{1}{2}$ , then the slop	e of $\overrightarrow{CD}$ =
	(a) $\frac{1}{2}$	(b) $-\frac{1}{2}$	(c) 2	(d)-2
23	If: $\overrightarrow{AB}$ ⊥ $\overrightarrow{CI}$	and the slope of A	$\overrightarrow{AB} = -\frac{2}{3}$ , then the s	slope of $\overrightarrow{CD} = \cdots$
	(a) $\frac{3}{2}$	(b) $\frac{-3}{2}$	(c) $-\frac{2}{3}$	(d) $\frac{2}{3}$
<b>24</b>	If: $\overrightarrow{AB} \perp \overrightarrow{CD}$	and the slope of A	$\overrightarrow{AB} = \frac{2}{3}$ , then the slo	ope of $\overrightarrow{CD} = \cdots$
	(a) $\frac{3}{2}$	(b) $\frac{-3}{2}$	(c) $\frac{2}{3}$	(d) $\frac{4}{9}$
25 8 8 8 8 8	4			4) perpendicular to the one ion of $X$ -axis, then $a = \cdots$ (d) $-1$ (Monofia 2012)
26 28 28	The straight list tan 45°, the		rough the two points (c) -1	(1,y), (3,4) its slope (d) 4
B 27 B 27		the line segment drav	يق التعلم التفاء	0) to the point (-4,3)
<u></u>	( ) 0			
	(a) 3	(b) 4	(c)√7	(d) 5
28 13 13 13 14				(d) 5 12) = ······ length
28 18 18	The distance b			
28 8 8	The distance bunits. (a) 7	between the two points (b) 13	nts (5,0) and (0,-	12) = ······ length (d) 10
28 BB BB BB BB BB BB BB BB BB BB BB BB	The distance bunits. (a) 7	between the two points (b) 13	nts (5,0) and (0,-	12) = ······ length (d) 10
	The distance bunits. (a) 7  If: C (-6,0) (a) 14	(b) 13 (b) 13 (c) D (0, 8), then C (d) 10	(c) 17 (D =length	12) = ······ length  (d) 10  unit.
28 BB BB BB BB BB BB BB BB BB BB BB BB BB	The distance bunits. (a) 7  If: C (-6,0) (a) 14	(b) 13 (b) 13 (c) D (0, 8), then C (d) 10	(c) 17 (D =length	12) = ······ length  (d) 10  unit.  (d) 2
## 28 ## 28 ## ## 29 ## ## ## ## ## ## ## ## ## ## ## ## ##	The distance bunits.  (a) 7  If: C (-6,0)  (a) 14  The distance bunits.  (a) 2	(b) 13  (b) 10  (b) 10  (c) (d) (etween the point (2)	nts (5,0) and (0,-  (c) 17  (D =length (c) 5  (c) 3	12) = ······ length  (d) 10  unit.  (d) 2  quals ····· units length

Mc Mc	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term	H # # # # # # # # # # # # # # # # # # #	
31	The distance between the (a) 5 (b) 2		x-axis = length unit. $(d) - 3$
# 32 # 32			s equalslength unit.
9	Distance between point (2) (a) 2 (b) -3	2, -3) and y-axis = (c) $\sqrt{13}$	length units. $ (d)\sqrt{5} $
34	The distance between the p (a) 3 (b) 4		in point equals(d) 7
35	The distance between the p  (a) 2  (b) -		gin point islength unit.
36	The distance between the point (a) 2 (b) -2		equals $\sqrt{5}$ , then $a = \cdots$
		line passing through the tv	wo points $(2, -1)$ and $(6, 3)$ is ure 45° with the positive direction  (Kafr El-Sheikh 2011)
		التعلم التفاعلي عر	تطبیق
		#### <b>#</b> ###############################	تطبيق مذكرات باهزة للطباعة    App Štore

	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term	<b>3</b>
	If the straight line $L_1$ passes through the two points (3 , 1) and (2 , k) and the straight line $L_2$ makes with the positive direction of the $X$ -axis an angle whose measure is 45°, then find k if the two straight lines $L_1$ and $L_2$ are : (1) parallel (2) perpendicular (Aswan 2014) $\ll 0$ , 2	
5		
3	If the points $(0, 1), (A, 3)$ and $(2, 5)$ are located on one straight line.	
<b>3</b>	Then find the value of A (El-Gharbia 2014) « 1	<b>»</b>
3		[
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3 3	GPS-APP	[
<b>3</b>	تطبيق التعلم التفاعلي عن بعد	(i
4	$\square$ If A $(-1,-1)$ , B $(2,3)$ and C $(6,0)$ , prove that: the triangle ABC is	
	a right-angled triangle at B (Suez 201	4)
		[
<b>8</b>		[
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	Prove by using the slope that the points $A(-1,3)$ , $B(5,1)$	), $C(6,4)$ and
	D (0, 6) are the vertices of the rectangle ABCD	(Beni Suef 201
	Ω T. Al. 1 . C	D
6	In the drawn figure: ABCD is a trapezoid where $\overline{AB} / / \overline{CD}$ , A (9, -2), B (3, 2)	
	, C $(X, -X)$ and D $(4, -3)$	/
	Find the coordinates of the point C	A
		(Alex. 2014) « (1 • – 1)
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	and the second s	تطبيق مذكرات جاهزة للط
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# **Sheet (15)**

# The Equation of the Straight Line Given its Slope and the Intercepted

**First** 

Finding the slope of a straight line and the length of the intercepted part from y-axis.

If the equation of a straight line in the form: y = m x + c, then:

- The slope of the straight line = m
- -The length of the intercepted part from y-axis = |c| and it passes through the point (0, c)

## For Example : -

• The straight line whose equation is  $y = \frac{1}{2} x + 7$  its slope =  $\frac{1}{2}$ 

and the intercepted part from y-axis = 7 length units and passes through the point (0,7)

• The straight line whose equation is  $y = 3 \times -5$ , its slope = 3 and cuts from the negative side of y-axis a part of 5 length units and passes through the point (0, -5)

## Remarks

If the equation of a straight line in the form :  $a \times b + b + c = 0$ 

then the slope of the straight line =  $\frac{-\text{coefficient of } x}{\text{coefficient of y}}$ 

and the straight line cuts y-axis at the point  $(0, \frac{-c}{b})$ 

*i.e.* The length of the intercepted part from y-axis =  $\left| \frac{-c}{b} \right|$ 

### For Example: -

The straight line whose equation : x - 2y + 3 = 0Its slope =  $\frac{-1}{-2} = \frac{1}{2}$  and cut y-axis at the point  $(0, \frac{3}{2})$ 

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		<i>i.e.</i> The straight line intercepts a part of length equals $\frac{3}{2}$ length unit from the positive
		side of y-axis.
	2	The straight line whose equation : $3 X + y + 4 = 0$
		Its slope = $-3$ and cut y-axis at the point $(0, -4)$
		i.e. The straight line intercepts a part of length equals 4 length units from the negative
# # # # # # # # # # # # # # # # # # #		side of y-axis.
		Second Finding the equation of the straight line given its slope
		and the length of intercepted part of y-axis
	The	straight line whose slope = m and cuts y-axis at the point $(0, c)$ its equation is in the form:
	y =	= m X + c
	_	
		The equation of the straight line which passes through the origin point $O(0,0)$
#		is $y = m x$ , where m is the slope of the straight line.
#	2	The equation of $x$ -axis is $y = 0$ The equation of $y$ -axis is $x = 0$
#	4	The equation of the straight line parallel to $x$ -axis and passes through the point
#		$(0, \ell)$ is $y = \ell$
	5	The equation of the straight line which is parallel to y-axis and passes through the
#		point $(k, 0)$ is $\chi = k$
		GPS-APP
		Choose the correct answer:
	1	تطبيق التعلم التفاعلي عن بعد
	•	The straight line whose equation is $2 X - y + 4 = 0$ intercepts a part from y-axis of length units.
		(a) $-4$ (b) 2 (c) $-1$ (d) 4
	•	
20 20 20 20 20 20 20 20 20 20 20 20 20 2	2	The straight line whose equation is $y = 2 \times -6$ intercepts from the y-axis a part of
# #		length unit.
#		(a) $-6$ (b) $-3$ (c) 2 (d) 6
#	3	The straight line whose equation is $y = \frac{2}{3} x + 2$ intercepts from the y-axis
#		a part of length length unit.
**		(a) $-6$ (b) $-2$ (c) $\frac{2}{3}$ (d) 2
		10 W W W W W W W W W W W W W W W W W W W
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4			s: $5 y = 2 X + 10$ into length unit. (c) 2	ercepts a part from y-axis, $(d) 2\frac{1}{2}$
5	The straight line a part of length		s: y-3 X=6 interc	epts from the y-axis
	(a) 6	(b) 2	(c) 3	(d) $-\frac{1}{3}$
6	* The straight li		6 intercepts from the	y-axis a part of length
	(a) 3	(b) 4	(c) 5	(d) 16
7	The length of the		f y-axis by the straig	ht line $y = 5 X - 4$ equal
	(a) 1	(b) 5	(c) 4	(d) 9
8	The straight line (a) (1,0)	-	y = X passing through (c) $(0, 0)$	
9	The equation of to X-axis is		nat passes through the	e point (1,3) and paralled
	(a) $X = 1$	(b) $X = 3$	(c) $y = 1$	(d) $y = 3$
10	_		hich passes through th	The state of the s
	(a) $X = -2$	(b) $y = -3$	ق التعلم التفاع (c) <i>X</i> = 2	(d) $y = 3$
11 11	The equation of is	the straight line	which passes through	n (– 7 , 2) parallel to y-axis
	(a) $X = 2$	(b) $X = -2$	(c) $y = 7$	$(d) \ \mathcal{X} = -7$
12 22 23 24 24 25 26 26 26 26 26 26 26 26 26 26 26 26 26	an angle of mea	sure 45° with the	positive direction of	
	(a) X = 1	(b) y = 1	•	لطبيق مذكرات جاهزة للطباعة على موجاياك الأندرويد أو الأيفوز (App Store ﴿ وَ الْ وَ وَ الْ وَ الْ الْ يَفُوزُ ( الله على موباياك الأندرويد أو الأيفوز ( py2day.com - ممثل التطبيق على موباياك الأندرويد أو الأيفوز

	athematics 3 <sup>rd</sup> Prep	1 <sup>st</sup> term			
33 33 33 34 35 36 37 38	The equation of the straight line when its slope equals 5 and intersects a positive part from the y-axis that equals 7 units is				
<b>8</b>	(a) $y = 5 X - 7$	(b) $y = 7 X + 5$	(c) $y = 5 X + 7$	(d) $y = 7 x - 5$	
# 14 # 14	The equation of th	ne straight line whose	slope is 1, passes the	rough the origin point	
	(a) $X = 1$	(b) $y = 1$	(c) $y = X$	(d) y = -X	
# 15	The equation of the point is	he straight line whose	slope = 2 and passes	through the origin	
# # # #	(a) $X = 2$	(b) $y = 2$	(c) $y = 2 X$	$(d) y = \frac{1}{2} x$	
# 16 # # # # # # # # # # # # # # # # # # #		traight line whose equ $(b) \frac{-a}{c} \qquad (a)$		= 0 is	
<b>**</b>	Essay prob	lems:		<b>₹</b>	
# 1		of the s <mark>traigh</mark> t line if :		<b>(8</b>	
		d intercepts from the p	ositive part of y-axis	7 units. (Suez 2015)	
<b>3</b>		2		<u>8</u>	
<b>33</b>					
**************************************		C D C	4.55		
<b>*</b>	GPS-APP				
<b>**</b>		نفاعلي عن بعد	طبيق التعلم الا		
# 2	Find the equation	of the straight line :		<u> </u>	
**************************************		of length 3 units from that ion: $2 \times x - 3 = 6$	he negative part of y-a	axis and is parallel to (El-Beheira 2011)	
<b>33</b>					
<b>3</b>					
***					
## ##					
## ## ##					
# ####################################		####### 147	で		
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	Ma	thematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>B####################################</b>
	3	Which passes through the point (2, -1) and its slope equals 2 (El-Kalyoubia 2011)
	4	Passing through the point $(-2,3)$ and perpendicular to the straight line whose equation : $y = \frac{1}{2}x - 5$ (El-Dakahlia 2013)
	5	Passing through the point (3, -5) and it is parallel to the straight line: $x + 2y - 7 = 0$ (Alexandria 2015)
<b>9</b>	6	Which passes through the point (3, 2) and parallel to the straight line passing through the two points (5, 6) and (-1, 2)  (Helwan 2009)  (Helwan 2009)

	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>Bassassassassassassassass</b>
*** <b>7</b> ********************************	Passing through the point (1, 2) and perpendicular to the straight line passing through the two points A (2, -3) and B (5, -4)  (Red Sea 2013 – El-Gharbia 2014)
8	Passing through the point $(2, -2)$ and perpendicular to the straight line which makes an angle of measure 45° with the positive direction of $X$ -axis (Luxor 2011)
\$\\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\	Which passes through the two points (2, -1) and (1, 1) (El-Gharbia 2013)  Choose the correct answer:
######################################	Choose the correct answer:  The slope of the straight line parallel to the straight line $y + 2 = 0$ equals
# 2 # 2 # # # # # # # # # # # # # # # #	

<b>33</b>	Ma	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>B</b> ###			<b>#</b>
<b>33</b>					<b>8</b>
	3	1 0	_	_	<b>8</b>
<b>88</b>		(a) 5 $(b) - 3$	(c) $\frac{5}{3}$	(d) $\frac{3}{5}$	8
	_				
	4	The slope of the straight line whose ed	quation: $2 \times -3 \text{ y}$	+ 5 = 0	8
<b>33</b>		(a) $\frac{-3}{2}$ (b) $\frac{-2}{3}$	(c) $\frac{2}{3}$	(d) $\frac{3}{2}$	<b>8</b>
		2 3	3	Z	8
##   ##   ##   ##   ##   ##   ##   ##	5	The slope of the straight line : $2 y = 6$	X + 1 is		<b>3</b>
		(a) $\frac{1}{3}$ (b) 3	(c) - 3	$(d) - \frac{1}{3}$	8
<b>33</b>		3		3	<u> </u>
<b>33</b>	6	The slope of straight line which is perpen	dicular to straight li	ine: $2 X + 3 y = 1$ is	8
<b>33</b>		(a) $\frac{2}{3}$ (b) $\frac{-2}{3}$	(c) $\frac{3}{2}$	$(d)\frac{-3}{2}$	8
		3	2	2	<b>8</b>
	7	The straight line whose equation is: 3	x - 3y + 5 = 0  m	nakes a positive angle with	<b>(4)</b>
		the positive direction of X-axis, its m		(El-Monofia 2011)	8
		(a) 30° (b) 45°	(c) 60°	(d) 90°	8
		(a) 30	(0) 00	(d) 90	<u> </u>
	8	If the the straight line $y = x \sin 30^\circ$	+ c passing throu	gh point (4,6),	
		then c =			8
			(0) 4	(4) 6	<b>8</b>
***		(a) $5$ (b) $-4$	(c) 4 2024	(d) 6	8
	9	If the straight line a $x - 4y = 1$ its s	lone equals 1 . f	hen a —	<b>8</b>
		(a) $-8$ (b) $-2$			8
		$(a) - 6 \qquad (b) - 2$	(c) 2	(d) 8	<u>8</u>
	10	If the straight line whose equation : $x$	1.3 y 6 = 0 is par	mandianlar to the	
**		line whose equation: a $x - 3y + 7 = 0$			8
				O	<b>8</b>
		(a) 2 (b) 9	(c) 4	(d) 1	8
<b>33</b>	11	If the straight line whose equation is	v = (a 1) v . 5:	e parallel to the etraight line	<b>1</b>
	•	If the straight line whose equation is:			•
		which passes through the two points (	1 , 2) and (3 , 6) ,		8
		() (		(El-Sharkia 2009)	•
		(a) 3 (b) 4	(c)-4	(d) 7	<b>₹</b>
<b>88</b>	12	If the two straight lines : $X + y = 5$ and	nd k Y + 2 v - 8 a	are both parallel	8
	• -	then $k = \cdots$	10 K A + 2 y - 0 a	are both paramer 7	8
			(-) 1	(4) 2	<b>8</b>
		(a) $-2$ (b) $-1$	(c) 1	(d) 2	8
<b>33</b>					<b>8</b>
					<b>8</b>
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# # # 13	M 164	4 2 0 11 1	4 8 0 0 0 0		
# 10 # 10	If the two straight lines: $3 \times 10^{-1}$ perpendicular, then $k = 10^{-1}$	-4y - 3 = 0 and $ky + 1$	$4 \times - 8 = 0$ are  (El-Fayoum 2011)		
## ## ##	(a) $-4$ (b) $-3$	(c) 3	(d) 4		
## ##	(0) 3	(6) 3	(4) 4		
<b>14</b>	The two straight lines : $y = a X +$	b and $y = c X + d$ are p	erpendicular,		
*** ***	then $\cdots = -1$		(El-Gharbia 2008)		
**	(a) $a \times d$ (b) $b \times$	c (c) $a \times c$	$(d) b \times d$		
# 15	Area of triangle bounded by straigh	ht lines $x = 0$ , $y = 0$ , 2	X + 3 y = 6 equals		
# #	(a) 6 (b) 5	(c) 4	(d) 3		
# # 16	☐ The area of the triangle in squ	uara unite which is bour	aded by the straight lines		
# #	3 $x - 4$ y = 12, $x = 0$ , y = 0 equ		(El-Sharkia 2012)		
# # #	(a) 6 (b) 7	(c) 12	(d) – 6		
## ##			<u>₹</u>		
# #1	Essay problems:		(1) (1) (1) (1) (1) (1) (1) (1) (1) (1)		
*** 4	Find the equation of the straigh	t line if			
**					
**		vo points $(4, 2)$ and $(-$	-2, $-1$ ) then prove that it passes		
	through the origin point.	0000	(Suez 2015 – Dakahlia 2012)		
**		2024			
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**					
	Which passes through the midp	oint of the line segmen	$ nt \overline{AB} \text{ where A } (3,6) $		
# #	and B $(-1, 4)$ and perpendicula	ar to the straight line v			
**	2y - 4X + 11 = 0		(Cairo 2009)		
***					
<b>**</b>			<u>8</u>		
**			<b>a</b>		
**					
# #					
**					
**					
<b>**</b>	1		تطبيق مذكرات باهزة للطباعة		
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<b>33</b>	Mc	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>Bassassassassassassassassassas</b>	<b>(8</b>
	3	<b>Prove that :</b> The straight line $\overrightarrow{AB}$ is parallel to the straight line whose equation :	
# # #		X - 2y + 8 = 0 where A (2, 3) and B (-2, 1) (El-Fayoum 2011)	
# #			
# # #			
# # #			
# #			
# # #			
**	4	<b>Prove that :</b> The straight line whose equation : $2 X + y + 8 = 0$ is perpendicular to the	
## ##		straight line passing through A $(2,3)$ and B $(-2,1)$ (Aswan 2012)	
**			
** ** **			
## ## ## ## ## ## ## ## ## ## ## ## ##			
		2024	
# #			
<b>**</b>	5	If the straight line whose equation: $2 \times -3 \times -6 = 0$ cuts the X-axis at point A and the	8
		y-axis at point B, find:  (El-Sharkia 2013)  (1) The coordinates of two points A and B	
**		(2) The equation of the straight line passing through the midpoint of $\overline{AB}$ and parallel to	
## ##		the y-axis.	
**			
## ## ##			
<b>**</b>			
## ## ##			
***			
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(M	athematics 3 <sup>rd</sup> Prep 1 <sup>st</sup> term <b>3000000000000000000000000000000000000</b>
6	If the straight line whose equation: a $x + 2y - 3 = 0$ is parallel to the straight line which passes through the two point $(2, 3), (1, 5)$ which lie on the same plane, then
	find the value of a (Souhag 2013) « 4 »
7	Find the equation of the axis of symmetry of $\overline{XY}$ , where X (3, -2) and Y (-5, 6)
·	(El-Dakahlia 2012 – Port Said 2014)
	(Bi Bananina 2012 - 1 ori Sala 2011)
	2.024
	GPS-APP
8	Find the equation of the straight line which intercepts from the positive parts of the
	coordinate axes «x-axis and y-axis» two parts of lengths 4 and 9 length unit respectively.
	(Assiut 2012)
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